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Fluorescence- and Reflection Spectroscopy of Industrially Relevant Minerals for Automatic Sensor Based Sorting Applications

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To my family.

Abstract

In the present work reflection- and fluorescence spectra of industrially relevant minerals were recorded and interpreted. Reflection spectra were measured with the Lambda 950 system of Perkin Elmer. The first and second derivatives of the spectra can be used to find spectral features which allow a classification of the materials in optical sorting. As sample set for reflection spectra Bauxite, Magnesite, Talc, Fluorite, Calcite, Chalcedony and Barite were chosen. For all chosen samples reflection data of good quality were obtained.

The measurement of fluorescence emission spectra with the LS 55 system of Perkin Elmer turned out to be more difficult. Because of the fact, that there is a certain pulse to pause ratio of the excitation source, a Xe-flashlamp and many internal data processing steps more operator knowledge is required. As sample set for the fluorescence emission spectra Fluorite, Calcite, Magnesite, Chalcedony, Silicon, CAB 15¹ and a commercially available lead doped glass (referred to as PbO reference glass 1) were chosen.

The illumination situation in the LS 55 instrument was investigated and compared to industrial laser illumination technologies. A semi-quantitative approach for comparing emission intensities of different samples is proposed and compared to a reference system for absolute Quantum Yield detection (Hamamatsu Quantaurus).

Furthermore a short overview of possible reflection and fluorescence databases on minerals available in the internet, literature on fluorescence of minerals and a short theoretical introduction to the field of solid state chemistry and solid state spectroscopy of minerals and solids are provided.

Zusammenfassung

In der vorliegenden Arbeit wurden Reflektions- und Fluoreszenzspektren von Industriemineralien gemessen und interpretiert. Die Reflektionsspektren konnten leicht mit dem Lambda 950 Reflektionsspektrometer von Perkin Elmer aufgezeichnet werden. Mit Hilfe der ersten und zweiten Ableitungen der Rohspektren konnten einige spektrale Eigenschaften zur Unterscheidung der Mineralien gefunden werden, die ein optisches Sortieren ermöglichen. Als Auswahl an Industriemineralien wurden Bauxit, Magnesit, Talk, Fluorit, Calcit, Chalcedon und Barit verwendet. Für all diese Proben konnten Reflektionsdaten in guter Qualität erhalten werden.

Die Fluoreszenzmessung mit dem LS 55 von Perkin Elmer an den ausgewählten Proben stellte sich als etwas problematischer heraus. Das Puls- zu Pause Verhältnis der Xe-Blitzlampe und geräteinterne Datenprozessierungsschritte müssen bei den Messungen berücksichtigt werden. Fluorit, Calcit, Magnesit, Chalzedon, Silizium, CAB 15² und ein handelsübliches Bleiglas wurden als Proben für die Fluoreszenzmessung verwendet.

Die Beleuchtungsverhältnisse im LS 55 wurden untersucht und mit industrieller Lasertechnologie verglichen. Für den Vergleich der relativen Fluoreszenzintensitäten verschiedener Proben wurde eine semiquantitative Methode vorgeschlagen und mit Ergebnissen einer absoluten Quantenausbeutemessung (Hamamatsu Quantaurus) verglichen.

Einige im Internet zugängliche Fluoreszenz- und Reflektionsdatenbanken für Mineralien, Literatur zur Mineralienfluoreszenz und eine kurze theoretische Einleitung zu Festkörperchemie und Festkörperspektroskopie an Mineralien anderen Festkörpern sind in der Arbeit zu finden.

¹ CAB 15 is an artificial lead doped calcium aluminum borate glass

² CAB 15 ist ein künstlich hergestelltes mit Blei dotiertes Calcium-Aluminium-Boratglas

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STATUTORY DECLARATION

I declare that I have authored this thesis independently, that I have not used other than the declared sources/resources, and that I have explicitly marked all material which has been quoted either literally or by content from the used sources.

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List of Symbols and Abbreviations

| a.u. | arbitrary units (for fluorescence intensities) |
|----------|---|
| CCD | charge coupled device |
| cf | crystal field |
| EM | Electromagnetic radiation |
| Emfilter | Emission filter |
| Emslit | Emission slit of the fluorimeter |
| EPR | Electron Paramagnetic Resonance (Spectroscopy) |
| EUV | extreme UV part of the EM spectrum with a wavelength of 100 -10 nm |
| Exslit | Excitation slit of the fluorimeter |
| FIR | Far infrared part of the electromagnetic spectrum. It is the region of wavelengths between $50 - 1000 \ \mu m$. |
| FWHM | full width at half maximum |
| LIBS | laser induced breakdown spectroscopy |
| MIR | mid infrared part of the electromagnetic spectrum It is considered as the region between $4000 - 400$ cm ⁻¹ (about a wavelength of $3 - 50$ µm) and is often used for structure determination in chemical syntheses. |
| MUL | Montanuniversität Leoben |
| NIR | Near infrared part of the electromagnetic spectrum. In the present work wavelengths from 780 nm to 2500 nm are considered as NIR-region, because no experiments with radiation over 2500 nm were carried out. |
| NMR | Nuclear Magnetic Resonance (Spectroscopy) |
| REE | rare earth element |
| TIR | Thermal Infrared Reflection |
| U | electrical voltage |
| UV | The ultraviolet part of the electromagnetic spectrum. In the present work wavelengths from 200 nm to 380 nm are considered as UV-region, because no experiments with radiation beneath a wavelength of 200 nm were carried out. |
| UV-C-FUV | far UV part of the electromagnetic spectrum with wavelengths of $280 - 200$ nm |

- UV-C-VUV vacuum UV part of the EM spectrum with wavelength of 200 100 nm
- TS Tanabe Sugano (abbreviation used for the term "Tanabe-Sugano diagrams")
- VIS the visible part of the electromagnetic spectrum: 380 nm to 780 nm
- XRF X-ray fluorescence
- XRT X-ray transmission

1 Introduction

1.1 Background

The present master thesis is part of a research project initiated by the local company Binder + Co with the aim to develop a flexible optical sensor based sorting system for a wide range of minerals and ores. In the frame of the thesis a representative sample set had to be compiled and optically characterized in terms of reflection- (UV-Vis-NIR) and luminescence spectra (UV-Vis).

The research project hast the intern name Minexx UV/Vis/NIR or Minexx Plus, based on the Minexx mineral sorting system, manufactured by Binder + Co.

The whole research project is carried out by the three project partners [14]:

- Binder + Co
- Montanuniversität Leoben (MUL)
- Graz University of Technology (TUG)

Those three organizations provide project-relevant know how and resources in their special field of expertise [85]:

- Binder + Co:
 - o Know-how concerning the limits of VIS-sorting for industrial relevant materials.
 - o Applications.
 - Employer of the project.
- MUL:
 - o Process technological know-how.
 - o Knows the shortcomings and problems with actual processes and separation procedures.
 - Provides information where in the process a sensor based sorter can be placed.
 - o Contacts to mining industry.
 - o Deposit know-how.
 - Higher degree of professionalism by using the correct language e.g. "Tailings", "Veinstuff", and so on.
 - o Mine run analysis via classical conditioning methods.
- TUG:
 - Know how concerning structural chemistry/lattice structure of the minerals of interest (Solid State Chemistry)
 - Kow-how in the area of optical effects and spectroscopic background (Solid State Spectroscopy)
 - Spectroscopic fundamental studies for Binder + Co (2009 until today)
 - o Database research concerning spectroscopic data bases.

1.2 Sorting and Beneficiation Technologies

There is a vast variety of beneficiation technologies on the market. The present work deals with fundamental research on optical sorting of minerals, glasses and other secondary raw materials.

Different traditional principles for material sorting are known [1]:

- Free settling: Sinking of particles in a volume of fluid which is large with respect to the total volume of particles, hence particle crowding is negligible. The particle density plays an important role in this sorting technology.
- **Hindered settling:** As the proportion of solids in the pulp increases, the effect of particle crowding becomes more apparent and the falling rate of the particles begins to decrease. The system begins to behave as a heavy liquid whose density is that of the pulp rather than that of the carrier liquid. This process is also based on particle density in comparison to the liquid.
- **Hydraulic classification:** The feed stream and additional fresh water are pumped through a cascade of columns. The direction of flow opposes that of the settling particles. The rising currents are graded from a relatively high velocity in the first sorting column, to a relatively low velocity in the last, so that a series of spigot products can be obtained.
- Hydrocyclones: Centrifugal force is used to accelerate the settling rate of particles.
- **Gravity concentration:** Specific heavier minerals are sorted from specific lighter ones by a liquid of intermediate density.
- Froth flotation: Different surface properties of the minerals and the gangue are used for separation. Three phases are encountered: solids, water and froth. Often the froth as "mineralized froth" contains the valuable content of the feed. Different collectors-agents, from a chemical point of view tensides and soaps are in use to create the desired froth. Furthermore it can be distinguished between activators (increasing the hydrophobicity of mineral surfaces) and depressants (increasing hydrophilicity of certain mineral fractions).
- **Magnetic separation:** Materials are sorted according to their magnetic properties. All materials can be subdivided into *diamagnetics* and *paramagnetics*. Diamagnetics are repelled from magnetic fields. This interaction is, however, rather small and cannot be used for sorting purposes. Paramagnetics (in particular ferromagnetic materials) are attracted by magnetic fields. There are several examples for commercial sorting of paramagnetic minerals. Magnetic separations can be furthermore subdivided into low-intensity and high intensity separating technologies with a threshold of 2 Tesla magnetic flux density.
- Electrical separation: This technology takes advantage of the different electric conductivities of minerals and gangue.
- Electronic sorting principles: The stream of minerals contaminated with gangue or other minerals is automatically separated using the response of a sensor. Different fundamental interactions of light with matter like reflectance, color in the VIS region of the electromagnetic spectrum, natural γ-radiation, X-Ray luminescence, IR-, Raman- or microwave attenuation are in use.

However, all those classification techniques can be broken down to physical or physico-chemical interactions and fundamentals.

1.3 Mineral and Glass Sorting

This work deals with the possibilities and fundamentals of sensor based sorting of minerals and glasses. As Kieler [2] has shown in her diploma thesis luminescence of lead doped glasses can easily be measured in UV-VIS range and hence can be used in optical sorting machines. An implementation of this basic phenomenon was made in the "CLARITY lead" system of Binder + Co, which has a capacity of up to 14 t/h [3]. A source for fundamental research data at pilot plant scale for sorting of fluorescent minerals is provided by Ören [5].

When either too low concentrations of a luminophor or concentration quenching effects for too high concentrations suppress luminescence signals, another useful tool can be the UV or NIR cut-off of the materials. Fundamental research of this useful topic was provided by Ohnewein [4].

A good technological overview of available sensor systems for optical sorters was provided by Wotruba and Kleine in 2010 and is reproduced in table 1 [6].

| Sensor | Material Property | Application | |
|-----------------------|-----------------------------------|------------------------------------|--|
| Radiometric | Natural Gamma Radiation | Uranium, Precious Metals | |
| XRT | Atomic Density | Base/ Precious Metals, Coals | |
| Energy dispersive XRF | Elemental Composition | Base/ Precious Metals | |
| XRF | Visible Fluorescence under X- | Diamonds | |
| | Rays | | |
| VIS | Reflection/ Absorption of Visible | Metals, Industrial Minerals, Gem | |
| | radiation | Stones | |
| CCD Color | Color, Reflection, Brightness, | Base/ Precious Metals, Industrial | |
| | Transparency | Minerals, Gem Stones | |
| Photometric | Monochromatic Reflection, | , Industrial Minerals, Gem Stones | |
| | Absorption | | |
| NIR | Reflection/ Absorption of NIR | R Base Metals, Industrial Minerals | |
| | Radiation | | |
| TIR | Microwave Excitation and | d Base Metals, Precious Metals | |
| | Thermal Infrared Reflection | | |
| LIBS | Emitted radiation of the plasma | Al-alloy sorting, all kinds of | |
| | generated by a focused pulse | homogeneous materials because a | |
| | laser | the small measurement spot | |

Table 1: Available detection systems, materials property and application according to [6]

Direct sorting criteria for minerals are defined as directly linked to the main elemental or mineralogical content. Therefore sensor techniques based on direct sorting criteria are XRT, XRF, NIR-spectroscopy and LIBS. NIR-sorting is based on the measurement at the surface, whereas XRT-sorting works with electromagnetic radiation penetrating the minerals. The attenuation of the radiation is measured in the latter technique. LIBS sensors measure the elemental composition of a small area of about $< 1 \text{ mm}^2$ of the sample. The emission of the plasma generated via a laser is analyzed and used for sorting [7].

1.4 Minerals

1.4.1 Origin and Definitions

Minerals are by definition substances that are naturally occurring parts of the earth or other celestial bodies, and can be represented by a chemical formula. Most of the minerals (with only a few exceptions) are inorganic, solid and crystalline [8]. Exceptions from this rule are for example naturally occurring mercury (Hg), opal (SiO₂·nH₂O) and vitreous silica (SiO₂) [10].

The origin of terrestrial minerals is mostly based on inorganic processes. There are, however minerals whose origin is found in biologic activities of certain organisms. A good example for a mineral of biologic origin is Apatite, which builds up teeth and bones of vertebrates. Minerals build up rocks and stones. Earth's mantle and earth's core as well as the moon and other celestial bodies can be considered to consist of minerals, even though their constitution is not exactly known or purely hypothetic [8].

A rock is defined as a solid aggregate of minerals. While the breakdown of a mineral leads to smaller parts of the same chemical and crystallographic composition, the breakdown of a rock leads to inhomogeneous parts. A common example for a rock is granite, which is a mixture of feldspar, biotite and quartz. There are rocks with one specific mineral (e.g. marble with CaCO₃) and rocks with more than one specific mineral (e.g. granite) [12].

Different classifications of minerals and rocks according to their genesis are known [9]:

- Igneous Rock
- Metamorphic Rock
- Sedimentary Rock

However, some minerals are formed stepwise via a combination of these three processes.

Igneous rocks are formed by solidification of molten fluids, generated in the earth's crust under high pressure and temperature. When these rocks undergo natural breakdown processes like weathering or transportation by streams to form beds of clay, sand and finally deposits of new minerals, they are called sedimentary rocks. When these sedimentary rocks undergo high pressure and temperatures which lead to changes in chemical composition or crystal structure metamorphic rocks are formed [11].

Ores are defined as aggregates of minerals or rocks of ore minerals, which have significant concentrations of metals or nuclear fuels like Uranium or Thorium. Ores can be subdivided as follows into classes with certain elements of interest [13]:

- Ores of ferrous metals (iron and elements which are used for steel refining): Fe, Mn, Ni, Co, Cr, V, Ti, Mo, Re, W, Nb, Ta, Zr, Hf, Te
- Ores of non-ferrous metals (base metals): Cu, Pb, Zn, Cd, Sn, Hg, As, Sb, Bi, Ga, In, Tl, Si, Ge
- Ores of light metal: Al, Mg, Be
- Ores of precious metals: Au, Ag, Pt and Pt-metals, Ru, Rh, Pd, Os, Ir
- Ores of Lanthanides (rare earth elements)
- Ores of Actinides (reactor fuels): Uranium, Thorium, Radium

1.4.2 Chemical Properties, Symmetry and Classification according to Struntz

Minerals usually are crystals. A possible definition of a "crystal" is: Crystals are solid, homogeneous and anisotropic bodies with a three-dimensional periodic arrangement of their chemical components (atoms, ions or molecules). These components build up what is called a crystal lattice. This lattice leads to the anisotropic properties of the crystal, which means that physical properties like the refractive index can vary in different directions [14].

When the lattice is visualized as a regular arrangement of points three lattice vectors can be found with the lengths of a, b and c. The three lattice vectors include the three angles α , β , and γ . This lattice vectors define the so-called unit cell of a crystal. It can be considered as the smallest repeat-unit which upon continuous duplication along the directions of the lattice vectors reproduces the complete crystal lattice. In 1845 Bravais defined 14 Bravais lattices in 7 crystal systems which turned out to be sufficient to describe the structures of all crystalline solids [16]. The 14 Bravais lattices are depicted in figure 1.

| | С | rystal Systems | Bravais Lattices |
|--------------|-------------------|--|---|
| Structure | Axes | Angles between the Axes | |
| Cubic | a = b = c | all angles equal to 90° | simple, face centered, body centered |
| Tetragonal | $a = b \neq c$ | all angles equal to 90° | simple, body centered |
| Orthorhombic | $a \neq b \neq c$ | all angles equal to 90° | simple, body centered, base centered, face centered |
| Hexagonal | $a = b \neq c$ | two angles equal to 90°, one angle equals 120° | hexagonal |
| Trigonal | a = b = c | all angels are equal and none equals 90° | rhombohedral |
| Monoclinic | $a \neq b \neq c$ | one angle (β) not equal to 90° | simple, base centered |
| Triclinic | $a \neq b \neq c$ | all angles are different and none equals 90° | triclinic |

 Table 2: Characteristics of the 7 crystal systems and 14 Bravais lattices [17]

After the type of the Bravais lattice is determined the points of the corresponding unit cell have to be filled with atoms or small groups of atoms generating the structure of the unit cell. This is called the basis. The basis builds up the unit cell of the crystal and the unit cell is the smallest repeating unit of the crystal itself. After considering the symmetry of both, the basis and the lattice, the crystal can be sorted into one of 32 point symmetry groups and of 230 possible space groups [18].



Figure 1: 14 Bravais lattices [126]

To understand crystal morphology of minerals and artificial crystals one has to know about symmetry. Symmetry operations are defined as operations which lead to arrangements of the atoms which are indistinguishable from the starting arrangement. These operations can be purely hypothetical in the sense of physical feasibility [15].

For every molecule or unit cell a list of possible symmetry operations can be found. According to this list a molecule can be assigned to a certain *point group*. Only operations corresponding to symmetry elements that intersect at least in one point of the molecule are taken into consideration – this specific point of a molecule is its center of gravity. Thus the term "point" group is used. For the classification of crystals translational symmetry has to be taken into account. Therefore for crystals the term *space group* is used. Every symmetry operation is linked to a symmetry element, e.g. the point, line or plane with respect to which the symmetry operation is carried out. There are two different notations for symmetry elements known: Schoenflies notation and the Hermann-Mauguin notation (also known as International notation system) which are compared in table 3 [19].

| Symmetry operation | Schoenflies | Hermann-Mauguin | Comment |
|--------------------------|--------------------------------|----------------------------|--|
| unity | Е | 1 | Necessary for the mathematical description of symmetry. It is a neutral |
| | | | element and equal with doing nothing. |
| n-fold rotation | C_n with $n = 1, 2, 3, 4, 6$ | n with $n = 1, 2, 3, 4, 6$ | Rotation about an axis with an angle $2\pi/n$ |
| reflection | σ | m | Reflection on a mirror plane |
| inversion | i | Ī | Inversion through a center of symmetry |
| n-fold improper rotation | S _n | with n = 3,4,6 | Also called "rotary reflection"; or equivalently "rotary inversion"; n-fold rotation followed by a reflection on a plane perpendicular to the n-fold axis. |

Table 3: Comparison of Schoenflies notation and Hermann-Mauguin notations for symmetryoperations [19, 20]

However, in contrary to molecules in crystals there are three more symmetry elements: *pure translations*³ of the unit cell with the value of the lattice constant, *screw axes*⁴ which rotate a part of the cell around an axis and then translate parallel to the axis and *glide planes*⁵ which reflect a part of the cell through a plane and then translate it parallel to the plane [21].

³ German: Translation (einfache Verschiebung um einen bestimmten Wert)

⁴ German: Schraubenachse

⁵ German: Gleitspiegelebene

Atoms in crystals arrange themselves in a certain way. Helpful tools to understand the arrangement of ions in solids are Pauling's rules [26] for ionic structures (even though there are many exceptions known today):

- 1. A coordinated polyhedron of anions is formed about each cation, the cation-anion distance is determined by the radius sum and the coordination number of the cation by the radius ratio.
- 2. In a stable coordination structure the electric charge of each anion tends to compensate the strength of the electrostatic valence bonds from the cations at the centers of the polyhedra of which it forms a corner.
- 3. The presence of shared edges, and particularly of shared faces, in a coordinated structure decreases its stability; this effect is large for cations with large valence and small coordination number, and is especially large in case the radius ratio approaches the lower limit of stability of the polyhedron.
- 4. In a crystal containing different cations those with large valence and small coordination number tend not to share polyhedron elements with each other.
- 5. The number of essentially different kinds of constituents in a crystal tends to be small.

In all packing types of atoms there are small holes between the atoms. Into these holes smaller atoms can be positioned. For example in a FCC (face centered cubic) unit cell there are four octahedral and eight tetrahedral sites for including atoms [24].

Since ideal crystals have a higher free energy than crystals with imperfections there are no perfect crystals in nature. The Gibbs free energy of every crystal encountered is lowered via increase of entropy, which means disturbance of the perfect order [22].

The Gibbs energy ΔG of a crystal is defined as:

$\Delta G = \Delta H - T \,\Delta S \qquad Equ. 1$

with ΔH the enthalpy of formation, T the temperature and ΔS the entropy associated with the large number of positions that a defect can occupy. Since ΔH increases linearly with the defect concentration and $-T \Delta S$ decreases, a minimum of ΔG can be reached with a certain concentration of defects [27].

Point defects are defined as localized disruptions in perfect atomic or ionic arrangements in a crystal structure. Point defects are [23]:

- vacancy
- interstitial atom
- small substitutional atom
- large substitutional atom
- Frenkel defect (a smaller ion is displaced from its original position to an interstitial site, a vacancy defect is created in its original position, while creating an interstitial on its new place)
- Schottky defect (ions of opposite charge leave the crystal and vacancies are left behind, the ratio of anionic and cationic charge stays the same)

A well-established notation for point defects is the Kröger-Vink notation [28]:

In M_S^C M is the species, e.g. atoms, vacancies, holes and electrons are possible, S is an index for the lattice site where the species can be found (the letter i is used to mark an interstitial) and C represents the electronic charge of the species in comparison to the site that it occupies. The symbols for charge are "x" for zero charge, "." for a single positive charge, ".." for double positive charge and so on and " '" for one negative charge.

For example: $Cu_i^{"}$ indicates a copper interstitial ion with a double positive charge.

It should be mentioned that there are some other notations for point defects available in literature [29].

Another type of imperfections in crystalline solids are dislocations. Dislocations are line imperfections which are introduced when a crystal is forming from a melt or when a solid body is deformed. The common known dislocations are: [24]

- Screw dislocations
- Edge dislocations
- Mixed dislocations with both edge and screw components

A consistent systematization of minerals has been made by Struntz [30]. Minerals are assigned to 10 classes which are subdivided on chemical-structural principles into divisions, subdivisions and groups of isotypic⁶ or homeotypic⁷ species, or individual minerals of a structure type. The alphanumeric coding scheme works as follows: The first numeric digit represents a class, the first alphabetic character represents a division and the second alphabetic character represents a subdivision. The final two numeric digits represent a group or individual mineral. The classes of the system are presented in table 4.

| Classes in the Strunz Mineralogical Tables | | |
|--|--|--|
| 1. Elements | | |
| 2. Sulfides and Sulfosalts | | |
| 3. Halides | | |
| 4. Oxides | | |
| 5. Carbonates + Nitrates | | |
| 6. Borates | | |
| 7. Sulfates | | |
| 8. Phosphates, Arsenates, Vanadates | | |
| 9. Silicates | | |
| 10. Organic Compounds | | |

Table 4: Simplified classification system for minerals according to Strunz [30]

⁶ Isotypy: Isotypic substances have the same crystallographic space group and analogous chemical formulae and crystal structures.

⁷ Homeotypy: Homeotypic substances have similar crystal structures, but with different crystallographic space groups and/or chemical compositions.

1.5 Solid State Spectroscopy

1.5.1 General Introduction

1.5.1.1 Quantum mechanical basics and overview on techniques

The wave-length range of the electromagnetic radiation used in this thesis was between 200 and 2500 nm. The introduction will also contain some basic information on the neighboring spectral ranges but will not go into details.

When talking about spectroscopy one should have in mind the spectrum of the electromagnetic radiation. It is depicted in figure 2. The energy of electromagnetic radiation depends on its wavelength or frequency according to Planck's equation:



$$E = hv = \frac{hc}{r} = hc\bar{v}$$
 Equ. 2

In equation 2 E is the energy in Joule, $h = 6,626 \cdot 10^{-34}$ Js is Planck's constant, ν is the frequency in s⁻¹ (Hz), c = 299,8 \cdot 10^6 m/s is the speed of light, λ the wavelengths in m and $\bar{\nu}$ the wavenumber in m⁻¹ [32].

Electronic or vibrational energy levels in matter cover a wide range of the energy scale. Which transitions are observed in an experiment is mostly dependent on the wavelength of the electromagnetic radiation used. The vibration frequencies of atoms in solids are about 10^{12} - 10^{13} Hz. Hence IR-radiation can be used to investigate the vibrational properties of a solid by recording its absorption or reflection by the sample. Information about the vibrating lattice is also obtained from Raman spectroscopy, where the scattering of the more energetic visible laser light (Raman scattering) is used [33].

Figure 2: the electromagnetic spectrum [31]

For solid state spectroscopy the rotations which are also excited via IR- and more efficiently via microwave radiation are not important, because in a solid body there are no rotational degrees of freedom left. For investigation of small molecules like CO_2 , H_2O , I_2 and others rotations are of great importance and have to be considered.

An overview from shorter to longer wavelength and corresponding radiation – matter interactions are given in table 5. The subdivision of the IR region into NIR, MIR and FIR was made according to the

recommendations in ISO 20473. The subdivision of the UV-region into UV-A, UV-B, UV-C-FUV, UV-C-VUV and EUV was made according to DIN 5031-7.

| Name of method or EM-radiation used | Wavelengths | Interaction between radiation and matter | Comment |
|---|--|--|--|
| NMR | in the scale of meters | transitions between nuclear spin states are induced | NMR transitions are excited at frequencies of about 10 ⁸ Hz |
| EPR | in the scale of millimeters to centimeters | transitions between electron spin states are induced | EPR transitions occur at frequencies of about 10 ¹⁰ Hz |
| IR | 780 nm - 1 mm | vibrational modes and rotational can be excited to higher energy states | |
| | FIR: 50 - 1000 μm | intramolecular and intermolecular vibrations [35] | for special applications |
| | MIR: 3 - 50 μm | mostly fundamentals and some overtones of vibrations and rotations [34] | standard laboratory technique |
| | NIR: 0,78 - 3 μm | overtones and combinations of fundamentals of vibrations and rotation [34] and excitations of valence electrons | today available in combined spectrometers for UV-VIS-NIR measurement |
| VIS | 780 - 380 nm | excitation of valence shell electrons excitations of electrons in unfilled d- or f- shells | |
| UV | 380 - 10 nm | excitation of valence and inner shell electrons | with a standard spectrometer the range of 380 - 200 nm is available |
| | UV-A: 380 - 315 nm | | |
| | UV-B: 315 - 280 nm | | |
| | UV-C-FUV: 280 - 200 nm | | |
| | UV-C-VUV: 200 - 100 nm | | Can only be handled under inert gas or vacuum. |
| | EUV: 100 - 10 nm | | Can only be handled under vacuum. |
| X-ray | 10 - 0,01 nm | ionization and inter-shell transitions | X-ray excitation is used to get absorption (XRT) and emission spectra (XRF) |
| γ-ray | ≤ 0,01 nm | transitions inside atomic nuclei | used in Mössbauer spectroscopy (information on oxidation state, CN, bond character and radioactive ions in solids |

 Table 5: Overview over common spectroscopic techniques and their wavelength range [33]

Since about 100 years it is known that for the discussion of molecular and atomic energy levels the concepts of classical mechanics are not suitable. In 1926 Erwin Schrödinger postulated his famous equation for the description of a particle with a mass of m and energy of E, that moves along x in some potential V [41]:

$$-\frac{\hbar^2}{2m}\frac{d^2\psi}{dx^2}+V(x)\psi=E\psi \qquad Equ. 3$$

In equation 3ψ is the wave function.

To make the transition from the world of classical mechanics to quantum mechanics quantities like the kinetic or potential energy have to be replaced by operators. These operators are applied to the wave functions of a system [39]. The operator which contains all possible contributions to the energy of a system is called "Hamiltonian Operator" \hat{H} . For the simple system of a particle moving in x-direction the Hamiltonian has two contributions:

$$\widehat{H} = \widehat{T} + \widehat{V}$$
 Equ. 4

In equation 4 \hat{T} is the operator for the kinetic energy and \hat{V} is the operator for the potential energy.

The kinetic energy is a function of x, the distance:

$$\widehat{T} = -\frac{\hbar}{2m} \nabla^2 \quad Equ. 5$$

where m is the mass of the particle and ∇^2 is the gradient operator with

$$\nabla^2 = \frac{d^2}{dx^2} + \frac{d^2}{dy^2} + \frac{d^2}{dz^2}$$
 Equ. 6

and \hbar is defined as [40]:

$$\hbar = \frac{h}{2\pi} = 1,05457 \cdot 10^{-34} Js \qquad Equ. 7$$

So Schrödinger's equation can be written for the simple cases as [41]:

$$\hat{H}\psi = E\psi$$
 Equ. 8

Even in these simple cases not a single energy is obtained from the solution of this equation, but a series of solutions differing in energy. These different energies correspond to the possible states of the system and are discriminated by a set of numbers – the quantum numbers.

Spectroscopic experiments show the transitions between these different energy states. In vibrational spectroscopy (IR, Raman) transition between different vibrational energy levels are observed.

1.5.1.2 Vibrational Spectroscopy and Symmetry Considerations

The energy levels of a simplified system consisting of two atoms can be depicted as in figure 3.



Figure 3: Energy levels of a diatomic molecule [37, 74]

Figure 3 shows the three most important transitions of a molecule: rotational transitions, vibrational transitions and electronic transitions.

The zero point energy of a system is the energy of its lowest permitted state. This zero point energy represents the difference between the minimum of the molecular potential curve and the vibrational state with quantum number v = 0. The zero point energy is based on the boundary conditions the wave functions of a system have to satisfy [38].

Several types of vibrations can be classified [36]:

- Symmetric vibrations or totally symmetric vibrations: symmetry properties of the molecule is preserved
- Nonsymmetric vibrations: symmetry properties like a C₂-axis or a σ-plane get lost during vibration

How can spectroscopic features be predicted? What is necessary to understand whether or not a molecule is active in the IR or Raman experiment? The key to these questions are the changes in symmetry when molecules undergo vibrations and deformations and the selection rules that are caused.

Vibrational excitation is modulated by diverse selection rules. These rules make it possible to predict whether a specific excitation will show up in the spectra. These predictions are based on quantum mechanical integrals related to the intensity of transitions. If these integrals are zero, the corresponding transitions are not observed and are called "forbidden". Again symmetry plays an important role.

The most important selection rule for each normal vibration is as follows: A vibration is active in the IR spectrum if the dipole moment of the molecule is changed during the vibration. This is the reason why homonuclear diatomic molecules (e.g. O2, N2, etc.) do not have IR spectra. In contrast, the Raman process is based on inelastic scattering which has nothing to do with dipole moments but requires an anisotropic polarizability. The polarizability of the electron cloud of a molecule is a measure for its ability to deform upon the action of external electric fields (like the strong electric field that go along with a laser beam). A vibration, is active in the Raman spectrum if the polarizability of the molecule is changed during the vibration. The polarizability of a molecule can be visualized as an ellipsoid containing the electron cloud of the molecule and therefore a vibration is Raman active if the ellipsoid changes in size, shape or orientation during the vibration. In a polyatomic molecule with a center of symmetry, the vibrations symmetric with respect to the center of symmetry are Raman active and are called "g" vibrations and are not IR active. "g" stands for the German word "gerade" (even). The vibrations antisymmetric to the center of symmetry are IR active and are called "u" vibrations, furthermore they are not Raman active. "u" stands for the German word "ungerade" (odd). This is called the "mutual exclusion rule" and it should be mentioned that there are several exceptions to this rule, especially when there are several symmetry elements in addition to the center of symmetry [36].

Group theory can be used to apply symmetry considerations to spectroscopically active centers. The symmetry properties of the active center (e.g. a transition metal or rare-earth ion in a solid) are also the symmetry properties of the Hamiltonian. These symmetry considerations can be used to solve problems such as [42]:

- Determining the number of energy levels of a particular active center
- Labelling these electronic energy levels with irreducible representations and determining their degeneracy
- Predicting the energy level splitting caused by the symmetry of the electric field surrounding the active center
- Establishing selection rules for optical transitions and determining their polarization character
- Determining the symmetry properties of the active centers eigenfunctions
- Analyzing the vibrations of a complex center

As mentioned in the previous chapter 32 point symmetry groups are known, which are listed in table 6. The order of the point group gives the number of possible symmetry operations and the number of classes⁸ indicates the number of sets of conjugate elements in the group [42, 43].

Again the symmetry point groups can be denoted either in the Schoenflies or the Hermann-Mauguin system. In Hermann-Mauguin notation n denotes an n-fold axis of rotation and m a mirror plane. A forward dash "/" means that the mirror plane is perpendicular to the axis of rotation. A bar over a number shows that this element is combined with an inversion. It is also important to distinguish symmetry

⁸ The term "class" comes from the definitions of group algebra. A good discussion of this topic is given in [43], but would go too far in the present work.

elements of the same sort but of a different class. E.g. 4/mmm denotes a symmetry group with 3 different classes of mirror elements σ_{v} , σ_{h} and σ_{d} [45].

| Schoenflies | Hermann-Mauguin | Group | Number of | Crystal System |
|-----------------------|-------------------|-------|-----------|----------------|
| Symbol | Symbol | order | classes | |
| C ₁ | l | 1 | 1 | Triclinic |
| Ci | 1 | 2 | 2 | Triclinic |
| Cs | m | 2 | 2 | Monoclinic |
| C ₂ | 2 | 2 | 2 | Monoclinic |
| C _{2h} | 2/m | 4 | 4 | Monoclinic |
| C_{2v} | 2mm | 4 | 4 | Orthorhombic |
| D ₂ | 222 | 4 | 4 | Orthorhombic |
| D _{2h} | mmm | 8 | 8 | Orthorhombic |
| C ₄ | 4 | 4 | 4 | Tetragonal |
| S_4 | 4 | 4 | 4 | Tetragonal |
| C _{4h} | 4/m | 8 | 5 | Tetragonal |
| C_{4v} | 4mm | 8 | 5 | Tetragonal |
| D _{2d} | $\overline{4}2m$ | 8 | 5 | Tetragonal |
| \mathbf{D}_4 | 422 | 8 | 5 | Tetragonal |
| D _{4h} | 4/mmm | 16 | 10 | Tetragonal |
| C ₃ | 3 | 3 | 3 | Trigonal |
| S_6 | 3 | 6 | 6 | Trigonal |
| C_{3v} | 3m | 6 | 3 | Trigonal |
| D_3 | 32 | 6 | 3 | Trigonal |
| \mathbf{D}_{3d} | $\overline{3}m$ | 12 | 6 | Trigonal |
| C _{3h} | 6 | 6 | 6 | Hexagonal |
| C ₆ | 6 | 6 | 6 | Hexagonal |
| C _{6h} | 6/m | 12 | 12 | Hexagonal |
| D _{3h} | $\overline{6} 2m$ | 12 | 6 | Trigonal |
| C _{6v} | 6mm | 12 | 6 | Hexagonal |
| D ₆ | 622 | 12 | 6 | Hexagonal |
| D _{6h} | 6/mmm | 24 | 12 | Hexagonal |
| Т | 23 | 12 | 4 | Cubic |
| T _h | m3 | 24 | 8 | Cubic |
| T _d | $\overline{4}2m$ | 24 | 5 | Cubic |
| 0 | 432 | 24 | 5 | Cubic |
| O _h | m3m | 48 | 10 | Cubic |

 Table 6: The 32 Point symmetry groups in crystals [44,45]

If the point group a molecule or a unit cell is not known, it can be found by successively working off the flow chart for point group determination [46].



Figure 4: Flow chart to find the proper point group for a molecular structure [46,47]

Mathematically every symmetry operation that can be performed on a spectroscopically active center can be considered as an operator. Performing the operation, in the mathematical picture, means to let this operator act on some basis. In the simplest case the basis could be a row vector holding the labels of all atoms of a molecule. By the action of the operator the basis is transformed, but can always be expressed by the original basis multiplied by a matrix. This matrix is quadratic and serves as a representation of the operator in the chosen basis. Other useful bases sets are the Cartesian coordinates or the p- and d- atomic orbitals. For example all 48 symmetry operations of the O_h group can be represented by sets of 48 matrices, whose dimensions depend on the chosen basis. Most of these sets of matrices are called "reducible representations" of the group Oh. The traces (i.e. sum over diagonal elements) of these matrices are known as "characters" in group theory. The character of a representation is independent of the chosen basis and contains a lot of useful information. The reducible representations can be broken down to smaller irreducible representations via a reduction algorithm. It turns out that the number of irreducible representations of a group equals the number of classes. The characters of the irreducible representations are contained in so-called character tables and are also used to perform the reductions of larger representations. The full information for a given group is contained in its character table. A character table is a quadratic array, its rows correspond to the irreducible representations (e.g. 10 for the O_h group), its columns to its classes and it contains the characters, and the set of basis functions [48].

Three main facts on character tables are important [48]:

- The number of classes is equal to the number of irreducible representations
- The set of characters of a representation is unique
- The dimension (that is the dimension of the matrices) of each irreducible representations is given by the character corresponding to the class E⁹.

| Group Symbol | Symmetry Classes | |
|--------------------|------------------|-----------|
| Irreducible | Characters | Basis |
| Representations in | | functions |
| Mulliken Notation | | |

Table 7: General appearance of a character table

In the Mulliken notation representations A and B are one-dimensional, E representations are twodimensional and T representation are three-dimensional. Higher irreducible representations are G, fourdimensional and H, five-dimensional [48]. The A's and the B's are distinguished by the fact, that A's have numbers of +1 for the rotation of about the axis of highest symmetry whilst B's have numbers of -1 [50].

As an example for a character table, the O_h character table is given in table 8.

 $^{^{9}}$ The dimension of the representation matrices, can always be seen from the character of the (n,n) matrix representing the identity operation E.

| O _h (m3m) | E | 8C3 | 6C ₂ | 6C4 | $3C_2$ (= C_4^2) | i | 6 S ₄ | 8 S ₆ | $3\sigma_h$ | 6σ _d | h = 48 | Basis sets |
|-------------------------|---|-----|-----------------|-----|------------------------|----|------------------|------------------|-------------|-----------------|-------------------|---------------------------------|
| A _{1g} | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | | $x^2 + y^2 + z^2$ |
| A _{2g} | 1 | 1 | -1 | -1 | 1 | 1 | -1 | 1 | 1 | -1 | | |
| Eg | 2 | -1 | 0 | 0 | 2 | 2 | 0 | -1 | 2 | 0 | | $(2z^2 - x^2 - y^2, x^2 - y^2)$ |
| T _{1g} | 3 | 0 | -1 | 1 | -1 | 3 | 1 | 0 | -1 | -1 | (R_x, R_y, R_z) | |
| T _{2g} | 3 | 0 | 1 | -1 | -1 | 3 | -1 | 0 | -1 | 1 | | (xz, yz, xy) |
| A _{1u} | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | | |
| A _{2u} | 1 | 1 | -1 | -1 | 1 | -1 | 1 | -1 | -1 | 1 | | |
| Eu | 2 | -1 | 0 | 0 | 2 | -2 | 0 | 1 | -2 | 0 | | |
| T _{1u} | 3 | 0 | -1 | 1 | -1 | -3 | -1 | 0 | 1 | 1 | (x, y, z) | |
| T _{2u} | 3 | 0 | 1 | -1 | -1 | -3 | 1 | 0 | 1 | -1 | | |

 Table 8: O_h character table (for an octahedral system) [51]
 [51]

1.5.1.3 Crystal field spectroscopy

The dimension of a representation corresponds to the degeneracy of its associated energy level [48].

For example the degeneracy of the set of the five d-orbitals in a free ion is 5 and all five d-orbitals have the same energy. When the free ion is placed into an octahedral crystal field – it could for example occupy a lattice site in a solid which is octahedrally surrounded by six ligands - the degenerate electron energy levels split. This is immediately seen by looking at the O_h character table: It does not have any five-fold degenerate irreducible representations. The set of 5 d-orbitals is split into two sets: e_g (two-dimensional = doubly degenerate) and three t_{2g} (three-dimensional = threefold degenerate) [49]. This example is illustrated in figure 5. In figure 5 the t_{2g} -orbitals are d_{xy} , d_{yz} and d_{zx} , the e_g orbitals are d_{z^2} and $d_{x^2-y^2}$.



Figure 5: d-orbitals in an octahedral crystal field [49]



Figure 6: Energy level splitting of the five degenerate states of a d-electron in an octahedral crystal field [49]

The energetic situation for the single electron d-orbitals in an octahedral electric field is easy to understand and can even be predicted by just looking at their shapes (the e_g orbitals have lobes pointing directly towards negatively charged ligands, and will therefore be energetically less favorable than the t_{2g} orbitals with their lobes pointing in between the ligands). The energetic situation for atoms having more than one electron in the d-shell is more complicated, but can nonetheless be calculated and predicted along the same symmetry and group theoretical lines outlined for the one-electron case. The results are usually presented in terms of so-called Tanabe-Sugano (TS) - diagrams. On the left-hand side of such diagrams the energies of the free ion Russsell-Saunders terms are given. The TS - diagram shows how the energies of the terms of an ion change as the strength of a crystal field increases. The ordinate is energy and the abscissa shows the strength of the crystal field. A special feature of TS-diagrams is, that the state of lowest energy (= the ground state) is always taken as the zero point of energy. The energies of the free ion energy levels are usually given in terms of the Racah parameters B and C. These parameters represent radial integrals which arise form electron-electron repulsion in the unfilled d-shell and are difficult to evaluate. Normally they are obtained from experimental gas phase atomic spectra of the respective d-element. It turns out that the values of B and C are in a constant ratio for a given d-element. It is convenient to normalize the axes of the TS-diagram to the Racah parameter B. Δ is the ligand field strength. Terms of the same symmetry follow the "non-crossing rule", which means that they mustn't cross each other and bend away, when Δ is increased. TS – diagrams for different symmetries of the crystal field and different ions are available in the literature [52]. An example of a TS-diagram is given in figure 9.

The ground state of an ion may change, as the crystal field is increased. In this case the diagram shows a sudden increase of other energy levels at the point of the change.

The crystal field energy states in the TS-diagrams are labeled with the irreducible representations of the corresponding symmetry group. Figure 9 shows for example that the ⁵D Russell-Saunders ground state of the free Fe³⁺ iron with the d⁶ configuration is split into a ⁵T_{2g} (lower energy = crystal field ground state) and a ⁵E_g crystal field level (this is in perfect analogy with the splitting of the 5 d-orbitals into t_{2g} and e_g states). At higher crystal field strengths the ¹A_{1g} crystal field level which arises from the splitting of the ¹I

term becomes even lower in energy and is the new ground state from there onward. The notation of the free ion states is briefly reviewed [53, 54, 55]:

The electron configurations of several transition metal ions from the first period are given in table 9. Only the unfilled d-shell is indicated, in addition all ions have a closed argon core [Ar]:

| | Ti ³⁺ | Ti ²⁺ | Cr ³⁺ | Cr^{2+} | Fe ³⁺ | Fe ²⁺ | | | | |
|------------------|------------------|------------------|------------------|------------------|------------------|------------------|-------------------------|------------------|------------------|------------------|
| Sc ³⁺ | V^{4+} | V ³⁺ | Mn ⁴⁺ | Mn ³⁺ | Mn ²⁺ | Co ³⁺ | Co ²⁺ | Ni ²⁺ | Cu ²⁺ | Zn ²⁺ |
| 3d ⁰ | 3d ¹ | $3d^2$ | $3d^3$ | $3d^4$ | d ⁵ | 3d ⁶ | 3 d ⁷ | 3d ⁸ | 3d ⁹ | 3d ¹⁰ |

 Table 9: Electron configurations for selected transition metal ions [55]

As usual the letter code for the orbital angular momenta l (for one-electron systems) and L (for multielectron systems) is:

| 1 = L = | 0 | 1 | 2 | 3 | 4 | 5 |
|---------|---|---|---|---|---|---|
| letter | S | р | d | f | g | h |
| | S | Р | D | F | G | Η |

According to the vector model for atoms, an orbital angular momentum of value 1 has several possibilities for its spatial arrangement, indicated by its z-component m₁:

$$m_l = l, l - 1, l - 2, ..., -l$$
 Equ. 9

Therefore (2l+1) values for m_l are possible. For a d-electron, with l = 2 the values of m_l are $m_l = 2, 1, 0$, -1, -2. Thus there are five d-orbitals.

In multi-electron transition metal free ions the electrons can occupy any of the degenerate d-orbitals. If as the only physical constraint the Pauli principle is taken (only two electrons per orbital and spin-pairing) then there are for example 45 possible arrangements of the two d-electrons of V^{3+} . These 45 arrangements however are no longer degenerate because of electron-electron repulsion. Some arrangements (with less possibility of repulsion) will be lower in energy than others. Hence the degeneracy of the 45 arrangements is lifted and discrete free ion energy levels occur, which are called the Russell-Saunders terms represented by a term symbol:

$$2S+1L_{1}$$

In a term symbol the letter L is S, P, D, F, etc. and corresponds to the **orbital angular momentum quantum number** L (0, 1, 2, 3, etc.). The multiplicity of the term is 2S + 1, where S is the total spin **quantum number** and J is the total angular momentum quantum number which is a consequence of spin-orbit coupling which is not considered as an important effect for the first period transition elements. Therefore their Russell-Saunders terms were denoted by just ${}^{2S+1}L$. Each of these terms has a degeneracy of $(2L+1) \cdot (2S+1)$ which can be lifted by external electric fields (like the crystal field in a solid).

For example the 45 degenerate d^2 configuration is split into (degeneracy is indicated underneath):

$$d^2 \rightarrow {}^3F, {}^3P; {}^1G, {}^1D, {}^1S$$

(45) (21) (9) (9) (5) (1)

Spin-orbit coupling is a major effect in ions with unfilled f-shells (lanthanides, rare-earth elements) and must be taken into account there. So the free ion RS terms of Rare earth ions ^{2S+1}L consist of 2J+1 states, which are usually degenerate in the absence of an external electric magnetic field and are split in their presence [53].

The J-values can be calculated from the L and S values [54]:

$$J = L + S, L + S - 1, ..., |L - S|$$
 Equ. 10

What was said about term symbols can be summarized [53]:

$${}^{multiplicity \rightarrow 2S+1}L_{I \leftarrow level} \leftarrow orbital angular momentum$$



Figure 7: Notation and origin of the splittings of energy levels in atoms and ions [53]

The correct term symbol of an electronic ground state can be found via the formalism of the orbital graph [55]. An orbital graph is a pictorial scheme of the d-shell, where the orbitals are represented by boxes. There are five rows with two boxes each, the rows are labeled with m_l and the columns with m_s . These boxes may be filled with electrons. By summing the individual m_l and m_s values of the electrons M_l and M_s values are obtained:

$$M_L = \sum m_l \qquad Equ. 11$$
$$M_S = \sum m_s \qquad Equ. 12$$

From: $M_L = L$, L-1, L-2, ..., -L; and $M_S = S$, S-1, S-2, ..., -S it is clear that $M_{L,max} = L$ and $M_{S,max} = S$.

By filling the boxes in such a way that the maximal value for M_L and at the same time the maximal value for M_S is results, one makes sure that the electronic ground state according to Hund's rules is obtained. This is always the case when the orbital graph is filled with electrons starting from top left.

This procedure is in accordance with Hund's rules [54]:

- 1. The term with maximum multiplicity lies lowest in energy.
- 2. For a given multiplicity, the term with the highest value of L lies lowest in energy.
- 3. For atoms with less than half-filled shells, the level with the lowest value of J lies lowest in energy.

For transition metal ions Hund's first and second rule have to be considered only. For rare earth ions, Hund's third rule has to be taken into consideration because of the spin-orbit coupling, which plays an important role for rare earths [55].

As an example Fe^{2+} and Fe^{3+} ground states will be determined. A neutral iron atom has the electron configuration $1s^22s^22p^63s^23p^63d^64s^2$ or simpler [Ar] $3d^64s^2$. When the neutral Fe loses 2 electrons and becomes Fe^{2+} the electronic configuration is [Ar] $3d^6$. This leads to a Russell-Saunders term symbol for the ground state of ⁵D. When the Fe²⁺ ion loses another electron [Ar] $3d^5$ to become Fe³⁺ the corresponding Russell-Saunders term symbol is ⁶S (see figure 9).



Figure 8: Orbital graphs for the d^5 and d^6 configuration of Fe^{3+} and Fe^{2+} , respectively

The higher energy states of an ion can be found by application of the Gray-Wills [57] or the Shudeman [56] method. Figure 9 shows the TS-diagram for these ions in O_h symmetry.


Figure 9: Tanabe Sugano diagrams for two d-electron systems in octahedral symmetry (for convenience the "g" index is not written – all states arising from d-systems are g)

1.5.1.4 Anharmonic Oscillator and IR-spectra

The short wave to long wave side of transmission or reflection spectra from 200 to approximately 900 nm can be understood with the concepts presented in the previous chapters. For the NIR to MIR region of the spectra the oscillator model gives a good explanation.

A molecule can be considered as a system of several masses, tied together by springs. Every possible oscillation of such a system can be visualized as an idealized harmonic oscillator or, more realistically, as an anharmonic oscillator. The anharmonic oscillator model includes the zero point energy, the energy of the state with quantum number v = 0 (which is not zero) and the dissociation limit of a molecule. The transition from v = 0 to v = 1 is called the fundamental. The transition v = 0 to v = 2 is called the first overtone and so forth. The energy of a vibration E_{VIB} can be calculated as follows: [58]

$$E_{VIB} = h v_{osc} \left(v + \frac{1}{2} \right) = \frac{h}{2\pi} \sqrt{\frac{k}{\mu}} \left(v + \frac{1}{2} \right) \qquad Equ. 13$$

In equation 13 h is Planck's constant, v_{osc} the oscillation frequency, v the quantum number of the oscillation, k the force constant and μ the reduced mass.



Figure 10: Potential curve for a harmonic (green) and an anharmonic (blue) oscillator [59]

For anharmonic systems the potential curve is well represented by the "Morse"-potential.

Overtones can be approximated within the harmonic oscillator model with the following equations [62]:

$$n = 0: E_0 = \frac{1}{2}hv_{osc}$$
$$n = 1: E_1 = \frac{3}{2}hv_{osc}$$
$$n = 2: E_2 = \frac{5}{2}hv_{osc}$$
$$n = 3: E_3 = \frac{7}{2}hv_{osc}$$

etc.

Combination vibrations of the system can be calculated as follows [60, 61]:

$$v_{comb} = a \cdot v_1 \pm b \cdot v_2 \pm c \cdot v_3 \pm \dots \quad Equ. 14$$

In equation 14 v_{comb} is the wavenumber of the combination vibration, v_n is the n-th fundamental (with n = 1,2,3,...) and a, b and c non-negative integral numbers.

However, the number of observable combinations and overtones of molecules is reduced by symmetry constraints. Furthermore the observed wavenumbers for combinations and overtones are lower than the calculated ones from the harmonic oscillator model due to the anharmonicity of the system [60, 61].

1.5.2 Reflection Spectroscopy with the L950 on Minerals

Since the theory of absorption of light was discussed in detail in previous parts of the work, this chapter will deal with some practical aspects of reflection measurements of solids.

The state of the art spectrometer type in laboratories is the double beam spectrometer. A schematic drawing of the optical system of the dispersive Lambda 950 transmission/reflection spectrometer is given in figure 11.



Figure 11: The optical system of the L950 spectrometer [63]

In figure 11 DL is the deuterium lamp, HL the halogen lamp, Mx the mirror number x, SA the slit assembly, G the grating, C the chopper assembly, CBM the common beam mask, FW the filter wheel assembly, C the chopper, Dp the depolarizer, R the reference and S the sample [64]. Figure 12 shows the L950 spectrometer, which was used to record all reflection and transmission spectra in this work.



Figure 12: a) the L950 spectrometer, b) the integrating sphere detector module, c) a Bauxite sample at the diffuse reflection port of the integrating sphere, d) the PMT-detector for UV-VIS-detection (left) and the InGaAs-detector for NIR-detection (right)

The most important law for all day laboratory work is the Beer-Lambert law:

$$I = I_0 \cdot exp(-\varepsilon cd) \qquad Equ. 15$$

or in the more common form:

$$log\left(\frac{I_0}{I}\right) = A = \varepsilon cd$$
 Equ. 16

In equations 15 and 16 I_0 is the intensity of the reference beam, I the intensity of the beam which passed the sample, A the Absorbance, ε the molar absorption coefficient, d the length of the cuvette and A the absorbance [65].

When light hits matter four phenomena can be encountered: reflection (R), scattering (S), transmission (T) and absorption (A).



Figure 13: Interaction of light with a sample [66]

In figure 13 I_R is the intensity of the reflected light, I_0 the intensity of the incident light, I_s the intensity of the scattered light, I_A the intensity of absorbed light and I_T the intensity of transmitted light.

The measurements in this work fall in the category of diffuse reflection measurement. The surface of the sample, which could be a powder, a rough surface of a mineral or a microcrystalline sample is optically scattering. The incident light may be partly reflected regularly (i.e, the angle of incidence is the same as the emergent angle), partly scattered diffusively and partly enter the substrate. The part that enters the substrate can undergo absorption within particles, undergo diffraction at grain boundaries, re-emerge at the sample surface and mix with reflected parts. Measured reflection values are therefore a sum of all these contributions. Reflectivity values can be transformed to absorbance values via mathematical models. One of these models is the Kubelka-Munk theory, which can be found in the literature [127]. For practical use the reflectivity will be defined as follows:

$$R_{\lambda} [\%] = \frac{I_{R,\lambda}}{I_0} \qquad Equ. 17$$

In equation 17 R_{λ} is the reflectivity at a certain wavelength λ , $I_{R,\lambda}$ is the intensity of reflected light at a certain wavelength and I_0 is the intensity of the incident beam.

The L950 spectrometer uses an integrating sphere with two possible measurement ports: a) the diffuse transmission port and b) the diffuse reflection port, where the sample is twisted 8° to the incident beam. The diffuse transmission port can be used for transmission measurements of opaque samples, since the scattered part of the transmitted light is gathered by the integrating sphere and reflected to the detector system. The slight twist of the sample at the diffuse reflection port is necessary to ensure that no reflected light goes back to the light source and is therefore lost for detection. It is also possible to exclude all the regular reflection from detection, by opening the integrating sphere at one side opposite to the sample.

The integrating sphere of the L950 system is coated with so called "Spectralon" which is pure Teflon (Poly(1,1,2,2-tetrafluorethylene). Teflon has a rather high reflectivity in the interesting region form 200 nm to 2500 nm. But it should be noted, that even this highly reflecting material is not a 100% reflector over all wavelengths. A reflection spectrum of spectralon is depicted in figure 14.



Figure 14: Spectralon reflection spectrum [128]

Since no two integrating spheres do have the same optical properties, even if they have the same coating material, correction of the reflection spectrum is necessary if reflection spectra are to be compared in detail as proposed by Clark et al. [128].

After cutting and polishing the mineral samples can be easily positioned at the reflection port of the integrating sphere and fixed by tape, the positioning mechanism at the outside of the sphere or plasticine. For samples smaller than the reflection port diameter of about 2,5 cm, a Teflon aperture was constructed, which has a hole diameter of 8 mm. If the Teflon aperture is used, it has to be positioned properly using the align-mode of the spectrometer.

The positioning of the samples is shown in figure 15.



Figure 15: Sample positioning at the L950 integrating sphere reflection port a) with the original holder, b) with tape using a Teflon aperture with 8 mm hole diameter

It should be avoided that samples fall into the integrating sphere, since the PMT-detector and the InGaAsdetector are positioned at the bottom side of the detector module. If the reflection coating is contaminated with dust from the laboratory, it can be cleaned with a N₂-gas stream.

The integrating sphere of the L950 system has a diameter of about 150 mm. Therefore the light (especially in the NIR region) reflected from the sample is attenuated and has to be intensified via the so called "InGaAs gain". It turned out, that a value of 16 yields good results. Figure 16 shows the schematic diagram of the control software UV-Winlab.



Figure 16: Schematic diagram of the control window of UV-Winlab

A comparison of two spectra of the same Holmium oxide reflection standard is given in figure 17.



Figure 17: Ho-oxide reflection spectrum with and without proper warm up time and gain settings

It is seen, that the proper gain setting greatly increases the signal to noise ratio and also that for a good wavelength accuracy the instrument has to be switched on for about 30 minutes to warm up the system.

1.5.3 Raman Spectroscopy of Minerals

Raman spectroscopy is based on the inelastic scattering of light by matter. It can be used to classify minerals and inclusions in minerals via comparison of the sharp stokes peaks in Raman-spectra of minerals with database entries. A good overview over the basics of the technology and applications for minerals with some data on Raman bands is given by Frezotti et al. [129]. The authors give also some examples for the identification of mineral phases with Raman-spectroscopy. An energy level scheme, example spectrum and basic setup of a Raman spectrometer are depicted in figure 18.



Figure 18: a) Example Raman spectrum, b) Energy level scheme for elastic Rayleigh scattering and inelastic Anti-Stokes and Stokes Raman scattering, c) basic setup of a Raman spectrometer [129]

Raman scattering can be explained as an interaction of light with matter in a quantum mechanical model: A molecule has different vibrational energy levels, the ground state v = 0 and ant the excited states v = 1, v = 2, v = 3, etc. are separated by a quantum energy $\Delta E = hv_m$. h is Planck's constant and v_m the the frequency of the molecular vibration. The incident light induces transitions to virtual energy levels of the molecule. This virtual energy levels are generated when light interacts with the molecule and the energy is risen. Because virtual energy levels are unstable the energy is released as scattered light immediately. Light of the frequencies v_1 (excitation frequency), $v_1 - v_m$ (Stokes) and $v_1 - v_m$ (Anti-Stokes) is emitted, where v_m is the fundamental rotational, vibrational or lattice frequency of the molecule. The Raman effect is a very weak optical phenomenon and since anti-Stokes lines are much weaker than Stokes lines, only Stokes lines are plotted in a Raman spectrum. The Rayleigh peak has the same frequency as the excitation source (usually a VIS laser) and is defined as the zero point in a Raman spectrum. The Stokes lines in Raman spectra represent vibrational energies (stretching and bending) of the analyzed molecules. When a vibration is observed in the Raman spectrum it changed the polarizability of the molecules [129]. The project partner Montanuniversität Leoben has a lab scale Raman spectrometer for identification of mineral phases in use.



Figure 19: Raman spectrometer at the MUL: a) Raman workplace, b) sample positioned in the apparatus, c) Raman spectrometer at work with the green laser light source.

For lack of space no Raman spectra are presented in the present work. However, it should be mentioned, that Raman spectrometers focus only on a small spot of the sample. Therefore the method is prone to errors originating from sample inhomogeneities.

1.5.4 Fluorescence Spectroscopy and Sorting of Minerals

1.5.4.1 From Molecular Fluorescence to Solid State Fluorescence

Molecular fluorescence is often explained with the configuration coordinate- or, alternatively, the Jablonski diagram, which are depicted in figure 20. A molecule can be excited from its electronic ground state to an excited or "activated state". This activated state can relax without emission of radiation for example by molecule-molecule or molecule-wall collisions in a liquid system or via phonons in a solid system. The energy is conversed into rotational, vibrational and translational energy. This process is also known as "thermal dissipation".

Fluorescence is considered as a rather fast phenomenon (nanoseconds), while phosphorescence is an emission that can last longer (microseconds to several hours). Usually the emitted light has a longer wavelength, corresponding to a lower energy, as the excitation light. This is known as the Stokes-shift of the system. Fluorescence can be summarized as follows:

- 1. Absorption of light
- 2. Excitation of the system from its ground state (singlet, S_0) to a higher electronic state (singlet, S_1)
- 3. Radiative and non raditative deactivation of the system

In Phosphorescence there is another step called intersystem crossing. Intersystem crossing is a spin forbidden transition, but enabled by spin-orbit coupling. Spin orbit coupling is usually high, when a molecule contains heavy elements like sulfur.

It is a transition from an excited singlet state to a triplet state. The triplet state serves as a slow radiative reservoir, because to return to the ground state is also spin forbidden. Therefore phosphorescence can be summarized as follows [131]:

- 1. Absorption of light
- 2. Excitation of the system from its ground state (singlet, S_0) to a higher electronic state (singlet, S_1)
- 3. Intersystem crossing: transition from S_1 to T_1
- 4. Radiative deactivation of the system



Internuclear distance

Figure 20: a) Mechanism of phosphorescence and fluorescence. The crucial feature for phosphorescence is the intersystem crossing (ISC) as a change from singlet to triplet state, which is possible because of the spin orbit coupling. b) Jablonski diagram [130]

For solids a very similar model can be applied. For example if a Cr^{3+} -ion is considered in an octahedral crystal field, like it is the situation in ruby $(Al_2O_3:Cr^{3+})$. Several vibrational modes can be found. An octahedron can be considered as a molecule with 7 atoms. The 3N-6 rule states, there must be 3.7-6 = 15 normal modes. The totally symmetric breathing mode can be described like a diatomic oscillator with one parameter Q which describes the in-phase vibration of the ligands towards the central Cr^{3+} .



Figure 21: a) Breathing mode of an octahedron [133], b) a diatomic osillator

A combination of the Tanabe-Sugano diagram and configuration coordinate diagrams can serve to predict emission spectra of solids. A combined diagram for the Cr^{3+} system in octahedral crystal field is presented

in figure 22. This diagram is the key to understand the emission spectrum of ruby, which was the first laser material.



Figure 22: Combined diagram for the system Cr³⁺ in octahedral crystal field [132]

The numbered steps in figure 22 can be described as follows:

- 1. ${}^{4}A_{2g} \rightarrow {}^{4}T_{1g}$: Excitation of electrons into the blue absorption band of the system populates excited vibrational levels of the ${}^{4}T_{1g}$ state.
- 2. Radiationless relaxation to the vibrational ground state of ${}^{4}T_{1g}$
- 3. ${}^{4}T_{1g} \rightarrow {}^{2}T_{1g}$: non radiative transition to ${}^{2}T_{1g}$ (this corresponds to ISC in the molecular model) ${}^{2}T_{1g} \rightarrow {}^{2}E_{g}$: vibronic transition
- 4. ${}^{2}E_{g} \rightarrow {}^{4}A_{2g}$: emission of photons (694 nm)
- 5. Possible non radiative transition in concurrence to 4

Thus the absorption and emission transitions can be predicted and are plotted in figure 23.



Figure 23: Absorption and emission spectrum of ruby $(Cr^{3+} in Al_2O_3)$ [132]

In general relative fluorescence intensities are measured. Intensity data recorded with the same instrument, using the same set of instrumental parameters (slit width, gain, etc.) can be compared easily. Comparing fluorescence intensities obtained with different instrumental parameters is more difficult (see chapter 3.2.1). If datasets from different instruments are compared, differences can occur because of the different optical properties of the instruments. Measurement of absolute intensities is also possible, but requires particular instruments.

Therefore the determination of absolute fluorescence intensity requires a much bigger experimental effort [86]. There is a commercial device provided by Hamamatsu: The "Absolute PL Quantum Yield Measurement System" consists of an excitation source and an integrating sphere. Details on this method can be found on the Hamamatsu homepage [87].

1.5.4.2 Mineral Fluorescence

Fluorescence of minerals of natural origin could be a promising field for sorting applications in industry. The existing data on mineral fluorescence, combined with available sensor-technologies can be used for sorting of industrially relevant minerals and ores [75].

The book "Luminescence Spectroscopy of Minerals and Materials" by Gaft et al gives a good overview on minerals fluorescing upon UV-light excitation [76]. The introduction chapter contains a table with 62 common fluorescing minerals which is reproduced below (see table 11).

| Native | Diamond | | | | |
|-----------------|---|--|--|--|--|
| Oxides | Brucite Mg(OH) ₂ , Corundum Al ₂ O ₃ , Ruby Al ₂ O ₃ , Sapphire Al ₂ O ₃ | | | | |
| Halogenides | Fluorite CaF ₂ , Halite NaCl, Calomel HgCl | | | | |
| Silica | Agate SiO ₂ , Opal SiO ₂ , Quartz SiO ₂ | | | | |
| Phyllosilicates | Pyrophyllite AlSi ₂ O ₅ OH, Talc Mg ₃ Si ₄ O ₁₀ (OH) ₂ , Serpentine | | | | |
| | $(Mg,Fe)_3Si_2O_5(OH)_4$ | | | | |
| Feldspar | Albite NaAlSi ₃ O ₈ , Microline KAlSi ₃ O ₈ | | | | |
| Pyroxenes | Diopside CaMgSi ₂ O ₆ , Spodumene LialSi ₂ O ₆ | | | | |
| Amphiboles | Anthophyllite (Mg, Fe) ₇ Si ₈ O ₂₂ (OH) ₂ , Tremolite Ca ₂ Mg ₅ Si ₈ O ₂₂ (OH) ₂ | | | | |
| Zeolites | Natrolite Na ₂ Al ₂ Si ₃ O ₁₀ x 2H ₂ O, Laumontite CaAl ₂ Si ₄ O12 x 4H ₂ O, | | | | |
| | Analcite NaAlSi ₂ O ₆ x H ₂ O | | | | |
| Feldspathoids | Sodalite Na ₄ Al ₃ (SiO ₄) ₃ Cl | | | | |
| Other silicates | Zircon ZrSiO ₄ , Datolite CaBSiO ₄ (OH), Danburite CaB ₂ Si ₂ O ₈ , | | | | |
| | Eucryptite LiAlSiO ₄ , Willemite Zn ₂ SiO ₄ , Wollastonite CaSiO ₃ , | | | | |
| | Sphene CaTiSiO ₅ , Scapolite Na ₄ (Al, Si) ₁₂ O ₂₄ , Axinite Ca ₂ (Mn, Fe, | | | | |
| ~ 1 | Mg)Al ₂ (BO ₃ OH)(SiO ₃) ₄ , Benitoite BaTiSi ₃ O ₉ , Thorite (Th,U)SiO ₄ | | | | |
| Carbonates | Aragonite CaCO ₃ , Calcite CaCO ₃ , Cerussite PbCO ₃ , Magnesite | | | | |
| <u> </u> | MgCO ₃ , Strontianite SrCO ₃ , Witherite BaCO ₃ | | | | |
| Sulfides | Sphalerite (Zn,Fe)S, Wutzite (Zn,Fe)S | | | | |
| Sulfates | Barrite BaSO ₄ , Celestine SrSO ₄ , Gypsum CaSO ₄ x $2H_2O$, Anhydrite | | | | |
| | CaSO ₄ , Alunite KAl ₃ (SO ₄) ₂ (OH) ₆ , Zippeite K ₄ (UO ₂) ₆ (SO ₄) ₃ OH ₁₀ x 4 | | | | |
| | H ₂ O, Ettringite Ca ₆ Al ₂ (SO ₄) ₃ (OH) ₁₂ x 26 H ₂ O, Hanksite | | | | |
| Dheamhatag | $\frac{\text{Na}_{22}\text{K}(\text{SO}_4)_9(\text{CO}_3)_2\text{Cl}}{\text{Amotiva}}$ | | | | |
| Phosphates | Apatite $Ca_5(PO_4)_3(OH,F,Cl)$, Wavellite $Al_3(PO_4)_2(OH)_3 \times 5 H_2O$, Amblygonite (Li,Na)AlPO ₄ (F,OH), Pyromorphite Pb ₅ (PO ₄) ₃ Cl, | | | | |
| | Monazite (Ce,La,Th,Nd,Y)PO ₄ , Autunite Ca(UO ₂) ₂ (PO ₄) ₂ x 10 H ₂ O, | | | | |
| | Xenotime YPO ₄ Xenotime YPO ₄ | | | | |
| Tungstates | Scheelite CaWO ₄ | | | | |
| Molybdates | Powellite CaMoO ₄ , Wulfenite PbMoO ₄ | | | | |
| Borates | $\frac{1}{10000000000000000000000000000000000$ | | | | |
| Organics | $\frac{1}{10000000000000000000000000000000000$ | | | | |
| | | | | | |

Table 11: Minerals luminescent under UV lamp excitation

The book also provides a short but good overview of the theory of mineral fluorescence and a collection of time resolved luminescence spectra. As minerals are by definition natural crystalline solids they can contain more than one luminescence center. For example two luminescence centers in the same mineral can show emission in the same spectral range with different decay and life times of the excited state. So

Gaft et al refer to the terms "delay time" abbreviated D and "gate time" abbreviated G in their book to describe this behavior in the quoted spectra. The spectra contained in the book are sorted by luminescent minerals bearing cations of interest such as Ca²⁺, Pb²⁺, Sn⁴⁺, Ba²⁺, Sr²⁺, Ti⁴⁺, Zn²⁺, Zr⁴⁺, Si⁴⁺, Al³⁺, Na⁺, Ag⁺, Mn²⁺, U⁶⁺, Mg²⁺, rare earths and carbon.

A standard reference book with the title **"Luminescent spectra of minerals"** has been published by Gorobets and Rogojine in 2001. It summarizes the main achievements in that field up to the year 2000 [77]. It provides a systematization of luminescent minerals with a hierarchical order in three levels:

- <u>1st level</u>: Luminescent minerals are divided into dielectrics (insulators), semiconductors and metals together with intermetallic compounds. This means *classification by the energy bandgap* E_g . Metals are minerals with $E_g = 0$. Low-bandgap semiconductors have values of E_g such as $0 \le E_g \le 1$ eV. Metals and semiconductors are opaque to optical photons (so they are incapable of luminescence in principle). Insulators with $4 < E_g < 10$ eV and large-bandgap semiconductors with $1 < E_g < 4$ eV are to some extend transparent to UV and visible light. Under certain circumstances this materials can transform external energy (photons or electrons) into luminescence photons.
- <u>2nd level:</u> Luminescent minerals are *subdivided by the type of chemical compounds* like homoatomic compounds, sulfides, halides and oxygen bearing compounds. The knowledge of the chemical composition gives hints to the mechanisms of the luminescence phenomenon.
- <u>3rd level:</u> Luminescent Minerals are partitioned by their *mineral formulae*. The associations of the donor-acceptor centers for examples with vacancies or interstitials determine whether a luminescence center is formed or not.

One further step in the system of Gorobets and Rogojine is to predict which luminescent metal impurities (luminescent cations) are to be expected for a given mineral according to the host cation in the mineral [78]. A compact overview over 25 possible classes of fluorescing minerals was provided by Gorobets et al and is reproduced in table 12. Furthermore it is stated that a luminescing mineral should satisfy the following three conditions [79]:

- 1. A suitable type of crystal lattice favorable for emission centers is formed.
- 2. The content of photoluminescent centers is high enough (usually > 0.01%)
- 3. The amount of iron or other quenchers is small enough (around 0,5 1 %). Iron is a principal quenching element in nature.



 Table 12: Schematic partition of minerals into groups with various luminescent properties due to

 different types of chemical bonding and composition [79]

Examples for the 25 classes of luminescing minerals in table 12 are given with their chemical formulas and the corresponding crystal systems which were looked up in [80]:

- 1. \mathbf{Mn}^{2+} : *Rhodonite*: $\mathbf{Mn}_3[\mathbf{Si}_5\mathbf{O}_{15}]$, triclinic
- 2. V⁵⁺: *Vanadinite*: Pb₅[Cl|(VO₄)₃], hexagonal
- 3. Cr⁶⁺: *Crocoite*: Pb[CrO₄], monoclinic
- 4. Ti^{4+} : *Ramsayite*¹⁰: Na₂Ti₂[O₃|Si₂O₆], orthorhombic
- 5. Mo⁶⁺: *Powellite*: Ca[MoO₄], tetragonal
- 6. **W⁶⁺**: *Scheelite*: Ca[WO₄], tetragonal
- 7. U^{6+} : *Otunite*¹¹: Ca[UO₂|PO₄]·10H₂O, tetragonal
- 8. **Sn⁴⁺:** *Cassiterite*: SnO₂, tetragonal
- 9. Ag⁺: *Chlorargyrite*: AgCl, cubic
- 10. Na⁺: *Halite*: NaCl, cubic
- 11. **Mg²⁺:** *Forsterite*: Mg₂[SiO₄], orthorhombic
- 12. Al³⁺_{oct}: *Spinel*: MgAl₂O₄, cubic
- 13. Al³⁺tetr, Si⁴⁺: *Feldspars*: (Ba, Ca, Na, K, NH₄)(Al, B, Si)₄O₈, family of minerals in different crystal systems and of different chemical compositions
- 14. K⁺,Cs⁺: Microline: K[AlSi₃O₈], triclinic; Pollucite: (Cs_{0,7}H₂O_{0,3})Na_{0,3}[AlSi₂O₆], cubic
- 15. **Ca²⁺:** *Calcite*: Ca[CO₃], trigonal; *Apatite*: Ca₅[(F, Cl, OH)|(PO₄)₃], family of minerals in different crystal systems and of different chemical compositions; *Fluorite*: CaF₂, cubic
- 16. **Zn²⁺:** *Willemite*: Zn₂[SiO₄], trigonal
- 17. Sr²⁺, Ba²⁺: Strontianite: SrCO₃, orthorhombic; Baryte: Ba[SO₄], orthorhombic
- 18. **Zr⁴⁺:** *Zircon*: Zr[SiO₄], tetragonal
- 19. (Y, La)³⁺: *Gagarinite*: NaCaYF₆, hexagonal
- 20. **Zn²⁺-S²⁻:** *Sphalerite*: ZnS, cubic
- 21. C: Diamond: C, cubic; Moisannite: SiC, family of minerals in different crystal systems and of different chemical compositions
- 22. CI: *Sodalite*: Na₈[Cl₂|(AlSiO₄)₆, cubic; *Pyromorphite*: Pb₅[Cl|(PO₄)₃], hexagonal
- 23. CO₃²⁻: *Calcite*: Ca[CO₃], trigonal; *Dolomite*: CaMg[CO₃], trigonal; *Hydrozincite*: Zn₅[(OH)₆|(CO₃)₂], monoclinic
- 24. **SiO**₄⁴⁻: *Forsterite*: Mg₂[SiO₄], orthorhombic
- 25. Gels of SiO₂, Al₂O₃: *Chalcedony*¹²: SiO₂, different crystal structures are known (trigonal, hexagonal, orthorhombic, hexagonal, tetragonal, cubic); *Opal*: SiO₂·nH₂O, three crystal structures of opal are known (A: amorphous, CT: cristobalite & tridymite, T: tridymite); *Allophane*: Al₂O₃·SiO₂·H₂O to 2 Al₂O₃·SiO₂·H₂O, amorphous and semi-crystalline

Since luminescence in minerals is often caused by rare earth elements the Dieke diagram is a useful tool in interpretation of unknown spectra. The Dieke diagram describes all ${}^{2S+1}L_J$ multiplets for the REs (rare earth elements).

¹⁰ Also known under the name Lorenzenite.

¹¹ Also known as Autunite.

¹² Calcedony is often referred to as cryptocrystalline quartz. Cryptocrystalline means that the texture cannot be resolved in a conventional light microscope.

$$\begin{array}{c} 10^{5} \text{cm}^{-1} & \frac{1}{14} & \frac{1}{1$$

Figure 24: Dieke diagram for rare earth ions in crystals [134]

1.5.5 The LS 55 - a labscale spectrofluorimeter

The LS 55 is a spectrofluorimeter from Perkin Elmer. It uses a pulsed Xe-flashlamp as light source. A solid sample holder was mounted in the measurement chamber. The solid sample holder should provide a good signal free from stray light. Prior to a measurement the solid sample holder has to be adjusted via the positioning screws at the bottom of the holder to its optimal position. This is done by operating the device in read mode while exciting a known sample (e.g. a Fluorite sample) with a wavelength of a good quantum efficiency for the emission (e.g. for the Fluorite with 366 nm) and observation at a known emission wavelength (e.g. 424 nm for Fluorite) while changing the positioning of the holder.

The LS 55 is depicted in figure 25.



Figure 25: a) the LS 55, b) solid sample holder of the LS 55 with a fluorite sample mounted

As can be seen in figure 25 b an additional ring was inserted between the sample and the front side of the solid sample holder. This was done because it turned out that the holder could be adjusted to a more intense signal that way. The guiding slots from the original positioning system seemed to be too short. The ring was made of steel and painted with black stove enamel. Figure 26 shows the light path in the instrument.



Figure 26: Optical layout of the LS 55 [135]

1.6 Spectral Databases

According to the diploma thesis contract with Binder + Co this thesis should contain an overview over the current situation concerning available spectral data of minerals in the literature, with the main focus on industrially relevant minerals. This chapter should reach the goal of working package 3b, mentioned in the contract [81]. An overview over free and commercially available spectral databases is given.

The spectral behavior of minerals, especially luminescence in general and fluorescence in particular are reported by many authors with hobby-mineralogical background [82, 83, 84]. In those publications fluorescent minerals are photographically documented under UV-light. Many authors distinguish between illumination with LW- (Long Wave) and SW- (Short Wave) – UV-light. These notations mean:

- LW: excitation at 366 nm wavelength
- SW: excitation at 254 nm wavelength

These wavelengths are available with many UV-mercury-lamps for laboratory or field use.

It should be noted, that some fluorescence databases on minerals in the internet are provided by semiprofessional hobby-collectors. In this chapter not only fluorescence databases of minerals are covered, but also databases containing information on transmission and reflection data of minerals. Some minerals show transparency which can be compared with the transparency of glass. An example for that is Quartz. Most of the project relevant materials are not transparent. For reflectance spectroscopy wide applications can be found in astronomy, industry and the military sciences.

Though this chapter gives a good overview over possible sources of information, the spectral features of minerals are often deposit-dependent. Thus data from data bases can only give hints were to look for interesting peaks in a spectrum. Therefore no database can substitute a careful experimental study in the spectroscopic laboratory for the particular case of mineral.

To the best of the author's knowledge 4 reference books on fluorescence spectroscopy of minerals have been printed in the last 30 years and are essential for understanding:

- Gorobets, B. S., *Luminescent Spectra of Minerals Reference Book, Luminescent Spectra of Minerals*; RPC VIMS; Moscow; 2002: a spectral atlas with a good theoretical introduction
- Gaft, M., Reisfeld, R., Panczer, G.; *Modern Luminescence Spectroscopy of Minerals and Materials*; Springer; Berlin, Heidelberg; 2010: a spectral atlas, most of the spectral data are available in the free *fluomin.org* database
- Marfunin, A.S.; Spectroscopy, Luminescence and Radiation Centers in Minerals; Springer; Berlin, Heidelberg; 1979: The first published textbook which explicitly mentions fluorescence in minerals. Provides a good theoretical and practical overview, not of interest for practical application.
- Marfunin, A.S.; *Physics of Minerals and Inorganic Materials*; Springer; Berlin, Heidelberg; 1979: Introduction to solid state chemistry, solid state spectroscopy, quantum mechanics and group theory with focus on minerals.

1.6.1 Fluorescence databases

After exhaustive search in the internet a collection of the following fluorescence databases were obtained:

| Name of the | Link | Comment |
|--|--|--|
| database | | |
| Fluomin | http://www.fluomin. org/uk/accueil.php | free database; contains spectroscopic data as a gallery; spectra reproduced but no spectral data files (ASCII or .csv) available; 970 data sets available; information on certain luminescence centers "activators" |
| Mindat | http://www.mindat. org/min-3560.html | free database; provides a good overview over crystallographic data and fluorescence; no spectral data files provided; very elaborate data on minerals; information on certain luminescence centers "activators" and tailings |
| The Fluorescent Mineral Society | http://uvminerals.or g/fms/join-fms | Commercial with fee; database for collectors and hobby mineralogists; Account for Binder + Co ordered. |
| Fact-Index | http://www.fact- index.com/ http://www.fact- index.com/s/se/serp entine.html | free database; rough overview over certain minerals (also fluorescence behavior); not too detailed information, comparable to Wikipedia; |
| Athena | http://athena.unige.c h/athena/mineral/sea rch.html# | free database; database was not operable at the time of the search; not relevant because database didn't work properly |
| Jm- derochette | http://jm- derochette.be/spectr ometer.htm | free database; small database providing information on a few minerals; Spectral data under microscope; not relevant for the project |

Table 13: Overview over fluorescence databases for certain minerals

1.6.2 Reflectance spectroscopy databases

Table 14 gives an overview on the databases in the internet which provide reflectance spectra and further information on minerals.

| Name of the database | Link | Comment |
|---|--|---|
| United States Geological Survey | usgs.gov | Part of the ASTER database; free; overview over statistical data to minerals; the second link |
| | http://speclab.cr.usgs.gov/spectral.lib06/ds231/ datatable.html | leads to the spectral database |
| ASTER Spectral Library | http://speclib.jpl.nasa.gov/ | Summarizes data from smaller databases; free; all data are available as .csv files |
| GHOOST | http://ghosst.obs.ujf-grenoble.fr/ | French database project; data should be available with July 2012; because of this, no sample data available presently |
| Bio Rad | http://www.bio-rad.com/ | Commercial database; contains about 420 spectra to minerals and clays |
| | http://www.knowitall.com/literature/default.as p?gclid=CNrIo6eR864CFQJj3wod6hXWJg#D atabases | |
| JPL | http://speclib.jpl.nasa.gov/documents/jpl_desc | Part of the ASTER database, no explicit sample data provided in the report (for sample data see chapter for ASTER database); free |
| Caltech-Datenbank/RRUFF-Projekt | http://rruff.info/chem=Al/display=default/R05 0610 | Summarizes various databases; XRD, Raman and IR data available; free; links to primary literature are provided; original data cannot be downloaded |
| NIST-database | http://webbook.nist.gov/chemistry/#Search | Provides spectra for many chemicals; free; focus on photoelectron spectroscopy; because of that no reference data provided |
| Spectral Library of Arizona State University | http://speclib.asu.edu/ | Database for minerals and rocks; focus on data for astronomy and astronautics |
| Laboratory of Photoinduced Effects Vibrational and X-Ray Spectroscopie | http://www.fis.unipr.it/phevix/ramandb.php | Free database from the University of Parma (Italy); focus on Raman data; because of this the database is not relevant fort the project |
| Thermo Scientific | http://www.thermoscientific.com/ecomm/ servlet/productsdetail?productId=13281397&g roupType= PRODUCT&searchType=0&storeId=11152&f rom=search | Commercial database; no access available at the date of writing; presumably more data on samples from organic chemistry than from mineralogy |
| FDM Reference Spectra Database | http://www.fdmspectra.com/index.html | Commercial database on ATR-IR-spectra; no access available at the date of writing; possibility of 14 day free trial; focus on samples from organic chemistry |

Table 14: Overview over reflection spectroscopic databases

1.6.3 Assesment of the Databases

The database and literature search showed that for the same mineral from different deposits different fluorescence behavior is to be expected depending on the content of luminescence centers (rare earths and others).

For powder reflection spectra (see dataset for Scheelite in ASTER) it can be said that the intensity of the peaks depends on the particle size of the powder. For Scheelite the intensity increases with increasing particle size.

Commercial databases for NIR data of minerals are not so extensive in comparison with free databases (for example ASTER). ASTER provides about 1400 spectra of minerals whereas Bio Rad has only 400 spectra in their database. Based on these facts it is recommended to stay with the free databases.

The Henkel Glossary, however, may be an interesting source of information. It contains a collection of fluorescence data covering about 570 mineral species. The price of the glossary is 18,50 \$. But after 3 months of e-mail correspondence and waiting for an answer the glossary must be considered as not available any more.

The whole database search can be broken down to two sections with five relevant and recommendable databases. For clarity each of these databases is indicated by a number to refer to it:

Reflection spectroscopic databases on minerals:

- **ASTER (1)**
- USGS (2)
- Speclib (3)

Fluorescence spectroscopic databases on minerals:

- Fluomin (4)
- Mindat (5) (also very good to get general and further information on the interesting mineral)

These five databases are listed with their link in the table 15.

Table 15: Summary of the five most important databases with their corresponding link

| Datebase | Number | Link | |
|----------|--------|---|--|
| ASTER | 1 | http://speclib.jpl.nasa.gov/ | |
| USGS | 2 | http://speclab.cr.usgs.gov/spectral.lib06/ds231/datatable.htm | |
| Speclib | 3 | http://speclib.asu.edu/ | |
| Fluomin | 4 | http://www.fluomin.org | |
| Mindat | 5 | http://www.mindat.org | |

During the research for this report it became obvious that there is a lot of data for NIR-reflection spectroscopy on minerals available, but only little data for the UV-VIS reflection and fluorescence

behavior of minerals. The books of Gorebets & Rogojine and Gaft et al could be considered as the only source books for mineral fluorescence spectra available on the market.

Since the fluorescence and reflection behavior of minerals is highly dependent on the deposit there is no way to avoid careful studies in the lab or pilot installation. For each application concrete measurements have to be carried out because there is no database that covers all deposits of industrial mineral in all interesting spectral ranges. This justifies the investment in certain lab-instruments in the context of the ongoing research project.

Finally the five remaining databases were searched to get information on 8 minerals of interest, defined in the introduction. The results are summarized in table 16.

| Mineral of interest | Tailings | Fluorescence of the mineral (spectra) | Reflection properties of the mineral (spectra) | Further information |
|---------------------|----------|---------------------------------------|--|------------------------|
| Bauxite | 5 | | | 5 |
| Chromite | 5 | 4 | 1, 2 | 5 |
| Feldspar | 5 | 4 | 1 | 5 |
| Calcite | 5 | 4 | 1,2,3 | 5 |
| Scheelite | 5 | 4 | 1 | 5 |
| Talc | 5 | 4 | 1,2,3 | 5 |
| Fluorite | 5 | 4 | 1,3 | 5 |
| Magnesite | 5 | 4 | 1,3 | 5 |

Table 16: Information on 8 industrial minerals in the 5 relevant databases

2 Materials and Methods

2.1 Sample Preparation

The mineral samples were cut with a flagstone cutting machine mounted with a diamond cutting disc. The cut face was then polished with abrasive papers of different roughness. The samples presented in this work where prepared with TU-Graz preparation devices, the other project relevant samples were prepared by Georg Weingrill with the machines at the MUL.

Both preparation places are depicted in figure 27.



Figure 27: a) polishing device TUG, b) cutting machine TUG, c) polishing place MUL and d) cutting machine MUL

It turned out that cutting and polishing of the monolithic mineral samples is a sufficient preparation for further analysis in the L950 the LS 55 or the Raman-spectrometer.

2.2 Reflection Measurement of Minerals

2.2.1 Measurement Procedure

The L950 spectrometer was allowed to warm up for about 30 minutes. After that the measurement parameters were set in the control window. The most important measurement parameters are given in table 17.

| D ₂ - lamp | on |
|-----------------------|--------|
| Tungsten-lamp | on |
| Scan from [nm] | 2500 |
| Scan to [nm] | 200 |
| Data interval [nm] | 5 |
| Ordinate mode | %R |
| Lamp Change [nm] | 319,2 |
| Gain - InGaAs | 16,00 |
| PMT - response [s] | 0,20 |
| InGaAs - response [s] | 0,20 |
| PMT -slit [nm] | 2,00 |
| InGaAs - slit | auto |
| CBM [%] | 100,00 |
| CBD | off |
| detector change [nm] | 860,80 |

Table 17: Measurement parameters for reflection measurements with the L950

However, it should be mentioned that the measurement settings can vary according to the measurement task. For example the data interval can be minimized up to 0,01 nm, at the cost of scan speed. For mechanical reasons the scan should always start from maximal wavelength to the smallest wavelength of a spectrum.

After setting the parameters, the instrument was blanked with a certified spectralon standard¹³ from labsphere® using the autozero function. The sample was fixed at the reflection port with adhesive tape or modeling material. Then the measurement chamber was sealed lightproof with the sealing cap. When a 8 mm teflon aperture was used, e. g. for measurement of small samples, the blanking was done with the aperture already in position, to avoid disturbing signals from the aperture.

¹³ USRS- 99-020 AS-01159-060

Serial Number: 7A 33D-7000

2.3 Fluorescence Measurements of Minerals

2.3.1 Method Development and Measurement Procedure

All samples can be placed into the measurement chamber of the LS 55 after proper cutting and polishing. The luminescence measurement, which seemed an easy task at the beginning, is rather difficult for minerals, because they seem to have rather long living excited states. The LS 55 which is usually designed for life sciences applications can be disturbed by life time effects of the sample.

The LS 55 works in certain measurement cycles. Data are obtained from the photomultplier, integrated, converted, digitally filtered and rationed before the PC receives the data. The path of the signal is described in the Perkin Elmer User Manual for the LS 55 [136].



Figure 28: Electronics diagram for the LS 55 [136]

According to the manual the instrument can operate in two possible measurement modes:

- Fluorescence
- Phosphorescence

In fluorescence mode four integrations are performed for every data collection cycle. Two integrations are taken from the emission channel and two from the excitation channel. These integrations are performed at fixed times with respect to the last source flash. Emission from the light source has a width at half peak height of less than 10 microseconds, the integrators are opened for 80 microseconds to collect all the signal. The effect of dark current (signal produced when no light is falling on the photomultplier) is eliminated by gating open both channels a second time just before the next flash and integrating the signal. The dark current signals are then subtracted from the main fluorescence signals to give a dark current corrected signal [137].

In phosphorescence mode the integration time is not fixed, but can be selected by the operator. The integration can be started between 0 s and 9000 ms after the start of the flash. This is the delay time. The time period over which the integration is performed, the gate time, can be varied from 0,01 ms to 500 ms. If the sum of the delay and gate times exceeds 13,0 ms the cycle time must be increased to allow a longer data collection period. The source can be pulsed between 1 and 10 times, to optimize the sample excitation and data collection. The exciting pulses occur on consecutive mains cycles (50 Hz for AC supply in Austria) at the start of the data collection cycle. The gate and delay times are measured form the beginning of the last pulse in the excitation pulse train. On initiating a phosphorescence measurement the dark current is measured and the value stored and subtracted from all sample signals [178].

The further details of signal handling will not be discussed, but can be looked up in figure 29.



Figure 29: Data handling diagram

The measurement procedure can be broken down to a simple diagram:



Figure 30: Measurement scheme of the LS 55 (not to scale)

Now in fluorescence mode any long lived luminescence can be rejected due to dark current subtraction, whereas in phosphorescence mode short lived luminescence can not be measured because of the time gating.

Based on these facts method details for the luminescence measurement in solids, which can show either fluorescence or phosphorescence, were proposed by Dr. Stuart Huckins, a former product developer of Perkin Elmer [138].

| Cycle time [ms] | 20 |
|-----------------|-----|
| Flash Count | 1 |
| Delay time [ms] | 0,1 |
| Gate time [ms] | 3 |

Table 18: Proposed setting for LS 55 for long lived luminescence

Only using these proposed settings sensible spectra, which agree with the visual color impression for several luminescent minerals were obtained. Based on this experience an optimal measurement routine for fluorescing minerals should be as follows:

- 1. Take a photograph of the sample under UV-light (e.g. 254 nm or 366 nm)
- 2. Measure the sample in fluorescence mode
- 2.1. If no signal can be obtained increase sensitivity via the slit width or the detector voltage
- 3. Measure the sample in phosphorescence mode
 - 3.1. If no signal can be obtained increase sensitivity via the slit width or the detector voltage
- 4. Compare the photograph (visual color impression) with the fluorescence and/or phosphorescence data and make sure they match in principle.
- 5. Compare the spectra with spectra of the same mineral in databases.
- 6. If possible cross reference with data from other spectrofluorimeters

2.4 Illumination situation in the LS 55

2.4.1 Fundamentals

An important question is how the illumination situation in the measurement chamber and the detector performance can be compared with the illumination conditions in industrial sorting systems.

Several approaches have been made to find this out:

- Investigation in the manuals of the manufacturer and references therein.
- Information search in the data sheets for the Xe-flash lamp and the used detection system.
- Summary of the signal processing in the LS 55 instrument. •
- Measurement of irradiance in the VIS (400 700 nm) with the Testo 545 luxmeter with various • slit width.
- Measurement of the irradiance in the UV C with the UVM CP radiometer in the reflection • position of the monochromator.
- Measurement of the irradiance at 254 nm with various slit width with a chemical actinometer.
- Comparison of the irradiance of several fluorescence excitation systems.

First a few definitions from the field of "Photonics" [67, 88] :

It can be distinguished between the radiometric and the photometric approach. The radiometric approach is based on straight forward physical reasoning. The photometric approach takes into account the brightness sensitivity¹⁴ of the standard observer. This brightness sensitivity is defined as a function in the DIN 5031 in 10 nm steps.

Some definitions:

The radiant energy¹⁵ \mathbf{Q} is the amount of energy transferred via electromagnetic radiation in J (J = W·s).

The radiant power¹⁶ Φ is defined as

$$\boldsymbol{\Phi} = \frac{dQ}{dt} \qquad Equ. \ 18$$

and is given in W (1 W = 1Js⁻¹).

The **irradiance**¹⁷ **E** is defined as

$$E = \frac{d\Phi}{dA} \qquad Equ. 19$$

Where A is the *irradiated area* and is given in W/m^2 .

¹⁴ German: Hellempfindlichkeitsgrad

 ¹⁵ German: Strahlungsenergie
 ¹⁶ German: Strahlungsleistung

¹⁷ German: Bestrahlungsstärke

The irradiation¹⁸ H is defined as the time integral of the *irradiance*:

$$H = \int E \, dt \qquad Equ. \ 20$$

These are the main equations we have to keep in mind, when talking about irradiation measurement in radiometric terms.

All these quantities have their counterpart in photometric terms, where the sensitivity of the human eye for certain wavelengths is taken into account.

Figure 31 shows the brightness sensitivity of a standard observer for daylight (photopic range) [89] defined by the CIE (Commission International de l'Éclairage) and documented the German DIN 5031 as a function of the wavelength λ in nm.



The luminous flux¹⁹ φ is measured in Lumen (lm). This leads to the unity for the quantity of light²⁰ in $lm \cdot s$ ("lumensecond"). This leads to the **luminance intensity**²¹ in lm/m^2 which is defined as one **lux** (lx):

$$1 lx = 1 \frac{lm}{m^2} \qquad Equ. 21$$

For the conversion of photometric units X_p to radiometric X_r units and vice versa in the case of monochromatic radiation the following equation can be used

$$X_p = K_m V(\lambda) X_r$$
 Equ. 22

where $K_m = 683 \text{ lm/W}$ is the maximum value of the *photometric radiation equivalent*²², whose value comes from the definition of the measurement unit candela.

¹⁸ German: Bestrahlung
¹⁹ German: Lichtstrom
²⁰ German: Lichtmenge

 ²¹ German: Beleuchtungsstärke
 ²² German: Photometrisches Strahlungsequivalent

For polychromatic radiation the spectral entities $X_{r,\lambda} = dX_p/d\lambda$ have to be integrated in the limits of the visible radiation [67]:

$$X_p = K_m \int_{380 nm}^{780 nm} V(\lambda) X_{e,\lambda} d\lambda \ Equ. 23$$

The definition of the unit candela was a consequence from the practical properties resulting of the handling of a real black body at higher temperatures to get a standard source for radiation in the VIS-range to measure the optical radiation power. It is defined as [90]:

The **candela** is the luminous intensity, in a given direction, of a source that emits monochromatic radiation of frequency $540 \cdot 10^{12}$ hertz (i.e. a wavelength of 555 nm) and that has a radiant intensity in that direction of 1/683 watt per steradian.

From the author's point of view the most useful quantity for a comparison of the illumination situation in the LS55 and in industrial sorting machines is the irradiance in W/m^2 or W/cm^2 .

To get the energy of one photon we can apply the known equation [91]:

$$E_{ph} = hv = \frac{hc_0}{\lambda}$$
 Equ. 24

where E_{ph} is the energy of the photon in [J], h is Planck's constant $h = 6,626 \cdot 10^{-34}$ [Js], v is the frequency of the photon in [s⁻¹], c₀ is the vacuum-velocity of light c₀ = 299 \cdot 10⁶ [m s⁻¹] and λ is the wavelength in [m].

Table 19 gives an overview over radiometric and photometric quantities.

| Radiometry | | | Photometry | | |
|----------------------|--------|------------------|--------------------|--------|------------------------|
| Quantity | symbol | units | Quantity | symbol | units |
| Radiant Energy | Q | J | Luminous energy | Q | lm s |
| Radiant Flux | Φ | W | Luminous flux | Φ | lm |
| Irradiance | Ε | W/m ² | Illuminance | Ε | $lm/m^2 = lx$ |
| Radiant Intensity | Ι | W/sr | Luminous Intensity | Ι | lm/sr |
| Radiance | L | $W/(m^2 sr)$ | Luminance | L | lm/(m ² sr) |

Table 19: Radiometric and photometric quantities [92, 93, 94, 95]

2.4.2 Manuals and Quotes

According to the quote for the LS 55 fluorescence spectrometer the device is equipped with a pulsed Xenon light source. Neither information on the power of this source nor on the energy of one pulse was provided. The spectrometer can be used to measure fluorescence, phosphorescence and bio- or chemiluminescence. The dark current of the detector is automatically corrected (which is known in the literature as "excitation correction") and the dark current of the detection system is automatically compensated. Available filters, polarizers and attenuators are [96]:

- 290 nm cut off filter (emission side)
- 350 nm cut off (emission side)
- 390 nm cut off(emission side)
- 430 nm cut off (emission side)
- 515 nm cut off (emission side)
- 1 % attenuator (emission side)
- shutter (emission side)
- horizontal and vertical polarizers (on excitation and emission side)

From the technical specifications for the LS 55 we know that the Xe flash lamp is pulsed at line frequency (50 or 60 Hz) with a pulse width at half peak height < 10 μ s and a power equivalent to 20 kW at continuous operation. The excitation slit can be varied in the interval 2,5 – 15 nm and the emission slit in the interval 2,5 – 20 nm [97].

In general authors provide information on the pulse energy of their lasers in millijoule and the deliver pulse duration in Nanoseconds. The power can be easily calculated with the known equation

$$P[W] = \frac{E[J]}{t[s]} \qquad Equ. 25$$

The following table gives a short overview of the Xe-flash lamp power in comparison to some examples for Laser Induced Fluorescence (LIF) from the literature.

| E [mJ] | [ns] | P [W] | Reference | Comment |
|--------|----------------------|------------------|-----------|---|
| | * | $20 \cdot 10^3$ | [97] | Power for the whole emission spectrum |
| 80 | 10 | $8 \cdot 10^6$ | [99] | pulse energy maintained between 10 - 80 mJ |
| 80 | 10 | $8 \cdot 10^{6}$ | [100] | pulse energy maintained between 10 - 80 mJ |
| 80 | 10 | $8 \cdot 10^{6}$ | [101] | pulse energy maintained between 10 - 80 mJ |
| 2 | 3 according to [103] | $6,7 \cdot 10^5$ | [102] | laser energy between 1 - 2 mJ per Pulse @ 20 Hz |

Table 19: Overview over excitation power P for mineral fluorescence from several references

*The emission from the source has a width at half peak height of less than $10 \ \mu s$ [98]
However the pulse duration to pause ratio was not mentioned in the literature references [99], [100] and [101].

Concerning the rather high excitation power of the laser sources the question remains how these laser intensities can be compared to irradiation intensities in common UV-C lamps.

For example the UV-C tube in Binder + Co sorting systems has a irradiance of 20 mW/cm² at the closest possible measurement point to the lamp and a irradiance of about 1,6 mW/cm² at the position of the material that should be sorted [104].

From the data in table 20 it becomes obvious why many authors use lasers as excitation source. Lasers emit their whole energy within one sharp coherent emission line whereas Xe-flashlamps have a continuum emission spectrum.

Since Nd-YAG-Lasers have an emission wavelength of about 1060 nm a frequency doubling or even tripling is necessary to get into the visible range of electromagnetic radiation [105]. For frequency doubling from 1,08 to 0,54 μ m up to 85 % conversion efficiency are reported [106]. In everyday laboratory work conversion efficiencies of 60 % are realistic [107].

2.4.3 Xe-flash lamp and the detector

2.4.3.1 The lamp

Though the emission in the UV is not too high for a Xe-flash lamp it is used in the LS 55. A Mercury-Lamp would only have several sharp maxima which make the recording of excitation spectra almost impossible. The excitation spectrum would be biased by the strong emission lines [108].

There are several types of excitation sources known from the literature [110]:

- Arc and incandescent Xe lamps
- Pulsed Xe lamps
- High pressure Hg lamps
- Xe-Hg arc lamps
- Quartz-Tungsten Halogen (QTH) lamps
- Low pressure Hg and Hg-Ar lamps
- LED light sources
- Laser Diodes

The emission spectrum of a Xe-flash lamp in comparison to a continuous arc lamp is shown in figure 32.



Figure 32: Spectral output of a continuous Xe arc lamp and Xe flash lamp [109]

For comparison the emission spectra²³ of the commercially available UV-lamp NU-4 KL were recorded with the LS 55 and are shown in figure 33:



Figure 33: Emission spectra for the UV-lamp NU-4 KL for setting of lamp to a) 254 nm and b) 366 nm Figure 34 shows the emission spectrum of a low pressure Hg-Ar-lamp:

²³ These spectra were emission corrected with the emred.corr function provided by Perkin Elmer



Figure 34: Emission spectrum of a low pressure Hg-Ar-lamp [111]

However, the Xe flash lamp in the LS 55 seems to be a good compromise between versatility and intensity.

2.4.3.2 R955 detector

To elevate the performance of the LS 55 a more sensitive photomultiplier tube was used as a detector. The original detector was a R8630 PMT from Hamamatsu. The R928 and the R955 are more sensitive than the R8630 which is a standard detector for biochemical applications. The R928 and R955 are also more sensitive towards the red region of the visible electromagnetic spectrum [112]. Figure 35 shows the spectral response for both, the R928 and the R955.



Figure 35: Typical spectral response for R928- and R955-PMT [112]

2.4.4 Testo 545 measurements: VIS

The Illuminance E was measured with the Testo 545 Luxmeter. The measuring chamber was opened and the measurement carried out at different wavelengths and slit widths. The laboratory was kept dark to avoid a bias from the light sources in the lab. Figure 36 shows the positioning of the measurement surface of the Testo 545 in the measurement spot. The instrument was held at a position where it gave maximal signal. The area of the measurement surface is $33,36 \text{ mm}^2$.



Figure 36: Measurement surface of Testo 545 in the LS 55

The results of the measurements are presented in tables 20 and 21 and figures 37 and 38.

| | slit width [nm] | | | | | | | | | | | | | | |
|------|-----------------|------|-------|------|-------|------|-------|------|-------|------|-------|--|--|--|--|
| 2 | 2,5 5 | | 7,5 | | 10 | | 12,5 | | 15 | | | | | | |
| λ | Е | λ | Е | λ | Ε | λ | Е | λ | Е | λ | Ε | | | | |
| [nm] | [Lux] | [nm] | [Lux] | [nm] | [Lux] | [nm] | [Lux] | [nm] | [Lux] | [nm] | [Lux] | | | | |
| 200 | 0 | 200 | 0 | 200 | 0 | 200 | 0 | 200 | 0 | 200 | 0 | | | | |
| 254 | 0 | 254 | 0 | 254 | 0 | 254 | 0 | 254 | 0 | 254 | 0 | | | | |
| 300 | 0 | 300 | 0 | 300 | 0 | 300 | 0 | 300 | 0 | 300 | 0 | | | | |
| 366 | 0 | 366 | 0 | 366 | 0 | 366 | 0 | 366 | 0 | 366 | 0 | | | | |
| 400 | 0 | 400 | 0 | 400 | 0 | 400 | 1 | 400 | 1 | 400 | 1 | | | | |
| 450 | 0 | 450 | 1 | 450 | 2 | 450 | 2 | 450 | 3 | 450 | 5 | | | | |
| 500 | 1 | 500 | 10 | 500 | 20 | 500 | 40 | 500 | 55 | 500 | 78 | | | | |
| 550 | 6 | 550 | 53 | 550 | 70 | 550 | 253 | 550 | 308 | 550 | 459 | | | | |
| 600 | 3 | 600 | 18 | 600 | 44 | 600 | 68 | 600 | 107 | 600 | 115 | | | | |
| 650 | 1 | 650 | 1 | 650 | 3 | 650 | 3 | 650 | 3 | 650 | 7 | | | | |
| 700 | 0 | 700 | 0 | 700 | 1 | 700 | 1 | 700 | 1 | 700 | 1 | | | | |

Table 20: Illuminance values for several slit widths and wavelengths



Figure 37: Illuminance values for several slit widths (in nm) and wavelengths at the measurement spot of LS 55

| slit width [nm] | illuminance [lux] |
|-----------------|-------------------|
| 2,5 | 6 |
| 5 | 53 |
| 7,5 | 70 |
| 10 | 253 |
| 12,5 | 308 |
| 15 | 459 |

Table 21: Illuminance and slit width at 550 nm



Figure 38: Illuminance values for several slit widths at 550 nm

After the experiments at several excitation wavelengths, the excitation monochromator was set to the reflection position. So the whole emission spectrum of the Xe-flash lamp was directed to the Testo 545 instrument. First positioning of the measurement area was tried by free hand. To get higher accuracy the measurement device was fixed to the cuvette holder with tape. Results of these measurements are presented in table 22 and figure 39.

| Positioning by | hand | fixing to the cuve | tte holder | |
|-----------------|---------|--------------------|------------|--|
| slit width [nm] | E [lux] | slit width [nm] | E [lux] | |
| 15 | 2580 | 15 | 880 | |
| 14 | 2500 | 14 | 855 | |
| 13 | 2470 | 13 | 820 | |
| 12 | 2390 | 12 | 790 | |
| 11 | 2308 | 11 | 740 | |
| 10 | 2280 | 10 | 690 | |
| 9 | 2050 | 9 | 630 | |
| 8 | 1980 | 8 | 566 | |
| 7 | 1590 | 7 | 486 | |
| 6 | 1005 | 6 | 408 | |
| 5 | 663 | 5 | 313 | |
| 4 | 605 | 4 | 218 | |
| 3 | 362 | 3 | 124 | |
| 2,5 | 293 | 2,5 | 73 | |

Table 22: Illuminance values for the LS 55 at reflection position of the excitation monochromator



Figure 39: Illuminance values for the LS 55 at reflection position of the excitation monochromator

The photometric values for illuminance can be converted to radiometric values for Irradiance using equation 26 [115]:

$$E_{irrad} = \frac{E_{illum}}{K_m \cdot V(\lambda)} \qquad Equ. \ 26$$

In equation 26 E_{irrad} is the irradiance in W/m², E_{illum} is the Illuminance in lm/m², K_m the luminous efficacy of radiation²⁴ in lm/W and V(λ) the spectral luminous efficiency²⁵ defined in DIN 5031. All E_{irrad} values were multiplied with 10⁻⁴ [m²/cm²] to get the irradiance in units of W/cm². K_m = 683 lm/W and V(550 nm) = 1 [115]. The results of the unit conversion are presented in tables 23, 24 and 25 as well as in figure 40.

 ²⁴ luminous efficacy of radiation: Ger.: photometrisches Strahlungsäquivalent
 ²⁵ spectral luminous efficiency: Ger.: spektraler Hellempfindlichkeitsgrad

| | | | S | lit width [1 | ım] | | | |
|---------------------------------|-------------------------------|--|--|-------------------------------|--|--|-------------------------------|--|
| | | | | 5 | 7,5 | | | |
| WL [nm] | Ill.[Lux] | Irr. [W/cm ²] | WL [nm] | III. [Lux] | Irr. [W/cm ²] | WL [nm] | III. [Lux] | Irr. [W/cm ²] |
| 200 | 0 | 0,00E+00 | 200 | 0 | 0,00E+00 | 200 | 0 | 0,00E+00 |
| 254 | 0 | 0,00E+00 | 254 | 0 | 0,00E+00 | 254 | 0 | 0,00E+00 |
| 300 | 0 | 0,00E+00 | 300 | 0 | 0,00E+00 | 300 | 0 | 0,00E+00 |
| 366 | 0 | 0,00E+00 | 366 | 0 | 0,00E+00 | 366 | 0 | 0,00E+00 |
| 400 | 0 | 0,00E+00 | 400 | 0 | 0,00E+00 | 400 | 0 | 0,00E+00 |
| 450 | 0 | 0,00E+00 | 450 | 1 | 1,46E-07 | 450 | 2 | 2,93E-07 |
| 500 | 1 | 1,46E-07 | 500 | 10 | 1,46E-06 | 500 | 20 | 2,93E-06 |
| 550 | 6 | 8,78E-07 | 550 | 53 | 7,76E-06 | 550 | 70 | 1,02E-05 |
| 600 | 3 | 4,39E-07 | 600 | 18 | 2,64E-06 | 600 | 44 | 6,44E-06 |
| 650 | 1 | 1,46E-07 | 650 | 1 | 1,46E-07 | 650 | 3 | 4,39E-07 |
| 700 | 0 | 0,00E+00 | 700 | 0 | 0,00E+00 | 700 | 1 | 1,46E-07 |
| | 10 | | | 1 | 2,5 | | 15 | |
| WL [nm] | Ill. [Lux] | Irr. [W/cm ²] | WL [nm] | III. [Lux] | Irr. [W/cm ²] | WL [nm] | III. [Lux] | Irr. [W/cm ²] |
| 200 | 0 | 0,00E+00 | 200 | 0 | 0,00E+00 | 200 | 0 | 0,00E+00 |
| 254 | | | | | | | | |
| | 0 | 0,00E+00 | 254 | 0 | 0,00E+00 | 254 | 0 | 0,00E+00 |
| 300 | 0 | 0,00E+00 0,00E+00 | 254 300 | 0 | 0,00E+00 0,00E+00 | 254 300 | 0 | 0,00E+00 0,00E+00 |
| 300 366 | | · · · · · · · · · · · · · · · · · · · | | | · · · · · · · · · · · · · · · · · · · | | | , |
| | 0 | 0,00E+00 | 300 | 0 | 0,00E+00 | 300 | 0 | 0,00E+00 0,00E+00 |
| 366 | 0 | 0,00E+00 0,00E+00 | 300 366 | 0 | 0,00E+00 0,00E+00 | 300 366 | 0 | 0,00E+00 0,00E+00 1,46E-07 |
| 366 400 | 0 | 0,00E+00 0,00E+00 1,46E-07 | 300 366 400 | 0 | 0,00E+00 0,00E+00 1,46E-07 | 300 366 400 | 0 0 1 | 0,00E+00 0,00E+00 1,46E-07 7,32E-07 |
| 366 400 450 | 0 0 1 2 | 0,00E+00 0,00E+00 1,46E-07 2,93E-07 | 300 366 400 450 | 0 0 1 3 | 0,00E+00 0,00E+00 1,46E-07 4,39E-07 | 300 366 400 450 | 0 0 1 5 | 0,00E+00 |
| 366 400 450 500 | 0 0 1 2 40 | 0,00E+00 0,00E+00 1,46E-07 2,93E-07 5,86E-06 | 300 366 400 450 500 | 0 0 1 3 55 | 0,00E+00 0,00E+00 1,46E-07 4,39E-07 8,05E-06 | 300 366 400 450 500 | 0 0 1 5 78 | 0,00E+00 0,00E+00 1,46E-07 7,32E-07 1,14E-05 |
| 366 400 450 500 550 | 0 0 1 2 40 253 | 0,00E+00 0,00E+00 1,46E-07 2,93E-07 5,86E-06 3,70E-05 | 300 366 400 450 500 550 | 0 0 1 3 55 308 | 0,00E+00 0,00E+00 1,46E-07 4,39E-07 8,05E-06 4,51E-05 | 300 366 400 450 500 550 | 0 0 1 5 78 459 | 0,00E+00 0,00E+00 1,46E-07 7,32E-07 1,14E-05 6,72E-05 |

Table 23: Various excitation slit widths - Testo 545 results in photometric and radiometric units

Table 24: Constant emission wavelength - Testo 545 results in photometric and radiometric units

| slit width [nm] | Illum. @ 550 nm [Lux] | Irrad. @ 550 nm [W/cm ²] |
|-----------------|------------------------|--------------------------------------|
| 2,5 | 6 | 8,78477E-07 |
| 5 | 53 | 7,75988E-06 |
| 7,5 | 70 | 1,02489E-05 |
| 10 | 253 | 3,70425E-05 |
| 12,5 | 308 | 4,50952E-05 |
| 15 | 459 | 6,72035E-05 |

| P | ositioning by ha | nd | Fixing to the cuvette holder | | | | |
|-----------------|------------------|-----------------------------|------------------------------|---------------|-----------------------------|--|--|
| slit width [nm] | Illum. [Lux] | Irrad. [W/cm ²] | slit width [nm] | Illum. [Lux] | Irrad. [W/cm ²] | | |
| 15 | 2580 | 3,78E-04 | 15 | 880 | 1,29E-04 | | |
| 14 | 2500 | 3,66E-04 | 14 | 855 | 1,25E-04 | | |
| 13 | 2470 | 3,62E-04 | 13 | 820 | 1,20E-04 | | |
| 12 | 2390 | 3,50E-04 | 12 | 790 | 1,16E-04 | | |
| 11 | 2308 | 3,38E-04 | 11 | 740 | 1,08E-04 | | |
| 10 | 2280 | 3,34E-04 | 10 | 690 | 1,01E-04 | | |
| 9 | 2050 | 3,00E-04 | 9 | 630 | 9,22E-05 | | |
| 8 | 1980 | 2,90E-04 | 8 | 566 | 8,29E-05 | | |
| 7 | 1590 | 2,33E-04 | 7 | 486 | 7,12E-05 | | |
| 6 | 1005 | 1,47E-04 | 6 | 408 | 5,97E-05 | | |
| 5 | 663 | 9,71E-05 | 5 | 313 | 4,58E-05 | | |
| 4 | 605 | 8,86E-05 | 4 | 218 | 3,19E-05 | | |
| 3 | 362 | 5,30E-05 | 3 | 124 | 1,82E-05 | | |
| 2,5 | 293 | 4,29E-05 | 2,5 | 73 | 1,07E-05 | | |

 Table 25: excitation monochromator in reflection position – Testo 545 results in photometric and radiometric units



Figure 40: Testo 545 results in irradiance

2.4.5 UVC intensity measurements

All measurements with the UVM-CP radiometer in the LS 55 showed a value of zero W/cm^2 . Therefore it could be assumed, that the used instrument is not sensitive enough. The functionality of the device was tested with a 4W UV-lamp.

Several measurements have been carried out with the UVM-CP instrument on the NU-4 KL UV-lamp at various distances of measurement device to lamp.



Figure 41: a) The UV-Lamp NU-4 KL, b) UVM CP radiometer, c) experimental setup

| | wavelength | | | | | | | | | | |
|------------------|------------|--------|------------------------------------|--|--|--|--|--|--|--|--|
| 25 | 54 nm | 366 nm | | | | | | | | | |
| distance [cm] | 2 | | Irradiance [W/cm ²] | | | | | | | | |
| 0 | 3,12 | 0 | 0,03 | | | | | | | | |
| 5 | 0,71 | 5 | 0 | | | | | | | | |
| 10 | 0,25 | 15 | 0 | | | | | | | | |
| 15 | 0,12 | 20 | 0 | | | | | | | | |
| 20 | 0,06 | 20 | 0 | | | | | | | | |
| 25 | 0,02 | 25 | 0 | | | | | | | | |
| 30 | 0,01 | 30 | 0 | | | | | | | | |
| 35 | 0 | 35 | 0 | | | | | | | | |
| 40 | 0 | 40 | 0 | | | | | | | | |
| 45 | 0 | 45 | 0 | | | | | | | | |
| 50 | 0 | 50 | 0 | | | | | | | | |
| 55 | 0 | 55 | 0 | | | | | | | | |
| 60 | 0 | 60 | 0 | | | | | | | | |
| 65 | 0 | 65 | 0 | | | | | | | | |

Table 26: Experimental data of irradiance for various distances to the UV-light source



Figure 42: irradiance vs. distance to a 4 W UV-lamp set at 254 nm emission wavelength

2.4.6 Actinometer measurements

Measurements with a chemical actinometer for the UV-region reported by Rahn [116] were used to determine the irradiation intensity (in W/m^2) in the Luminescence Spectrometer LS 55. A solution of 0,6 M iodide and 0,1 M iodate in 0,01 M borate buffer at a pH of 9,25 was illuminated in the LS 55 at various slit widths.

The Borate-buffer contained 2,0127 g of water free $Na_2B_4O_7$ dissolved in 1000 mL H₂O to yield a concentration of 0,01 mol/L. The pH-value of the buffer was tested with a pH-meter²⁶ which was calibrated with standard buffer solutions²⁷ at 7,00 and 11,01 before the measurement (pH = 9,23).

For the actual measurement 9,9606 g KI and 2,1400 g KIO_3 where dissolved in 100 ml Borate-buffer solution.

The illumination wavelength was kept at 254 nm. According to the publication of Rahn [115] the overall reaction equation is:

$$8I^{-} + IO_{3}^{-} + 3H_{2}O \xrightarrow{hv} 3I_{3}^{-}$$
 Equ. 27

After illumination at maximum slit width dark smears can be seen in the cuvette indicating the production of I_3 a species, which absorbs in the short wavelength part of the visible range with a maximum at 352 nm. Before the measurement of the transmission spectra of the illuminated samples the cuvette was shaken to ensure good homogenization.

Transmission spectra of the irradiated solutions were measured in the L950 spectrometer, using the detector for transmission measurements. An empty cuvette of the same manufacturer was used as a reference in the reference beam slot. Before illumination of the sample a baseline was collected using both cuvettes (empty sample and reference cuvette).

Figure 43 compares the spectrum of the original and the illuminated solution.

²⁶ WTW – Vario with pH-Electrode SenTix 41

²⁷ Buffer solutions: Hanna Instruments buffers HI 70007 and HI 70010



Figure 43: Absorbance of a) the original and b) the illuminated actinometer solution

Six cuvettes with actinometer solutions were prepared, one cuvette for every slit adjustment. The cuvette for the actual adjustment was measured in the instrument after illumination periods of 0, 5, 10 and 15 minutes, respectively. The slit width was varied starting from 2,5 nm to 15,0 nm in steps of 2,5 nm.

| | Abso | rbance valu | ies @ 352 i | date experiment was carried out | |
|--|-----------|-------------|-------------|---------------------------------|------------|
| slit width [nm]/ illumination time [min] | 0 | 5 | 10 | 15 | |
| 15,0 | 0,0077095 | 0,17248 | 0,36558 | 0,55866 | 03.07.2012 |
| 12,5 | 0,0093607 | 0,18122 | 0,34908 | 0,51255 | 03.07.2012 |
| 10,0 | 0,00956 | 0,11215 | 0,20117 | 0,3155 | 03.07.2012 |
| 7,5 | 0,010037 | 0,071831 | 0,13242 | 0,19653 | 03.07.2012 |
| 5,0 | 0,054061 | 0,079556 | 0,10468 | 0,12754 | 04.07.2012 |
| 2,5 | 0,10048 | 0,1034 | 0,10459 | 0,10687 | 05.07.2012 |

Table 27: Original measurement data for the chemical actinometer measurements

The experiment was carried out in 3 days. This explains the slight increase of the absorbance of the nonirradiated solutions (see table 27), which is caused by ambient UV light, cosmic radiation and/or radioactivity. The sensitivity of the actinometer can even be used for dosimetry of ionizing radiation as reported from Rahn et al [117].

For the evaluation the zero value of each experiment at the fixed slit width was subtracted. These values are noted in table 28.

| | Absorbance values @ 352 nm | | | | | | | |
|--|----------------------------|-----------|-----------|-----------|--|--|--|--|
| slit width [nm]/ illumination time [min] | 0 | 5 | 10 | 15 | | | | |
| 15,0 | 0 | 0,1647705 | 0,3578705 | 0,5509505 | | | | |
| 12,5 | 0 | 0,1718593 | 0,3397193 | 0,5031893 | | | | |
| 10,0 | 0 | 0,10259 | 0,19161 | 0,30594 | | | | |
| 7,5 | 0 | 0,061794 | 0,122383 | 0,186493 | | | | |
| 5,0 | 0 | 0,025495 | 0,050619 | 0,073479 | | | | |
| 2,5 | 0 | 0,00292 | 0,00411 | 0,00639 | | | | |

Table 28: Corrected measurement data for the chemical actinometer measurements

These data can be plotted. It becomes evident that the absorbance increases with the length of the illumination period as well as the slit width and hence the chemical actinometer is a useful tool to assess the irradiation of the sample.



Figure 44: Absorbance values after correction for the actinometer experiment

The chemical actinometer was successfully used at the assessment of a corona reactor in a diploma thesis [118] at the TU-Graz. The following calculation of the irradiation intensity was taken from this work and the original papers from Rahn [116,119].

The absorption values of the actinometer solution can be used to calculate the irradiation intensity as follows:

$$c(I_3^-) = \frac{A_{352} \cdot S}{\varepsilon_{352} \cdot d}$$
 Equ. 28

Where $c(I_3^-)$ is the concentration of the iodate ion in mol/L, A is the value of the (corrected) absorbance in dimensionless unit of the actinometer solution, ε_{352} is the extinction coefficient for the iodate ion at 352 [nm] with the known value of $\varepsilon_{352}(I_3^-) = 27.600 \left[\frac{1}{M \cdot cm}\right]$ and is the thickness of the cuvette. (d = 1 [cm] for standard cuvettes). S is a dilution factor, which is S = 1 here, because the irradiated solutions were measured without further dilution.

The number of incident photons N_{ph} in [mol] can be calculated as follows:

$$N_{ph} = \frac{\Delta c(I_3^{-}) \cdot V_{cuv}}{QE_{\lambda}} \qquad Equ. \ 29$$

Where $\Delta c(I_3^{-})$ is the change in the concentration of the iodate ion in [mol/l], V_{cuv} is the volume of the cuvette in [m³] and QE_{λ} is the quantum yield of the actinometer-reaction in dimensionless units [] from 0 to 1. To keep the value for V_{cuv} constant, the cuvette was filled with the actinometer solution using a volumetric pipette²⁸ with nominal volume of 3 mL or $3 \cdot 10^{-6}$ m³.

The photon flux in [mol photons/s] can be calculated according to:

$$\Phi_P = \frac{N_{ph}}{\Delta t} \qquad Equ. \ 30$$

Where N_{ph} is the number of incident photons in [mol] and Δt is the time of irradiation in [s].

The desired irradiance P_{λ} in W without respect of the irradiated area follows the equation

$$P_{\lambda} = \Phi_P \cdot \frac{h \cdot c}{\lambda} \cdot N_A$$
 Equ. 31

Where Φ_P is the photon flux in [mol photons/s], h is Planck's constant with $h = 6,626 \cdot 10^{-34}$ [Js], c is the velocity of light with $c = 299 \cdot 10^6$ [m/s], λ the wavelength of the used radiation in m and N_A Avogadro's constant with N_A = $6,022 \cdot 10^{23}$ [1/mol].

The quantum yield QE_{254} of the actinometer reaction follows the empiric equation:

$$QE_{254} = 0,75[1+0,02\cdot(T-20,7)][1+0,23\cdot(c-0,577)]$$
 Equ. 32

²⁸ German: Vollpipette

Where T is the temperature in $[^{\circ}C]^{29}$ and c is the concentration of KI in [mol/L]. The temperature in the laboratory was kept constant at 23[$^{\circ}C$] via air condition and the actinometer solution was allowed to come to the room temperature. The concentration of KI is 0,6 [mol/L]. This gives a value of $PE_{254} = 0,789$

The illuminated area in the instrument was determined with a piece of millimeter paper an illumination of a spot of this paper at an excitation slit width of 15 nm, which is the maximum setting for the LS 55, at a wavelength of 550 nm. The illuminated area was 10.3 mm, which yields an illuminated area of 30 mm² or $3 \cdot 10^{-5} \text{ m}^2$.

It was assumed that the illuminated area does not change with the variation of the slit width.

The combination of equations 28-32 and division of P_{λ} with the irradiated area in cm² yields the irradiation intensity $P_{\lambda,A}$ in [W/cm²]:

$$P_{\lambda,A} = \frac{A_{352} \cdot S \cdot V_{cuv} \cdot h \cdot c \cdot N_A}{Q E_{254} \cdot \varepsilon_{352} \cdot d \cdot \Delta t \cdot \lambda \cdot A \cdot K} \qquad Equ. 33$$

Explanation of the terms in equation 33 is given above. K is the conversion factor from an area in m^2 to cm^2 . Using equation 33 the corrected absorbance values from table 29 can be used to calculate the irradiation intensity:

| term | explanation | unit | value | |
|-------------------------|---------------------------|--------------------------------|-----------|-------------|
| $P_{\lambda,A}$ | irradiance | [W/cm ²] | Х | numerator |
| A ₃₅₂ | absorbance @ 352 nm | [] | у | |
| S | dilution factor | [] | 1 | |
| V _K | cuvette volume | [m ³] | 3,00E-06 | |
| h | Planck's constant | [J s] | 6,626E-34 | |
| с | velocity of light | [m/s] | 2,99E+08 | |
| N _A | Avogadro's constant | [1/mol] | 6,022E+23 | |
| E ₃₅₂ | extinction coefficient | [1/((mol/l)m)] | 2,76E+03 | denominator |
| d | thickness of the cuvette | [m] | 1,00E-02 | |
| Δt | irradiation time | [s] | Z | |
| λ | wavelength | [m] | 2,54E-07 | |
| А | irradiated area | [m ²] | 3,00E-05 | |
| QE ₂₅₄ | quantum yield of reaction | [] | 0,789 | |
| K | conversion factor | $[\mathrm{cm}^2/\mathrm{m}^2]$ | 1E04 | |

Table 30: Parameters for calculation of irradiance with Equ. 33

²⁹ It is important to use the temperature in degree Celsius for the calculation.

| | co | rrected absor | bance values | s @ 352 nm | | |
|-------------------------|-----|---------------|--------------|------------|--------------------------|---------------|
| illumination time [sec] | 0 | 300 | 600 | 900 | | |
| slit width [nm] | - | - | - | - | | |
| 15 | 0 | 0,1647705 | 0,3578705 | 0,5509505 | | |
| 12,5 | 0 | 0,1718593 | 0,3397193 | 0,5031893 | | |
| 10 | 0 | 0,10259 | 0,19161 | 0,30594 | | |
| 7,5 | 0 | 0,061794 | 0,122383 | 0,186493 | | |
| 5 | 0 | 0,025495 | 0,050619 | 0,073479 | | |
| 2,5 | 0 | 0,00292 | 0,00411 | 0,00639 | | |
| | | | | | | |
| slit width [nm] | irr | adiance [W/o | em2] | | mean [W/m ²] | stdev. [W/m2] |
| 15 | 0 | 0,00E+00 | 1,18E-04 | 2,57E-04 | 2,57E-04 | 1,39E-04 |
| 12,5 | 0 | 0,00E+00 | 1,24E-04 | 2,44E-04 | 2,43E-04 | 1,19E-04 |
| 10 | 0 | 0,00E+00 | 7,38E-05 | 1,38E-04 | 1,44E-04 | 7,33E-05 |
| 7,5 | 0 | 0,00E+00 | 4,44E-05 | 8,80E-05 | 8,88E-05 | 4,48E-05 |
| 5 | 0 | 0,00E+00 | 1,83E-05 | 3,64E-05 | 3,59E-05 | 1,73E-05 |
| 2,5 | 0 | 0,00E+00 | 2,10E-06 | 2,96E-06 | 3,22E-06 | 1,27E-06 |

Table 29: Corrected absorbance values @ 352 nm and calculated irradiance values



Figure 45: Irradiance vs. slit width

2.4.7 Comparison to other illumination techniques

To summarize it could be said, that the irradiance of the measurement spot in the LS 55 is in the scale of about 10^{-4} – to 10^{-5} W/cm². In comparison the lead glass sorting systems of Binder + Co uses an irradiance of about $1.6 \cdot 10^{-3}$ W/cm². Typical pulse characteristics of a Nd-YAG laser used by Gaft et al for laser excitation of minerals are pulse durations t = 6 - 10 ns and pulse energies between P = 0, 1 - 1 J [120]. This³⁰ and the assumption of an irradiated area of about 1 mm² yields irradiance values of about 10⁹ W/cm^2 to about $10^{11} W/cm^2$.

For a comparison to possible LIF-laser sources the lasers which are listed by Broicher are shown in table 30 [121]. For the following table only conditions of highest possible irradiance³¹ were chosen (e.g. maximum power and smallest pulse duration). If no beam width was indicated about 1 mm was assumed to calculate the irradiance.

| Laser Type | | Name | Model | WL [nm] | Beamwidth [mm] | Pulse energy [J] | Power [W] | Pulse duration [\$] | durability | Irradia- nce [W/cm ²] |
|-----------------|----|----------------|---------------------------|------------|-------------------|---------------------|--------------|---------------------------|--------------------------|---|
| real lasers | cw | Laser- Star | DUV LS266 xxxS | 266 | 0,8 | - | 1,00E-01 | - | 3000 h | 1,99E-03 |
| | | Klasstec h | VERVE | 266 | 1,0 | - | 1,00E-01 | - | 12 months guaranteed | 1,27E-03 |
| | | Coherent | MDB266 | 266 | 1 | - | 2,00E-01 | - | ? | 2,55E-03 |
| | | Coherent | Azure TM CW 266 | 266 | 1,05 | - | 2,30E-01 | - | > 6250 h | 2,66E-03 |
| | | Coherent | Genesis CX 355 | 355 | 1,0 | - | 1,00E-01 | - | ? | 1,27E-03 |
| | | CryLas | DL 375-100/200 | 375 | 1,0 | - | 2,00E-01 | - | ? | 2,55E-03 |
| quasi lasers | cq | Teem Phot. | PNU-M1510 | 266 | 1 | ? | 1,7E-02 | 3,50E-10 | ? | 2,17E-04 |
| | | CryLas | FQCW 266-100 | 266 | 0,55 | ? | 1,00E-01 | ? | ? | 4,21E-03 |
| | | EKSPL A | NL20# | 266 | 0,7 | 7,0E-04 | 1,00E+05 | 7,00E-09 | ? | 2,60E+03 |
| | | Spectra- Ph | Hippo Prime 266-2 DPSS | 266 | 1 | ? | 2,00E+00 | ? | ? | 2,55E-02 |
| | | Coherent | AVIA 266-3 | 266 | 2 | ? | 3,00E+00 | ? | 2 years | 9,55E-03 |
| | | EdgeWa ve | Innoslab BXxxIV | 266 | 3 | 1 | 6,00E+00 | 9,00E-09 | ? | 8,49E-03 |
| | | Spectra- Ph | Hippo 355-5 DPS | 355 | 1 | ? | 5,00E+00 | ? | ? | 6,37E-02 |
| | | Coherent | AVIA 355-5 | 355 | 2 | ? | 5,00E+00 | ? | > 12.000 h | 1,59E-02 |
| | | Coherent | MATRIX 355-1-60 BE | 355 | 2,2 | - | 1,00E+00 | ? | very long | 2,63E-03 |
| | | EKSPL A | NL20# | 355 | 0,7 | 1,50E-03 | 2,15E+05 | 7,00E-09 | ? | 5,59E+03 |
| pulsed laser | | CryLas | FQSS 266-Q DPSS | 266 | 1 | ? | 3,00E+02 | ? | ? | 3,82E+00 |
| | | Quantel | Centurion DPSS | 266 | 2,6 | 2,00E-03 | 2,50E+02 | ? | about 109 pulses | 4,71E-01 |
| | | Spectra- Ph | Explorer 349 DPSS | 349 | 0,18 | ? | 2,40E+04 | ? | ? | 9,44E+03 |
| | | CryLas | FTSS 355 - 300 | 355 | 0,8 | ? | 2,00E+05 | ? | ? | 3,98E+03 |
| | | Quantel | Centurion DPSS | 355 | 2,6 | 6 | 7,50E+05 | ? | > 10 ⁹ pulses | 1,41E+03 |

Table 30: Different lasers and irradiance values form Broicher's LIF report [121]

 $\overline{{}^{30} P_{\text{lowest}} = 10^7 \text{ J}, P_{\text{highest}} = 1/6 \cdot 10^9 \text{ J}}$

³¹ The laser spot was assumed spherical therefore $A = \frac{\pi \cdot d^2}{4} = 0,785 \cdot d^2$

The relevant facts can be summarized in table 31.

| Application | Irradiance values for measuring spots [W/cm ²] |
|--|--|
| LS 55 – measuring chamber | $10^{-5} - 10^{-4}$ |
| Binder + Co lead glass sorting system | $10.10^{-3} - 1.6.10^{-3}$ |
| Lasers for LIF recommended from Broicher | $2,17 \cdot 10^{-3} - 5,59 \cdot 10^{3}$ |
| LIF – labscale system after Gaft et al | $10^9 - 10^{11}$ |

Table 31: Irradiance values for several fluorescence applications

The comparison of different types of light sources shows, that the present LS 55 system has the lowest irradiance and is about one to two orders of magnitude lower than the excitation system in the Binder + Co lead glass sorting systems. The lasers reported form Broicher show a very broad band of irradiance values of about six orders of magnitude. The outstanding highest irradiance values occur for the LIF- labscale system reported from Gaft et al. It should be mentioned that many of the calculated values are based on assumptions. However, this survey shows how wide the irradiation span for actual luminescence excitation systems is.

3 Results and Discussion

3.1 Reflection Spectra and Interpretation

From the vast amount of available samples of the Binder + Co R&D department seven minerals have been chosen for further discussion:

- Bauxite
- Magnesite
- Talc
- Fluorite
- Calcite
- Chalcedony
- Baryt

This sample set represents some minerals and mixtures of minerals, which are of interest in the ongoing research project Minexx Plus. Some of the minerals are fluorescent minerals and will be discussed again in following chapters.

Minerals which are fluorescent under UV-light usually show high absorbance in the UV- region. The UV-light is "converted" to light of higher wavelength, which means lower energy. Therefore, when the reflection spectra of such samples are recorded in the UV, sometimes reflectance values over 100 % are encountered. This does not mean violation of the conservation of energy. It simply means, that the sample shows fluorescence when excited in the UV. In order to get rid of this additional intensity (which is of a different wavelength) a second dispersive element like a prism or a diffraction grid between sample and integrating sphere would be required. With respect to the wavelength dependence of features of spectrometer components, e. g. the quantum efficiency of a photomultiplier tube or the absorption of the reflective coating of the integrating sphere, reflectance values over 100 % can only be encountered if the sample emits photons caused by luminescence.

3.1.1 Bauxite

Bauxite is the most important source of Alumina and used for manufacturing of artificial corundum. It is a mixture of several Alumina- and Iron-Hydroxides: Gibbsite: γ -Al(OH)₃, Boehmite: γ -AlOOH, Diaspore: α -AlOOH, Hematite: Fe₂O₃, Goethite: α -FeO(OH) [122,123]. Gibbsite forms crystals with monoclinic, unit cells. In Gibbsite, edge-sharing Al(OH)₆ octahedra form sheets with only 2/3 of the octahedral sites occupied, creating a sheet consisting of a network of 6-membered rings; the sheets are linked by hydrogen bonds [140]. Boehmite forms crystals with orthorhombicunit cells. In Boehmite Al(O,OH)₆ octahedra share six of their 12 edges to form double sheets; the sheets are linked by hydrogen bonds [141]. Diaspore forms crystals with unit cells of orthorhombicsymmetry. Edge sharing Al(O,OH)₆ octahedra form double chains; the chains are linked by sharing corners of the octahedra, and by strong H-bonding [142]. Hematite crystallizes with trigonal [143] and Goethite like Diaspore with orthorhombic unit cells [142].

The analyzed Bauxite sample is depicted in figure 46.



Figure 46: Bauxite sample

Interpretations of the Bauxite reflection spectrum was made according to literature [156].



Figure 47: Bauxite reflection spectrum

3.1.2 Magnesite

Magnesite has the chemical formula MgCO₃, it crystallizes with trigonal $\overline{3}$ unit cells and forms crystals of rhombohedral habit, the structure is isotypic to the Calcite structure. Magnesite is an important resource for fire resistant coating stones. These coatings are especially used for the reactors of the LD – process and electric furnaces for steel production. Raw Magnesite is sintered to the fireproof sintered magnesia under temperatures of 1500 °C [114, 144].

$$MgCO_3 \xrightarrow{1500 \ ^{\circ}C} MgO + CO_2$$

The analyzed Magnesite sample is depicted in figure 48.



Figure 48: Magnesite sample

In figure 49, the characteristic band for CO_3^{2-} at 2318 nm or 6882 cm⁻¹ can be identified as a combination of 3 Carbonate fundamentals. These fundamentals are listed in the table 32.

Table 32: CO₃²⁻ fundamentals for interpretation of the Carbonate feature in NIR [157]

| Fundamental | $\overline{\lambda} [\mathrm{cm}^{-1}]^{32}$ |
|----------------|---|
| v_1 | 1373 |
| v ₂ | 1069 |
| v ₅ | 1482 |

The combination of the three fundamentals was calculated in equation 34.

 $2 \cdot (v_5 + v_1) + v_2 = 6779 \, cm^{-1}$ Equ. 34

The deviation of about 3 cm⁻¹ is expected and due to the anharmonicity of the vibrations.

³² The wavenumber of fundamentals is given in units of cm⁻¹. The conversion is: $\frac{1}{\lambda[nm]} \cdot 10^7 = \overline{\lambda}[cm^{-1}]$



Figure 49: Magnesite reflection spectrum

3.1.3 Talc

Talc is a sheet silicate mineral, $[SiO_4]$ -tetrahedrons are linked together in an infinite tetrahedron sheet. Each $[SiO_4]$ tetrahedron has 3 bridging oxygen atoms to neighboring tetrahedrons. Talc has the chemical formula Mg₃[(OH)₂/Si₄O₁₀]. Ions like OH⁻, F⁻, K⁺, Na⁺, Ca²⁺, etc. can be intercalated between the sheets [139]. Talc is trioctahedral, with three divalent cations occupying occupying all the octahedral sites. These sheets are linked by van der Waals forces [147]. Two different forms of Talc are known: Talc-1A crystallizing in triclinic cells and Talc-2M₁ forming monoclinic unit cells, both of the same chemical formula [145].

Talc forms crystals in the crystal class 2/m, but can also form triclinic or rhombohedral polytopes. Talc has technological value because of its hydrophobic properties and good ability to absorb organic compounds. Powdered talc is known as talcum powder and used in glass-, paper- and dye industry, as lubricant, binder for drugs and cosmetics and extender for plastic [146]. The analyzed talc sample is depicted in figure 50.



Figure 50: Talc sample

The talc reflection spectrum shows several very sharp peaks around 1300 nm, which are presumable combinations and overtones of the OH-group. These sharp features indicate that that the OH-groups sit at very defined places in the crystal structure, probably in the surrounding of metal-cations. Talc shows several features which were just encountered in the bauxite spectrum. The complex structure over 1800 nm supposedly consists of OH and Si-O overtones and is hard to interpret. The presence of the broad feature around 900 nm is an indication of Fe³⁺ in the mineral. The presence of Fe³⁺ is also supported by a strong vibrational overtone at around 1400 nm.



Figure 51: Talc reflection spectrum

3.1.4 Fluorite

Fluorite has the chemical formula CaF_2 and crystallizes with cubic $\overline{3}$ unit cells. It forms a framework of edge-sharing MF₈ cubes. This structure is known as the CaF₂-type [147]. Fluorite occurs in nearly all colors like green, violet, yellow, colorless or black-violet. The color is caused by trace elements, disturbances in the crystal structure, or radioactive irradiation. Many Fluorite show fluorescence under UV-light because they carry rare earth elements instead of Ca²⁺ions. Dark fluorites bear colloidal elemental Ca, which is reduced Ca²⁺, reduced by nuclear radiation. This metallic Ca works as a dark pigment in the usually colorless host. Fluorite is of technological value as flux melting agent in metallurgy, a raw material for the synthesis of hydrofluoric acid and fluorine containing chemicals. Very pure synthetic Fluorite can be used for optical instruments e.g. as lens. It shows high transmittances in the UV-region [148]. The analyzed fluorite sample is depicted in figure 52.



Figure 52: Fluorite sample

The fluorite reflection spectrum shows broad OH-features in the NIR region at around 1400 and 1900 nm. This indicates that the OH are not so defined in the crystal structure. Maybe these bands come from adsorbed or included water in the mineral.

The features at around 550 and 600 come from Eu^{2+} and were reported in the literature. The whole region around 200 – 700 nm can be affected by Eu^{2+} or color centers which are built in presence of Eu^{2+} [158]. The sharp features under and around 400 nm can also origin from intercalated transition metal ions.



Figure 53: Fluorite reflection spectrum

3.1.5 Calcite

Calcite shows the chemical composition CaF_2 , it forms crystals with trigonal unit cells $\overline{3}$ and is therefore structurally equivalent to Magnesite. Sheets of planar CO₃ groups and sheets of corner sharing Caoctahedra are formed. Each O of a CO₃-group connects a Ca atom of the underlying sheet to a Ca atom of the overlying sheet, forming a 3-dimensional framework. This structure is known as the Calcite-structure [149]. Different calcites in varying habit are known. Calcite is easily soluble in cold diluted acids under gas formation (CO₂). Calcite is an important material for the building industry as building stones and decoration stone. Calcites of high quality are known as commercial marble. Furthermore it is a raw material for lime mortar, Portland cement and as a flux material in metallurgical industry. Calcite finds also application as a white pigment in paper [150]. The examined calcite sample is depicted in figure 54.



Figure 54: Calcite sample

The calcite reflection spectrum shows typical features for OH-combinations and overtones around 1400 and 1900 nm, but also the typical $CO_3^{2^-}$ feature around 2300 nm encountered in the Magnesite reflection spectrum. The band around 1100 nm can indicate Fe^{2^+} and was reported in the literature [159]. The small features around 500 nm and 360 nm indicate small amounts of Mn^{2^+} , this feature was reported by several authors. [160, 161, 162]. However, slight differences from the reported wavelength values in the literature can occur, due to the differences in crystal field.



Figure 55: Calcite reflection spectrum

3.1.6 Chalcedony

Chalcedony is cryptocrystalline quartz and has the chemical formula SiO₂. Cryptocrystalline means, that the crystals, which build up the mineral are very small and only visible under the microscope. 6 Modifications of modifications of Quartz with unit cells of different point groups are known. Several minerals are build up by Quartz: rock crystal, amethyst, citrine, ametrine, tiger-eye, chalcedony, agate, carnelian, chrysoprase, heliotrope, onyx, flint (firestone), chert, jasper, etc. Which form of quartz is build up is determined by the temperature T. Temperature range and point group of the unit cell of the 6 forms of quartz are as follows [151]:

- Quartz/ T < 573 °C/ Trigonal
- β -Quartz/ T > 573 °C/ Hexagonal
- Tridymite/ T: 180 350 °C/ Orthorhombic
- β-Tridymite/ T: 465 1470 °C/ Hexagonal
- Cristobalite/ T < 268 °C/ Tetragonal
- β-Cristobalite/ 1470 1728 °C/ Cubic

Chalcedony is a collective term for all micro- and cryptocrystalline parallel-fibrous structured Quartz-varieties. Because of submicroscopic pores and H₂O-contents of 0,5 - 2 % the density is relative low with 2,59 - 2,61 g/cm³. Chalcedony is often of bluish color and has shell-shaped break planes [152]. The analyzed sample of chalcedony is depicted in figure 56.



Figure 56: Chalcedony sample

The reflection spectrum of chalcedony shows the typical OH bands around 1400 and 1900. The bands at 988 nm, 1182 nm and 1213 nm are of unknown origin. These unknown bands can indicate a transition element or be unknown features of the UO_2 present in the sample. The slight band around 698 nm comes from a trace amount of UO_2 and was reported in the literature [163].



Figure 57: Chalcedony reflection spectrum

3.1.7 Barite

Barite hast the chemical formula BaSO₄, and forms Orthorhombic unit cells. Ba is in a mirror symmetric coordination and shares three edges and four corners with SO₄-tetrahedra; six short Ba-O bond lengths and strong binding forces in sheets are responsible for the perfect cleavage of BaSO₄. Other minerals in the Barite (often referred as "Baryte") group like Celestine, Anglesite, Olsacherite and Kerstenite are isostructural [153].

Barite is an important raw material for white dyes. Barite is also used as radiation protection in X-Ray technology and nuclear power plants. It is a component of heavy concrete and used for the preparation of Barium bearing chemicals in chemical industry [168].

The examined barite sample is depicted in figure 58.



Figure 58: Barite sample

The reflection spectrum of barite does not show any significant features except the known OH-peaks at around 1400 nm and 1900 nm. $BaSO_4$ was an alternative to Teflon as a white standard and therefore used

for coatings of integrating spheres or reflection reference material. The OH-peaks indicate adsorbed or included H_2O in the sample.



Figure 59: Baryt reflection spectrum

3.1.8 Discrimination of minerals via the reflection spectrum

An easy to use method to distinguish different minerals is the simple comparison of their UV-VIS-NIR reflection spectra.



Figure 60: Reflection spectra of 7 minerals

If no evident discriminating spectral feature can be found in the spectra, comparison of the first or second derivation can be useful. The plots for the first and second derivative of the reflection data are presented in the figures 61 and 62. The UV-VIS region is plotted separately in figures 63, 64 and 65 while the NIR data are shown in detail in the plots 66, 67 and 68.



Figure 61: Reflection Spectra of 7 Minerals – 1 st derivative



Figure 62: Reflection Spectra of 7 Minerals – 2 nd derivative



Figure 63: UV-VIS – reflection spectra of 7 minerals – raw data



Figure 64: UV-VIS reflection spectra of 7 minerals



Figure 65: UV-VIS reflection spectra of 7 minerals – 2 nd derivative



Figure 66: NIR reflection spectra of 7 minerals – raw data



Figure 67: NIR reflection spectra of 7 minerals – 1 st derivative



Figure 68: NIR reflection spectra of 7 minerals – 2 nd derivative
3.2 Fluorescence Measurements

3.2.1 Parameter Dependence of Intensities

The measurement of absolute fluorescence intensities is a rather difficult task. Several attempts are described in the literature to determine absolute quantum yield, but none of them is easy to apply [69]. One commercially available system for determination of absolute quantum yields is the Hamamatsu Quantaurus system [70]. However, such a system was not available at the time of the project and it seemed appropriate to work with relative intensities.

Clearly, the measured luminescence intensity of samples excited with a suitable wavelength depends on a number of instrumental settings – in particular on the gain of the photomultiplier and on the emission slit width. Samples showing only weak luminescence require either more gain on the detector or a larger emission slit width in order to be recorded properly. Hence a major problem arises, when relative intensities are to be compared.

To assess the intensity dependence of emission slit width while all other instrument parameters are kept constant an emission experiment with fluorite was performed. The instrument settings are given in table 33.

| Scan type | Emission |
|------------------------------|--------------|
| Scan range [nm] | 400 - 900 |
| Ex. Wl [nm] | 355 |
| Scan Speed [nm/min] | 1200 |
| Gain Voltage [V] | 775 |
| Measurement mode | Fluorescence |
| Excitation Correction | on |
| Delay [ms] | - |
| Gate [ms] | - |
| Cycle [ms] | - |
| Flash count | - |
| Excitation Slit [nm] | 10 |
| Emission Slit [nm] | Х |
| Emission cut off filter [nm] | 390 |

Table 33: Instrument settings for the measurement of intensity vs. emission slit width

The sample was excited at 355 nm. The characteristic emission peak of fluorite can be found with a maximum at 428 nm. The emission spectra for the four possible emission slit settings are depicted in figure 69. Greater slit widths led to signal overflow. As a measure of the fluorescence intensity the peak height was taken. A fit of the relation between slit width and intensity is given in figure 70.



Figure 69: Emission spectra for fluorite at different emission slit settings (in nm)

| Table 34: Emission slit width and measured | peak | heights fo | or fluorite |
|--|------|------------|-------------|
|--|------|------------|-------------|

| Em. Slit width [nm] | Peak |
|---------------------|--------|
| | height |
| 3 | 65,0 |
| 4 | 253,8 |
| 5 | 539,0 |
| 6 | 882,0 |



Figure 70: Observed and fitted peak height vs. emission slit width relation

From the best fit to the experimental data points (see figure 70), an empirical equation for the emission slit width dependence of the measured intensity can be obtained:

$$I(sw) = 38,55 sw^2 - 73,33 sw - 63,89$$
 Equ. 35

In equation 35 I(sw) is the intensity and sw the slit width in nm.

For the relative intensity scale the PbO-reference glass no. 1 is set at 100 % because it shows the brightest glow under UV light and furthermore is one of the specimens which can already be sorted with the machines of Binder + Co. The relative intensity of any sample can be calculated according to equations 36 and 37:

$$I_{rel.} = \frac{I_{max}(Pb0, no.1)}{I_{max}(sample)} \cdot C \qquad Equ. 36$$

$$C = \frac{(38,55 \, sw(Pb0,no.1)^2 - 73,33 \, sw(Pb0,no.1) - 63,89)}{(38,55 \, sw(sample)^2 - 73,33 \, sw(sample) - 63,89)} Equ. 37$$

The scale of relative intensities for several minerals is evaluated for the fluorescing samples, which are described in more detail in the next chapters. In fact, when the phosphorescence mode is applied, a considerable bias value for measured intensity can be found. For measurements marked with "phosphorescence" the bias value was subtracted from the maximum intensity.

The results for the calculation of the relative intensities according to equations 36 and 37 are denoted in table 35.

| Sample | Rel. Int(calc.) [%] | Excitation WL [nm] | Emission slit width | WL of most intense peak [nm] | Height of most intense peak | Mesurement mode |
|--------------------------|-------------------------|-----------------------|------------------------|---------------------------------|-----------------------------------|-----------------|
| Fluorite | 7,17 | 366 | 6 | 427 | 714,4 | fluorescence |
| Calcite | 0,31 | 254 | 20 | 619 | 81,3 | phosphorescence |
| Magnesite | 0,41 | 254 | 20 | 478 | 42,5 | phosphorescence |
| Chalcedony | 2,84 | 254 | 8 | 525 | 250 | phosphorescence |
| CAB 15 | 31,02 | 266 | 4 | 336 | 367,5 | fluorescence |
| PbO-reference glass 1 | 100,00 | 254 | 3 | 429 | 271,3 | fluorescence |
| Si sample | 0,00 | 254 | 20 | 0 | 0 | phosphorescence |

Table 35: Results for relative intensities for several glass and mineral samples



Figure 71: Relative fluorescence intensity scale with some examples



Figure 72: Samples for the comparison of luminescence intensities under 254 nm excitation: a) Calcite, b) Chalcedony, c) Magnesite, d) Fluorite, e) PbO reference glass 1, f) CAB 15, g) Silicon

The proposed scale of relative intensities (see figure 71) is just a very simple approach to get an idea of the order of magnitude of differences in fluorescence intensity. It is an easy to use tool for every day testing practice in the lab. However, the scale is only valid, when only the emission slit width is different in the measurement and the method described in table 33 is applied. PbO ref. glass – 1 and 2, Fluorite and a Scheelite sample were sent to Hamammatsu Germany to analyze absolute quantum yields at their Quantaurus system. The result from this analysis is presented in table 36.

| Quantum Yield Da | Quantum Yield Data with Quantaurus system | | | | |
|---------------------------|---|------|--|--|--|
| Sample Em. WL [nm] QY [%] | | | | | |
| PbO ref glass - 1 | 280 | 16,6 | | | |
| PbO ref glass - 2 | 280 | 21,1 | | | |
| Fluorite sample | 300 | 1,4 | | | |
| Scheelite Mittersill | 250 | 8,7 | | | |

Table 36: Quantum Yield data for several samples from Quantaurus measurements

3.2.2 Emission Correction Functions

Fluorescence emission spectra have to be corrected in two ways: a) the excitation correction and b) the emission correction. Excitation correction is realized via a fluorescence cell with a known fluorophor (e.g. Rhodamin B) and a detector in the excitation channel. Excitation correction compensates time dependent alterations of the light source of the spectrofluorometer. The emission correction compensates the wavelength dependent bias of the emission channel. This bias comes from the quantum efficiency of the photomultiplier tube and the wavelength dependent characteristics of the optical parts in the emission channel [71].

One possibility for emission correction is the recording of emission spectra of the certified reference dyes provided from Federal Institute for Materials Research and Testing (BAM).

The measured spectra are compared to the known certified spectra of the dyes. The samples were prepared according to the SOP (Standard Operation Procedure) provided with the standard kit from Fluka. The kit is used for the determination of the spectral responsivity $s(\lambda)$ of the instrument. The inverse spectral responsivity $1/s(\lambda)$ is termed as emission correction curve [72].

The experiments were carried out according to the SOP [72]. The experimental procedure is the depicted in figure 73.



Figure 73: Overview of the experimental procedure according to BAM [72]

Two different instrument settings were chosen. The BAM certificate provides reference spectra for emission bandwidth of 1 nm, 4 nm and 8 nm. The one nm emission bandwidth cannot be set in the LS 55 (range of emission bandwidth is 2,5 - 20 nm). The settings are described in table 37.

| Parameter/Setting | a) | b) |
|---------------------------|-----|-----|
| excitation bandwidth [nm] | 4 | 2,5 |
| emission bandwidth [nm] | 4 | 8 |
| PMT-voltage [V] | 775 | 690 |
| scan speed [nm/min] | 100 | 100 |

Table 37: Instrument settings for calibration measurement of LS 55

For every measurement an emission cut-off filter was chosen to avoid second order radiation interference from the excitation source. Table 38 lists the used cut off filters for the measurements.

| Standards | Excitation WL [nm] | Emission cut off WL [nm] |
|-----------|--------------------|--------------------------|
| BAM-F001 | 280 | 290 |
| BAM-F002 | 315 | 350 |
| BAM-F003 | 380 | 390 |
| BAM-F004 | 420 | 430 |
| BAM-F005 | 550 | - |

It was noticed that the noise in the lower excitation wavelength region was less when the cuvette was twisted for a few degrees. For the higher excitation wavelengths the noise disappeared. But all experiments have been carried out with twisted cuvettes for the measurement geometry has to be kept the same all the time.

Figure 74 gives a comparison of technical³³ spectra of BAM-F001 first in a non-twisted and then in a twisted cuvette, recorded under the measurement settings b).

³³ technical spectra means that for the spectrum no emission correction was carried out



Figure 74: BAM-F001 twisted and non-twisted emission spectra

The experimental setup with the twisted cuvette is depicted in figure 75.



Figure 75: : a) zero degree position – top view; b) zero degree position – side view; c) twisted position – top view; d) twisted position – side view

The twisting angle of the cuvette is approximately 15°. Every emission measurement for the standard and the blank solution was repeated 5 times. The spectral grade ethanol provided with the test kit was used for the blank measurements.



Figure 76: BAM standards under UV lamp NU-4 KL

The data were processed with the software provided with the standard test kit. The mean value of 5 measurements for the standards solutions and the blank were averaged³⁴. For the following plot the mean of the blank was subtracted from the mean of the standards. The technical averaged spectra for both settings are depicted in the figures 77 and 78.

For proper data processing of the data files all commas "," have to be replaced with points ".". Unfortunately the LinkCorr-Software is not compatible with Windows 7 64 bit-versions. Furthermore the original CD has to be in the CD-drive for proper functioning of the program. Data evaluation has been done on a WinXP(SP2)-PC.

As a result from the LinkCorr-Calculation the relative spectral responsivity $1/s(\lambda)$ was obtained. This factor is used to standardize a technical emission spectrum via multiplication [72].

³⁴ arithmetic mean



Figure 77: Technical emission spectra for the BAM standards in setting a)



Figure 78: Technical emission spectra for the BAM standards in setting b)

The observed intensity is sensitive to changes in emission or excitation bandwidth. Therefore normalization of the correction function is required for applicability of the correction function to different instrument settings. The reciprocal of $1/s(\lambda)$ was calculated to get $s(\lambda)$. This value was then normalized to the highest value in the series to obtain $s_{norm}(\lambda)$. Now the new correction spectrum can be used to correct spectra of different spectral bandwidth for correction via simple division.

The correction data are presented in the figure 79 in comparison with the old correction function EMRED.corr from Perkin Elmer.



Figure 79: Comparison of available detection functions from the calibration experiment

The comparison of the Perkin Elmer spectrum EMRED.cor with the data from the measurements shows that there are several deviations (see figure 79). Therefore the calibration measurements of the certified BAM standards were an important step in the ongoing research project.

The $s_{norm}(\lambda)$ -values for the two different settings are nearly equal. Thus the change of the spectral band width between 4 - 8 nm can be seen as not critical.

Unfortunately the data evaluation of the measurements of the BAM-standard kit yielded a correction spectrum which only ranges to 730 nm.

For corrections from 730 to 900 nm the measurement of a calibrated light source could be useful. Correction procedures with standard lamps are described in the literature [73].

The breaking down to zero of the $s_{norm}(\lambda)$ -function between 300 – 310 nm can be considered as a result of an oscillation of the data evaluation algorithm. Obviously the signal to noise ratio for the measurements of the BAM-F001 was not good enough.

For correction of measurements below 310 nm further calibrations with standard lamps seem to be indicated. Since the resources for such calibration experiments were not available at the time of the work and the values for Corrfun a) and Corrfun b) do not differ too much, the values for Corrfun a) were simply extrapolated between 200 - 300 nm and 720 - 900 nm with a straight line. The result for this correction is depicted in figure 80.



Figure 80: Resulting correction function of calibration experiments

The values for this correction function are tabulated in the Appendix.

3.2.3 Spectra of Minerals and Glasses with Interpretation

Six fluorescing and one not fluorescing samples have been chosen to demonstrate the possibilities for the measurements of luminescence spectra on the LS 55:

- Fluorite (blue fluorescence)
- Calcite (red fluorescence)
- Magnesite (pale blue fluorescence)
- Chalcedony (green fluorescence)
- CAB 15 (blue fluorescence)
- PbO-reference glass no. 1
- Si sample

The Fluorite, Calcite, Magnesite and Chalcedony samples were taken from the same deposit in Turkey. Optical sorting of these samples was a research topic of the R&D department of Binder + Co at the time of the project.

CAB 15³⁵ was one of the most intense fluorescing glasses of Kieler's sample set, prepared in 2009 during her diploma thesis [2]. It contains about 1,47 w% of PbO [2]. It was found, that industrial PbO-containing glasses normally show more intense fluorescence than the CAB-glasses. This can be explained with the different composition and preparation conditions of the glasses. Usually the preparation temperature for industrial glasses is much higher than for the CAB glasses. CAB glasses were chosen as a test system because of the relative ease of preparation and because they still show the typical lead emission band [68].

PbO-reference glass no. 1 was cut out of a commercially available drinking glass of lead crystal. The PbO content of about 24,80 w% of PbO-reference glass no. 1 was determined with XRF (Thermo Scientific; Niton XL3t, see figure 81).



Figure 81: XRF analyzer calibrated with lead crystal of known PbO-content

³⁵ CAB stands for Calcium Aluminum Borate

The Si sample was high-purity silicon from a manufacturer of the semiconductor industry. It was considered that it should not show any fluorescence signal because of high purity. Therefore it was used as a blank sample.

An overview of the samples under white light and under UV-light is presented in figure 82.



Figure 82: Samples for the recording of luminescence spectra a) under white light b) under 15W excitation with light of 254 nm at a distance of about 10 cm: 1) Calcite, 2) Chalcedony, 3) Magnesite, 4) Fluorite, 5) PbO reference glass 1, 6) CAB 15, 7) Silicon

To avoid overflow of the detection system, the emission slit was adjusted in a way that the maximum peak was as large as possible without generation of overflow. The relative intensity scale of the detection system ranges from 0 to 1000. Intensities over 1000 are not in the linear range of the detection system.

It should be mentioned that in the following sections only data without second order artifacts of the emission grating of the LS 55 are presented. An example is presented in figure 83. Second-order transmission artifacts are a device characteristic of fluorimeters with a grating as dispersive element.

The interference maxima of a diffraction grating can be described via the following equation:

$$g \cdot sin\theta = m \cdot \lambda$$
 Equ. 38
m = 0, 1, 2,...

In equation 38 g is the grating constant that describes the distance between the grating lines, θ is the angle between interference maxima, m the reflection order and λ the wavelength [124].



Figure 83: Emission spectrum for Fluorit at excitation wavelength of 254 nm a) with second order artifacts, b) without second order artifacts

For the fluorescence emission measurements at an excitation wavelength of 266 nm an additional cut offfilter was brought into the emission channel of the fluorimeter. The filter WG 320 should cut off the excitation light, which passed the implemented 290 nm cut-off filter. The cut off edge of WG 320 starts at 300 nm and ends at a transmission of 80 % at 330 nm. The transmission spectrum of WG 320 is shown in figure 84.



Figure 84: Transmission curve of WG 320

As depicted in figure 83 the excitation light of the source can be found as second order artifact in the spectrum. E.g. the 266 nm excitation wavelength can be found as a huge peak at 532 nm (see figure 85).



Figure 85: Fluorescence Emission Spectrum of Magnesite with and without a cut off filter

3.2.3.1 Fluorite – Luminescence Spectra

The fluorite fluorescence emission spectrum is in good accordance with the reported spectrum in literature. The peak around 420 nm is related to Eu^{2+} , the two peaks between 300 – 400 nm are of unknown origin. An emission of Gd^{3+} in Fluorite around 310 nm is reported [164].



Figure 86: Fluorite fluorescence emission spectra

| | Fluorite 2D - Fluorescence Mode | | | | |
|---------------------|---------------------------------|---------------|---------------|---------------|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | |
| Emslit [nm] | 8 | 8 | 6 | 4 | |
| Exslit [nm] | 10 | 10 | 10 | 10 | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | |
| Delay [ms] | - | - | - | - | |
| Gate [ms] | - | - | - | - | |
| Cycle time [ms] | - | - | - | - | |
| Flash count | - | - | - | - | |
| Additional Emfilter | - | WG 320 | - | - | |

Table 39: Method parameters for Fluorite fluorescence emission spectra



Figure 87: Fluorite phosphorescence emission spectra

| | Fluorite 2D - Phosphorescence Mode | | | | |
|---------------------|------------------------------------|---------------|---------------|---------------|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | |
| Emslit [nm] | 8 | 8 | 8 | 8 | |
| Exslit [nm] | 10 | 10 | 10 | 10 | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | |
| Delay [ms] | 0,10 | 0,10 | 0,10 | 0,10 | |
| Gate [ms] | 3,00 | 3,00 | 3,00 | 3,00 | |
| Cycle time [ms] | 20 | 20 | 20 | 20 | |
| Flash count | 1 | 1 | 1 | 1 | |
| Additional Emfilter | - | - | - | - | |

Table 40: Method parameters for Fluorite phosphorescence emission spectra



Figure 88: Fluorite fluorescence 3D spectra



Figure 89: Fluorite phosphorescence 3D spectra

3.2.3.2 Calcite – Luminescence Spectra

The calcite phosphorescence emission spectrum shows an emission feature at 620 nm which is linked to Mn^{2+} [165]. The fluorescence spectra do not show any useful results.



Figure 90: Calcite fluorescence emission spectra

| | Calcite 2D - Fluorescence Mode | | | | |
|---------------------|--------------------------------|---------------|---------------|---------------|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | |
| Emslit [nm] | 8 | 8 | 8 | 8 | |
| Exslit [nm] | 10 | 10 | 10 | 10 | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | |
| Delay [ms] | - | - | - | - | |
| Gate [ms] | - | - | - | - | |
| Cycle time [ms] | - | - | - | - | |
| Flash count | - | - | - | - | |
| Additional Emfilter | - | WG 320 | - | - | |

Table 41: Method parameters for the Calcite fluorescence emission spectra

The fluorescence data of Calcite are not plausible in comparison to the image of the mineral under UV-light.



Figure 91: Calcite phosphorescence emission spectrum

| | Calcite 2D - Phosphorescscence Mode | | | | |
|---------------------|-------------------------------------|---------------|---------------|---------------|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | |
| Emslit [nm] | 20 | 20 | 20 | 20 | |
| Exslit [nm] | 10 | 10 | 10 | 10 | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | |
| Delay [ms] | 0,10 | 0,10 | 0,10 | 0,10 | |
| Gate [ms] | 3,00 | 3,00 | 3,00 | 3,00 | |
| Cycle time [ms] | 20 | 20 | 20 | 20 | |
| Flash count | 1 | 1 | 1 | 1 | |
| Additional Emfilter | - | - | - | - | |

Table 42: Method parameters for the Calcite phosphorescence emission spectra

It should be mentioned, that the red emission of the Calcite sample could only be measured properly, when the emission slit was opened at its maximum.



Figure 92: Calcite fluorescence 3D data



Figure 93: Calcite phosphorescence 3D spectra

3.2.3.3 Magnesite – Luminescence Spectra

The Magnesite phosphorescence spectra show a bluish emission peak around 450 nm, which is not clearly defined in the literature [166]. The Magnesite fluorescence spectrum is plausible concerning the maximum in the blue region, but resembles the emission spectrum of Calcite, Chalcedony and even the Si-sample.



Figure 94: Magnesite fluorescence emission spectra

| | Magnesite 2D - Fluorescence Mode | | | | | | |
|---------------------|----------------------------------|---------------|---------------|---------------|--|--|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | | | |
| Emslit [nm] | 8 | 8 | 8 | 8 | | | |
| Exslit [nm] | 10 | 10 | 10 | 10 | | | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | | | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | | | |
| Delay [ms] | - | - | - | - | | | |
| Gate [ms] | - | - | - | - | | | |
| Cycle time [ms] | - | - | - | - | | | |
| Flash count | - | - | - | - | | | |
| Additional Emfilter | - | WG 320 | - | - | | | |

Table 43: Method parameters for the Magnesite fluorescence emission spectra



Figure 95: Magnesite phosphorescence emission spectra

| | Magnesite 2D - Phosphorescscence Mode | | | | | |
|---------------------|---------------------------------------|---------------|---------------|---------------|--|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | | |
| Emslit [nm] | 20 | 20 | 20 | 20 | | |
| Exslit [nm] | 10 | 10 | 10 | 10 | | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | | |
| Delay [ms] | 0,10 | 0,10 | 0,10 | 0,10 | | |
| Gate [ms] | 3,00 | 3,00 | 3,00 | 3,00 | | |
| Cycle time [ms] | 20 | 20 | 20 | 20 | | |
| Flash count | 1 | 1 | 1 | 1 | | |
| Additional Emfilter | - | - | - | - | | |

Table 44: Method parameters for the Magnesite phosphorescence emission spectra



Figure 96: Magnesite fluorescence 3D spectra



Figure 97: Magnesite phosphorescence 3D spectra

3.2.3.4 Chalcedony – Luminescence Spectra

The phosphorescence spectrum of Chalcedony shows the characteristic triple peak of $(UO_2)^{2+}$ at 502 nm, 521 nm and 544 nm, reported in the literature [167]. The fluorescence spectra are similar to Calcite, Fluorite, Silicon and Magnesite.



Figure 98: Chalcedony fluorescence emission spectra

| Table 45: Method | · · · | | ~ 1 1 1 | a | • • |
|--------------------|---------------|--------|-------------|--------------|---------------------------------------|
| Table As Method | navamotove to | nr tha | I halcodowy | thunkageoueo | omicción choctra |
| I UUUC TJ. MICINUU | Durumeters n | | Chuiceuonv | nuorescence | |
| | r | | | J | · · · · · · · · · · · · · · · · · · · |

| | Chalcedony 2D - Fluorescence Mode | | | | | |
|---------------------|-----------------------------------|---------------|---------------|---------------|--|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | | |
| Emslit [nm] | 8 | 8 | 8 | 8 | | |
| Exslit [nm] | 10 | 10 | 10 | 10 | | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | | |
| Delay [ms] | - | - | - | - | | |
| Gate [ms] | - | - | - | - | | |
| Cycle time [ms] | - | - | - | - | | |
| Flash count | - | - | - | - | | |
| Additional Emfilter | - | WG 320 | - | - | | |



Figure 99: Chalcedony phosphorescence emission spectra

| | Chalcedony 2D - Phosphorescence Mode | | | | | |
|---------------------|--------------------------------------|---------------|---------------|---------------|--|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | | |
| Emslit [nm] | 8 | 8 | 20 | 20 | | |
| Exslit [nm] | 10 | 10 | 10 | 10 | | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | | |
| Delay [ms] | 0,10 | 0,10 | 0,10 | 0,10 | | |
| Gate [ms] | 3,00 | 3,00 | 3,00 | 3,00 | | |
| Cycle time [ms] | 20 | 20 | 20 | 20 | | |
| Flash count | 1 | 1 | 1 | 1 | | |
| Additional Emfilter | - | - | - | - | | |

| Table 16. Mathad | navamatava | for the | Chaladam | nhaa | nhavasaanaa | amissian | spaatua |
|------------------|------------|---------|------------|--------|-------------|----------|---------|
| Table 46: Method | purumeters | jor ine | Charceaony | ' pnos | phorescence | emission | spectra |



Figure 100: Chalcedony phosphorescence 3D spectra



Figure 101: Chalcedony phosphorescence 3D spectra

3.2.3.5 Silicon – Luminescence Spectra

Silicon was used as a blank for fluorescence and phosphorescence measurement. Since the fluorescence measurement (see fig. 102) shows very intensive peaks, which are not plausible if the Si sample is seen under UV light, the fluorescence mode of the LS 55 has to be considered as not reliable for non- or very weak fluorescing minerals. Very similar fluorescence spectra were obtained with Chalcedony, Magnesite and Calcite. However, a nearly straight baseline, as expected for Si was observed in the phosphorescence mode.



Figure 102: Si sample fluorescence emission spectra

| Table 47: Method parameters for the Si sample fluorescence emission spectra |
|---|
| |

| | Si sample 2D - Fluorescence Mode | | | | | | |
|---------------------|----------------------------------|---------------|---------------|---------------|--|--|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | | | |
| Emslit [nm] | 8 | 8 | 8 | 8 | | | |
| Exslit [nm] | 10 | 10 | 10 | 10 | | | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | | | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | | | |
| Delay [ms] | - | - | - | - | | | |
| Gate [ms] | - | - | - | - | | | |
| Cycle time [ms] | - | - | - | - | | | |
| Flash count | - | - | - | - | | | |
| Additional Emfilter | - | WG 320 | - | - | | | |



Figure 103: Si sample phosphorescence emission spectra

| | Si sample 2D - Phosphorescence Mode | | | | | | |
|---------------------|-------------------------------------|---------------|---------------|---------------|--|--|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | | | |
| Emslit [nm] | 20 | 20 | 20 | 20 | | | |
| Exslit [nm] | 10 | 10 | 10 | 10 | | | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | | | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | | | |
| Delay [ms] | 0,10 | 0,10 | 0,10 | 0,10 | | | |
| Gate [ms] | 3,00 | 3,00 | 3,00 | 3,00 | | | |
| Cycle time [ms] | 20 | 20 | 20 | 20 | | | |
| Flash count | 1 | 1 | 1 | 1 | | | |
| Additional Emfilter | - | - | - | - | | | |

| Table 48: Method | narameters | for the | Si samnle | nhasnharøsconco | emission snectra |
|------------------|------------|-----------|-----------|-----------------|------------------|
| Tuble 40. Mellou | purumeters | joi ine s | si sumpie | phosphorescence | emission speciru |



Figure 104: Si sample fluorescence 3 D spectra



Figure 105: Si sample phosphorescence 3D spectra
3.2.3.6 CAB 15 – Luminescence Spectra

The CAB 15 sample showed an intense peak around 350 nm in the fluorescence spectrum. This peak is assigned to the $s^2 \rightarrow sp$ transition, which was reported from Kieler in her master thesis [2]. The phosphorescence spectra show a baseline, which indicates fast decay of the PbO-acitivator.



Figure 106: CAB 15 fluorescence emission spectra

| | CAB 15 2D - Fluorescence Mode | | | | | | |
|---------------------|-------------------------------|---------------|---------------|---------------|--|--|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | | | |
| Emslit [nm] | 4 | 4 | 8 | 8 | | | |
| Exslit [nm] | 10 | 10 | 10 | 10 | | | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | | | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | | | |
| Delay [ms] | - | - | - | - | | | |
| Gate [ms] | - | - | - | - | | | |
| Cycle time [ms] | - | - | - | - | | | |
| Flash count | - | - | - | - | | | |
| Additional Emfilter | - | - | - | - | | | |

Table 49: Method parameters for the CAB 15 fluorescence emission spectra



Figure 107: CAB 15 phosphorescence emission spectra

| | | CAB 15 2D - Phosphorescence Mode | | | | | | |
|---------------------|---------------|----------------------------------|---------------|---------------|--|--|--|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | | | | |
| Emslit [nm] | 20 | 20 | 20 | 20 | | | | |
| Exslit [nm] | 10 | 10 | 10 | 10 | | | | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | | | | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | | | | |
| Delay [ms] | 0,10 | 0,10 | 0,10 | 0,10 | | | | |
| Gate [ms] | 3,00 | 3,00 | 3,00 | 3,00 | | | | |
| Cycle time [ms] | 20 | 20 | 20 | 20 | | | | |
| Flash count | 1 | 1 | 1 | 1 | | | | |
| Additional Emfilter | - | - | - | - | | | | |

| Table 50: Method | parameters | for the CAB | 15 phos | phorescence | emission s | nectra |
|--------------------|------------|--------------|---------|-------------|-------------|--------|
| I ubic 50. michiou | purumeters | joi inc chib | 15 phos | phorescence | chiission s | pecau |



Figure 108: CAB 15 fluorescence 3D spectra



Figure 109: CAB 15 phosphorescence 3D spectra

3.2.3.7 PbO reference glass 1 – Luminescence Spectra

The Pb reference glass 1 shows much higher fluorescence intensity, than it is observed for CAB 15. This peak is assigned to the $s^2 \rightarrow sp$ transition of Pb²⁺ [2]. Like for CAB 15 no peak can be measured under phosphorescence settings.



Figure 110: Pb-glass 1 fluorescence emission spectrum

| | | Pb-Glas_1 2D - Fluorescence Mode | | | | | | | |
|---------------------|---------------|----------------------------------|---------------|---------------|--|--|--|--|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | | | | | |
| Emslit [nm] | 3 | 4 | 8 | 8 | | | | | |
| Exslit [nm] | 10 | 10 | 10 | 10 | | | | | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | | | | | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | | | | | |
| Delay [ms] | - | - | - | - | | | | | |
| Gate [ms] | - | - | - | - | | | | | |
| Cycle time [ms] | - | - | - | - | | | | | |
| Flash count | - | - | - | - | | | | | |
| Additional Emfilter | - | - | - | - | | | | | |

Table 51: Method parameters for the Pb-glass 1 fluorescence emission spectra



Figure 111: Pb-glass 1 phosphorescence emission spectra

| | | Pb-Glas_1 2D - Phosphorescence Mode | | | | | | |
|---------------------|---------------|-------------------------------------|---------------|---------------|--|--|--|--|
| | Exc. @ 254 nm | Exc. @ 266 nm | Exc. @ 355 nm | Exc. @ 366 nm | | | | |
| Emslit [nm] | 20 | 20 | 20 | 20 | | | | |
| Exslit [nm] | 10 | 10 | 10 | 10 | | | | |
| U(PMT) [V] | 775 | 775 | 775 | 775 | | | | |
| Emfilter [nm] | 290 | 290 | 390 | 390 | | | | |
| Delay [ms] | 0,10 | 0,10 | 0,10 | 0,10 | | | | |
| Gate [ms] | 3,00 | 3,00 | 3,00 | 3,00 | | | | |
| Cycle time [ms] | 20 | 20 | 20 | 20 | | | | |
| Flash count | 1 | 1 | 1 | 1 | | | | |
| Additional Emfilter | - | - | - | - | | | | |

| Table 52: Method | parameters | for the | Pb-glass 1 | 1 phosphorescence |
|------------------|------------|---------|------------|-------------------|
| | | | | |



Figure 112: Pb-glass 1 fluorescence 3D spectra



Figure 113: Pb-glass 1 phosphorescence 3D spectra

3.2.4 Decay curves

The experimental results indicated that the fluorite sample showed no measurable emission at a delay time of 0,10 ms and gate time of 3,00 ms. To investigate the possibilities for decay measurements with the LS 55, the gate time was varied from the smallest possible setting of 0,01 ms to 0,05 ms where no emission could be observed any more. The measured spectra are plotted in figure 114.



Figure 114: Fluorite spectra - raw data for the decay curves

In the phosphorescence mode different values for the y-axis offset were observed. This offset values were subtracted from the maxima at a wavelength of 424 nm.

| Measurement mode | Fluorescence | Phosphorescence | Phosphorescence | Phosphorescence | Phosphorescence |
|-----------------------|--------------|-----------------|-----------------|-----------------|-----------------|
| Delay [ms] | 0 | 0,05 | 0,03 | 0,02 | 0,01 |
| Exc. WL [nm] | 366 | 366 | 366 | 366 | 366 |
| Emslit [nm] | 6 | 6 | 6 | 6 | 6 |
| Exslit [nm] | 10 | 10 | 10 | 10 | 10 |
| U(PMT) [V] | 775 | 775 | 775 | 775 | 775 |
| Emfilter [nm] | 390 | 390 | 390 | 390 | 390 |
| Delay [ms] | - | 0,05 | 0,03 | 0,02 | 0,01 |
| Gate [ms] | - | 3,00 | 3,00 | 3,00 | 3,00 |
| Cycle time [ms] | - | 20 | 20 | 20 | 20 |
| Flash count | - | 1 | 1 | 1 | 1 |
| Additional Emfilter | - | - | - | - | - |
| Peak height. @ 424 nm | 714,73 | 0,97 | 3,37 | 32,15 | 402,43 |

Table 53: Decay experiment – results and method parameters

The results for the peak height at the wavelength of 424 nm in as a function of delay time are presented in figure 115.



Figure 115: Peak height at 424 nm vs. delay time

However, the Eu^{2+} emission at 424 nm has a reported decay time of 600 – 800 ns and should not be observed in the LS 55 system in the phosphorescence mode [125]. It must be mentioned that there is a mismatch between the reported decay times of Eu^{2+} in the literature and the measured decay times. This mismatch is presently unresolved.

4 Conclusion

Preparation for the samples for the optical measurements was achieved by cutting and polishing. The purity of mineral phases can be assessed by tests with the Raman spectroscope of the project partner MUL.

The NIR-reflection measurements of the chosen mineral samples (Bauxite, Magnesite, Talc, Fluorite, Calcite, Chalcedony and Barite) show good discrimination possibilities for those minerals, when the first and second derivatives of the spectra are compared. Data produced with the L950 system are of good quality and can serve as a base for implementation in UV, VIS, NIR reflection or transmission sensor sorting systems. However, the reflection measurements are more time consuming than the measurements with industrial sensor systems. Some bands in the reflection spectra were interpreted according to the literature. Often occurring OH-combinations and overtones at around 1400 nm and 1900 nm can be increased and identified if the samples are wetted with H_2O . An easy to use standard method and analysis procedure for the measurement of reflection spectra was defined.

It was shown that a discrimination via the emission spectrum of a mineral with the LS 55 is possible, if a suitable activator is present in the mineral, e.g. Mn^{2+} in Calcite or Eu^{2+} in Fluorite. The emission features recorded in the spectrofluorimeter allow to set discriminators for sorting purposes. Crucial information can be obtained either in the fluorescence or phosphorescence spectra. It is a major problem of the LS 55 that life time of excited states can lead to problems in detection of the activators. An attempt to assess fluorescence intensity with a straightforward approach was made. While taking the photographs under UV light, it turned out that the use of a 15 W shortwave UV-lamp is highly recommended for good photograph quality with standard digital cameras. For all the examined minerals and glasses (Fluorite, Calcite, Magnesite, Chalcedony, CAB 15 and a PbO reference glass) bands in the emission spectra could be measured. A silicon piece of very high purity was used as a blank standard for fluorescence. In a hypothetical sorting experiment, all the mentioned samples can be distinguished from one another. Due to the life time problem emission measurements are more complex than reflection measurements. However, easy to use methods for emission side of the LS 55 was recorded according to the recommended BAM standards.

The illumination situation in the LS 55 spectrofluorimeter was assessed with radiometric measurements and the use of a chemical actinometer. This illumination situation was compared to the irradiance values for commercial available laser illumination systems. In the LS 55 irradiance values in the range of $10^{-5} - 10^{-4}$ W/cm² could be measured. The glass sorting systems from Binder + Co work with irradiances of $10^{-2} - 10^{-3}$ W/cm². Laser systems recommended for LIF-sorting applications are in the order of $10^{-3} - 10^{-3}$ W/cm². LIF labscale systems work with irradiances of about $10^9 - 10^{-11}$ W/cm².

A database and literature search was carried out. It is important to have reference data to compare spectra of actual samples to find activators and spectroscopically active species in the minerals. The three most important databases available in the internet are: USGS for reflection spectra of minerals, Mindat for general information on Minerals and Fluomin for fluorescence spectra. The literature research on fluorescent minerals showed that there are three books of great importance for the field, the works of: Marfunin [154], Gorobets & Rogojine [155] and Gaft, Reisfeld & Panczer [76].

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6 Appendix



6.1 Emission Correction function for the LS 55 with R955 PMT

| Х | у | Х | у | Х | у | Х | у |
|-------|------------|-------|------------|-------|------------|-------|------------|
| 200,0 | 0,10000001 | 210,5 | 0,10851153 | 220,5 | 0,11661773 | 231 | 0,12512925 |
| 200,5 | 0,10040532 | 211 | 0,10891684 | 221 | 0,11702304 | 231,5 | 0,12553456 |
| 201,0 | 0,10081063 | 211,5 | 0,10932215 | 221,5 | 0,11742835 | 232 | 0,12593987 |
| 201,5 | 0,10121594 | 212 | 0,10972746 | 222 | 0,11783366 | 232,5 | 0,12634518 |
| 202 | 0,10162125 | 212,5 | 0,11013277 | 222,5 | 0,11823897 | 233 | 0,12675049 |
| 202,5 | 0,10202656 | 213 | 0,11053808 | 223 | 0,11864428 | 233,5 | 0,1271558 |
| 203 | 0,10243187 | 213,5 | 0,11094339 | 223,5 | 0,11904959 | 234 | 0,12756111 |
| 203,5 | 0,10283718 | 214 | 0,1113487 | 224 | 0,1194549 | 234,5 | 0,12796642 |
| 204 | 0,10324249 | 214,5 | 0,11175401 | 224,5 | 0,11986021 | 235 | 0,12837173 |
| 204,5 | 0,1036478 | 215 | 0,11215932 | 225 | 0,12026552 | 235,5 | 0,12877704 |
| 205 | 0,10405311 | 215,5 | 0,11256463 | 225,5 | 0,12067084 | 236 | 0,12918235 |
| 205,5 | 0,10445842 | 216 | 0,11296994 | 226 | 0,12107615 | 236,5 | 0,12958766 |
| 206 | 0,10486373 | 216,5 | 0,11337525 | 226,5 | 0,12148146 | 237 | 0,12999297 |
| 206,5 | 0,10526904 | 217 | 0,11378056 | 227 | 0,12188677 | 237,5 | 0,13039828 |
| 207 | 0,10567435 | 217,5 | 0,11418587 | 227,5 | 0,12229208 | 238 | 0,13080359 |
| 207,5 | 0,10607966 | 218 | 0,11459118 | 228 | 0,12269739 | 238,5 | 0,1312089 |
| 208 | 0,10648497 | 218,5 | 0,11499649 | 228,5 | 0,1231027 | 239 | 0,13161421 |
| 208,5 | 0,10689028 | 219 | 0,1154018 | 229 | 0,12350801 | 239,5 | 0,13201952 |
| 209 | 0,1072956 | 219,5 | 0,11580711 | 229,5 | 0,12391332 | 240 | 0,13242483 |
| 209,5 | 0,10770091 | 220 | 0,11621242 | 230 | 0,12431863 | 240,5 | 0,13283014 |
| 210 | 0,10810622 | 220,5 | 0,11661773 | 230,5 | 0,12472394 | 241 | 0,13323545 |

| х | у | х | У | х | У | х | у |
|-------|------------|-------|------------|-------|------------|-------|------------|
| 241,5 | 0,13364076 | 262 | 0,15025849 | 282,5 | 0,16687621 | 303 | 0,18349393 |
| 242 | 0,13404608 | 262,5 | 0,1506638 | 283 | 0,16728152 | 303,5 | 0,18389924 |
| 242,5 | 0,13445139 | 263 | 0,15106911 | 283,5 | 0,16768683 | 304 | 0,18430455 |
| 243 | 0,1348567 | 263,5 | 0,15147442 | 284 | 0,16809214 | 304,5 | 0,18470986 |
| 243,5 | 0,13526201 | 264 | 0,15187973 | 284,5 | 0,16849745 | 305 | 0,18511517 |
| 244 | 0,13566732 | 264,5 | 0,15228504 | 285 | 0,16890276 | 305,5 | 0,18552048 |
| 244,5 | 0,13607263 | 265 | 0,15269035 | 285,5 | 0,16930807 | 306 | 0,18592579 |
| 245 | 0,13647794 | 265,5 | 0,15309566 | 286 | 0,16971338 | 306,5 | 0,1863311 |
| 245,5 | 0,13688325 | 266 | 0,15350097 | 286,5 | 0,17011869 | 307 | 0,18673641 |
| 246 | 0,13728856 | 266,5 | 0,15390628 | 287 | 0,170524 | 307,5 | 0,18714172 |
| 246,5 | 0,13769387 | 267 | 0,15431159 | 287,5 | 0,17092931 | 308 | 0,18754703 |
| 247 | 0,13809918 | 267,5 | 0,1547169 | 288 | 0,17133462 | 308,5 | 0,18795234 |
| 247,5 | 0,13850449 | 268 | 0,15512221 | 288,5 | 0,17173993 | 309 | 0,18835766 |
| 248 | 0,1389098 | 268,5 | 0,15552752 | 289 | 0,17214524 | 309,5 | 0,18876297 |
| 248,5 | 0,13931511 | 269 | 0,15593283 | 289,5 | 0,17255055 | 310 | 0,18916828 |
| 249 | 0,13972042 | 269,5 | 0,15633814 | 290 | 0,17295586 | 310,5 | 0,18957359 |
| 249,5 | 0,14012573 | 270 | 0,15674345 | 290,5 | 0,17336117 | 311 | 0,1899789 |
| 250 | 0,14053104 | 270,5 | 0,15714876 | 291 | 0,17376648 | 311,5 | 0,19038421 |
| 250,5 | 0,14093635 | 271 | 0,15755407 | 291,5 | 0,17417179 | 312 | 0,19078952 |
| 251 | 0,14134166 | 271,5 | 0,15795938 | 292 | 0,17457711 | 312,5 | 0,19119483 |
| 251,5 | 0,14174697 | 272 | 0,15836469 | 292,5 | 0,17498242 | 313 | 0,19160014 |
| 252 | 0,14215228 | 272,5 | 0,15877 | 293 | 0,17538773 | 313,5 | 0,19200545 |
| 252,5 | 0,14255759 | 273 | 0,15917531 | 293,5 | 0,17579304 | 314 | 0,19241076 |
| 253 | 0,1429629 | 273,5 | 0,15958062 | 294 | 0,17619835 | 314,5 | 0,19281607 |
| 253,5 | 0,14336821 | 274 | 0,15998593 | 294,5 | 0,17660366 | 315 | 0,19322138 |
| 254 | 0,14377352 | 274,5 | 0,16039124 | 295 | 0,17700897 | 315,5 | 0,19362669 |
| 254,5 | 0,14417883 | 275 | 0,16079655 | 295,5 | 0,17741428 | 316 | 0,194032 |
| 255 | 0,14458414 | 275,5 | 0,16120187 | 296 | 0,17781959 | 316,5 | 0,19443731 |
| 255,5 | 0,14498945 | 276 | 0,16160718 | 296,5 | 0,1782249 | 317 | 0,19484262 |
| 256 | 0,14539476 | 276,5 | 0,16201249 | 297 | 0,17863021 | 317,5 | 0,19524793 |
| 256,5 | 0,14580007 | 277 | 0,1624178 | 297,5 | 0,17903552 | 318 | 0,19565324 |
| 257 | 0,14620538 | 277,5 | 0,16282311 | 298 | 0,17944083 | 318,5 | 0,19605855 |
| 257,5 | 0,14661069 | 278 | 0,16322842 | 298,5 | 0,17984614 | 319 | 0,19646386 |
| 258 | 0,147016 | 278,5 | 0,16363373 | 299 | 0,18025145 | 319,5 | 0,19686917 |
| 258,5 | 0,14742131 | 279 | 0,16403904 | 299,5 | 0,18065676 | 320 | 0,19727448 |
| 259 | 0,14782663 | 279,5 | 0,16444435 | 300 | 0,18106207 | 320,5 | 0,19767979 |
| 259,5 | 0,14823194 | 280 | 0,16484966 | 300,5 | 0,18146738 | 321 | 0,1980851 |
| 260 | 0,14863725 | 280,5 | 0,16525497 | 301 | 0,18187269 | 321,5 | 0,19849041 |
| 260,5 | 0,14904256 | 281 | 0,16566028 | 301,5 | 0,182278 | 322 | 0,19889572 |
| 261 | 0,14944787 | 281,5 | 0,16606559 | 302 | 0,18268331 | 322,5 | 0,19930103 |
| 261,5 | 0,14985318 | 282 | 0,1664709 | 302,5 | 0,18308862 | 323 | 0,19970634 |

| Х | У | х | у | Х | у | Х | у |
|-------|------------|-------|------------|-------|------------|-------|------------|
| 323,5 | 0,20011165 | 344 | 0,27098808 | 364,5 | 0,38958679 | 385 | 0,53759317 |
| 324 | 0,20051696 | 344,5 | 0,27272521 | 365 | 0,39465402 | 385,5 | 0,54023968 |
| 324,5 | 0,20092226 | 345 | 0,27451492 | 365,5 | 0,39950708 | 386 | 0,54260126 |
| 325 | 0,2034528 | 345,5 | 0,27663126 | 366 | 0,40321924 | 386,5 | 0,54406027 |
| 325,5 | 0,20570801 | 346 | 0,28014678 | 366,5 | 0,40767384 | 387 | 0,54580438 |
| 326 | 0,20677937 | 346,5 | 0,28280938 | 367 | 0,41256686 | 387,5 | 0,54666203 |
| 326,5 | 0,20820061 | 347 | 0,28489587 | 367,5 | 0,41673705 | 388 | 0,5475196 |
| 327 | 0,2103469 | 347,5 | 0,28581903 | 368 | 0,42030611 | 388,5 | 0,54860876 |
| 327,5 | 0,21265122 | 348 | 0,28704701 | 368,5 | 0,42381573 | 389 | 0,551424 |
| 328 | 0,21535717 | 348,5 | 0,2888714 | 369 | 0,4276312 | 389,5 | 0,55413936 |
| 328,5 | 0,21906251 | 349 | 0,29013199 | 369,5 | 0,43193139 | 390 | 0,556395 |
| 329 | 0,22190914 | 349,5 | 0,29068276 | 370 | 0,43613679 | 390,5 | 0,55811897 |
| 329,5 | 0,22332472 | 350 | 0,29137388 | 370,5 | 0,44120732 | 391 | 0,55982424 |
| 330 | 0,22444821 | 350,5 | 0,29168005 | 371 | 0,44696633 | 391,5 | 0,56015285 |
| 330,5 | 0,22529732 | 351 | 0,29412418 | 371,5 | 0,45215014 | 392 | 0,5604616 |
| 331 | 0,22705676 | 351,5 | 0,29500368 | 372 | 0,45626969 | 392,5 | 0,56114823 |
| 331,5 | 0,22899056 | 352 | 0,2961787 | 372,5 | 0,46018622 | 393 | 0,5627038 |
| 332 | 0,23046834 | 352,5 | 0,29786687 | 373 | 0,46391011 | 393,5 | 0,56447851 |
| 332,5 | 0,23420472 | 353 | 0,29841641 | 373,5 | 0,46741315 | 394 | 0,56568783 |
| 333 | 0,23673219 | 353,5 | 0,29926625 | 374 | 0,47044079 | 394,5 | 0,56679893 |
| 333,5 | 0,23922888 | 354 | 0,29934965 | 374,5 | 0,47386883 | 395 | 0,56799433 |
| 334 | 0,24224858 | 354,5 | 0,29980367 | 375 | 0,47777377 | 395,5 | 0,5690261 |
| 334,5 | 0,24407307 | 355 | 0,30126526 | 375,5 | 0,48138786 | 396 | 0,56988992 |
| 335 | 0,24637838 | 355,5 | 0,30262296 | 376 | 0,48518823 | 396,5 | 0,57093013 |
| 335,5 | 0,24699068 | 356 | 0,30485276 | 376,5 | 0,48944603 | 397 | 0,57238438 |
| 336 | 0,24674729 | 356,5 | 0,30712108 | 377 | 0,49308434 | 397,5 | 0,57405921 |
| 336,5 | 0,24690098 | 357 | 0,30832527 | 377,5 | 0,49650027 | 398 | 0,57549005 |
| 337 | 0,24673058 | 357,5 | 0,30925625 | 378 | 0,49981999 | 398,5 | 0,57639572 |
| 337,5 | 0,24743407 | 358 | 0,31015041 | 378,5 | 0,50291958 | 399 | 0,57710501 |
| 338 | 0,24913003 | 358,5 | 0,3109769 | 379 | 0,5059637 | 399,5 | 0,57808952 |
| 338,5 | 0,25045434 | 359 | 0,31727008 | 379,5 | 0,50897114 | 400 | 0,57865093 |
| 339 | 0,25207383 | 359,5 | 0,32770717 | 380 | 0,51200589 | 400,5 | 0,58057339 |
| 339,5 | 0,25276749 | 360 | 0,33482331 | 380,5 | 0,51484288 | 401 | 0,58326454 |
| 340 | 0,25382909 | 360,5 | 0,34157204 | 381 | 0,5171204 | 401,5 | 0,58521477 |
| 340,5 | 0,25550544 | 361 | 0,3474406 | 381,5 | 0,52088679 | 402 | 0,5860436 |
| 341 | 0,25768244 | 361,5 | 0,35334695 | 382 | 0,52449703 | 402,5 | 0,58693623 |
| 341,5 | 0,26051461 | 362 | 0,35916011 | 382,5 | 0,52674102 | 403 | 0,58688598 |
| 342 | 0,26442875 | 362,5 | 0,3653456 | 383 | 0,52944066 | 403,5 | 0,58607038 |
| 342,5 | 0,26768002 | 363 | 0,37183722 | 383,5 | 0,53180678 | 404 | 0,58532537 |
| 343 | 0,26932547 | 363,5 | 0,3781978 | 384 | 0,53385068 | 404,5 | 0,58601984 |
| 343,5 | 0,27018697 | 364 | 0,38436703 | 384,5 | 0,53533448 | 405 | 0,58772221 |

| Х | У | х | у | х | у | х | у |
|-------|------------|-------|------------|-------|------------|-------|------------|
| 405,5 | 0,58944827 | 426 | 0,66414191 | 446,5 | 0,79548678 | 467 | 0,82158747 |
| 406 | 0,59140093 | 426,5 | 0,66520221 | 447 | 0,79682371 | 467,5 | 0,82352636 |
| 406,5 | 0,59392884 | 427 | 0,66496217 | 447,5 | 0,79803538 | 468 | 0,82546253 |
| 407 | 0,59599784 | 427,5 | 0,66552291 | 448 | 0,79926821 | 468,5 | 0,82785093 |
| 407,5 | 0,59775415 | 428 | 0,66794234 | 448,5 | 0,80040362 | 469 | 0,82993148 |
| 408 | 0,59902748 | 428,5 | 0,68302737 | 449 | 0,80151945 | 469,5 | 0,83159755 |
| 408,5 | 0,60090672 | 429 | 0,69501163 | 449,5 | 0,80278414 | 470 | 0,83258149 |
| 409 | 0,60261968 | 429,5 | 0,70308327 | 450 | 0,80392216 | 470,5 | 0,83413407 |
| 409,5 | 0,60313574 | 430 | 0,71100454 | 450,5 | 0,80516185 | 471 | 0,83588835 |
| 410 | 0,60411906 | 430,5 | 0,71917382 | 451 | 0,80640996 | 471,5 | 0,83767926 |
| 410,5 | 0,60430931 | 431 | 0,72749589 | 451,5 | 0,80749873 | 472 | 0,83980136 |
| 411 | 0,60508474 | 431,5 | 0,73429696 | 452 | 0,80845294 | 472,5 | 0,84239036 |
| 411,5 | 0,60653795 | 432 | 0,73956165 | 452,5 | 0,8088953 | 473 | 0,84468121 |
| 412 | 0,60889189 | 432,5 | 0,74363971 | 453 | 0,80917446 | 473,5 | 0,84707523 |
| 412,5 | 0,61255725 | 433 | 0,74851582 | 453,5 | 0,80981581 | 474 | 0,84873752 |
| 413 | 0,61509797 | 433,5 | 0,75342301 | 454 | 0,81018165 | 474,5 | 0,85142303 |
| 413,5 | 0,61711483 | 434 | 0,75756286 | 454,5 | 0,81037631 | 475 | 0,85350273 |
| 414 | 0,61982829 | 434,5 | 0,76089671 | 455 | 0,81070277 | 475,5 | 0,85585692 |
| 414,5 | 0,62185286 | 435 | 0,7642031 | 455,5 | 0,81101202 | 476 | 0,85835267 |
| 415 | 0,62459071 | 435,5 | 0,76636456 | 456 | 0,8114193 | 476,5 | 0,86131364 |
| 415,5 | 0,62756784 | 436 | 0,7683568 | 456,5 | 0,81140988 | 477 | 0,86376876 |
| 416 | 0,63025455 | 436,5 | 0,7694038 | 457 | 0,81154456 | 477,5 | 0,86677686 |
| 416,5 | 0,63303692 | 437 | 0,77156028 | 457,5 | 0,81205189 | 478 | 0,86941082 |
| 417 | 0,63438445 | 437,5 | 0,77336645 | 458 | 0,81215328 | 478,5 | 0,87248389 |
| 417,5 | 0,63609817 | 438 | 0,77497163 | 458,5 | 0,81212197 | 479 | 0,87527903 |
| 418 | 0,63753225 | 438,5 | 0,77677324 | 459 | 0,81253141 | 479,5 | 0,87779526 |
| 418,5 | 0,63984394 | 439 | 0,77842128 | 459,5 | 0,81278389 | 480 | 0,88059277 |
| 419 | 0,64344801 | 439,5 | 0,78025927 | 460 | 0,813136 | 480,5 | 0,88359554 |
| 419,5 | 0,64621152 | 440 | 0,78231565 | 460,5 | 0,81345345 | 481 | 0,88634683 |
| 420 | 0,64804053 | 440,5 | 0,78351898 | 461 | 0,81384278 | 481,5 | 0,88967538 |
| 420,5 | 0,65070405 | 441 | 0,78458577 | 461,5 | 0,81449844 | 482 | 0,89308983 |
| 421 | 0,65252769 | 441,5 | 0,78519551 | 462 | 0,81495622 | 482,5 | 0,8965421 |
| 421,5 | 0,65364521 | 442 | 0,78596309 | 462,5 | 0,81516916 | 483 | 0,90033388 |
| 422 | 0,65496565 | 442,5 | 0,78692342 | 463 | 0,81526757 | 483,5 | 0,90367248 |
| 422,5 | 0,65810709 | 443 | 0,78764464 | 463,5 | 0,8154997 | 484 | 0,90711665 |
| 423 | 0,66072169 | 443,5 | 0,78868584 | 464 | 0,81559412 | 484,5 | 0,90981903 |
| 423,5 | 0,66173749 | 444 | 0,78986865 | 464,5 | 0,81626277 | 485 | 0,91247787 |
| 424 | 0,66329449 | 444,5 | 0,79075931 | 465 | 0,81723603 | 485,5 | 0,91546812 |
| 424,5 | 0,66446492 | 445 | 0,79172027 | 465,5 | 0,81817732 | 486 | 0,91908887 |
| 425 | 0,66458841 | 445,5 | 0,7929377 | 466 | 0,81916644 | 486,5 | 0,92271361 |
| 425,5 | 0,66428902 | 446 | 0,7942865 | 466,5 | 0,8200904 | 487 | 0,92639404 |

| Х | у | х | у | Х | у | х | у |
|-------|------------|-------|------------|-------|------------|-------|------------|
| 487,5 | 0,92932888 | 508 | 0,98957074 | 528,5 | 0,99338588 | 549 | 0,93929354 |
| 488 | 0,93261875 | 508,5 | 0,99182092 | 529 | 0,99291063 | 549,5 | 0,93822099 |
| 488,5 | 0,93499035 | 509 | 0,99261146 | 529,5 | 0,99186082 | 550 | 0,9370588 |
| 489 | 0,9371212 | 509,5 | 0,99260836 | 530 | 0,99059967 | 550,5 | 0,93580876 |
| 489,5 | 0,93961043 | 510 | 0,99290366 | 530,5 | 0,9897766 | 551 | 0,93434914 |
| 490 | 0,94210943 | 510,5 | 0,99248663 | 531 | 0,98899595 | 551,5 | 0,93372238 |
| 490,5 | 0,94448909 | 511 | 0,99123934 | 531,5 | 0,98730991 | 552 | 0,93273088 |
| 491 | 0,94640872 | 511,5 | 0,99186143 | 532 | 0,98623749 | 552,5 | 0,93147543 |
| 491,5 | 0,9476274 | 512 | 0,99296395 | 532,5 | 0,98548104 | 553 | 0,93069876 |
| 492 | 0,94991885 | 512,5 | 0,99402527 | 533 | 0,98524476 | 553,5 | 0,93007349 |
| 492,5 | 0,95153587 | 513 | 0,99477048 | 533,5 | 0,98500265 | 554 | 0,92816125 |
| 493 | 0,952717 | 513,5 | 0,99591097 | 534 | 0,98431891 | 554,5 | 0,92614182 |
| 493,5 | 0,95428916 | 514 | 0,99617767 | 534,5 | 0,98322941 | 555 | 0,92428908 |
| 494 | 0,95562412 | 514,5 | 0,99570785 | 535 | 0,98165809 | 555,5 | 0,92192555 |
| 494,5 | 0,95662233 | 515 | 0,99515938 | 535,5 | 0,97939523 | 556 | 0,92022152 |
| 495 | 0,95765247 | 515,5 | 0,99563943 | 536 | 0,97734214 | 556,5 | 0,91908409 |
| 495,5 | 0,95822546 | 516 | 0,99589975 | 536,5 | 0,97595005 | 557 | 0,9181633 |
| 496 | 0,95923085 | 516,5 | 0,99554797 | 537 | 0,97501676 | 557,5 | 0,91678182 |
| 496,5 | 0,96025009 | 517 | 0,99588712 | 537,5 | 0,97498493 | 558 | 0,91560898 |
| 497 | 0,96133252 | 517,5 | 0,99616987 | 538 | 0,97444204 | 558,5 | 0,91489905 |
| 497,5 | 0,96288895 | 518 | 0,99623492 | 538,5 | 0,97343923 | 559 | 0,91439865 |
| 498 | 0,96496044 | 518,5 | 0,99678348 | 539 | 0,97265007 | 559,5 | 0,91312885 |
| 498,5 | 0,96664175 | 519 | 0,99775986 | 539,5 | 0,97150879 | 560 | 0,91257552 |
| 499 | 0,96917266 | 519,5 | 0,99863138 | 540 | 0,96965826 | 560,5 | 0,91088185 |
| 499,5 | 0,97119241 | 520 | 0,99946674 | 540,5 | 0,96846323 | 561 | 0,90870027 |
| 500 | 0,97403768 | 520,5 | 0,999917 | 541 | 0,96696707 | 561,5 | 0,90672681 |
| 500,5 | 0,97826891 | 521 | 0,99994357 | 541,5 | 0,96616944 | 562 | 0,9045347 |
| 501 | 0,98330085 | 521,5 | 1 | 542 | 0,96453189 | 562,5 | 0,90265292 |
| 501,5 | 0,98582558 | 522 | 0,99948841 | 542,5 | 0,96274395 | 563 | 0,90172423 |
| 502 | 0,98802851 | 522,5 | 0,99904763 | 543 | 0,96191734 | 563,5 | 0,8999268 |
| 502,5 | 0,98970453 | 523 | 0,99879539 | 543,5 | 0,96061479 | 564 | 0,89807896 |
| 503 | 0,99109571 | 523,5 | 0,99849626 | 544 | 0,95920872 | 564,5 | 0,89510217 |
| 503,5 | 0,9906279 | 524 | 0,99807468 | 544,5 | 0,95825909 | 565 | 0,89271822 |
| 504 | 0,99054831 | 524,5 | 0,99758524 | 545 | 0,95639883 | 565,5 | 0,89024962 |
| 504,5 | 0,99159303 | 525 | 0,99734422 | 545,5 | 0,95510199 | 566 | 0,88701336 |
| 505 | 0,99220256 | 525,5 | 0,99720147 | 546 | 0,95313426 | 566,5 | 0,88475604 |
| 505,5 | 0,99051946 | 526 | 0,99655815 | 546,5 | 0,95108829 | 567 | 0,88351098 |
| 506 | 0,99001876 | 526,5 | 0,99609374 | 547 | 0,94895015 | 567,5 | 0,881133 |
| 506,5 | 0,98959168 | 527 | 0,99598566 | 547,5 | 0,94652785 | 568 | 0,87921986 |
| 507 | 0,9890121 | 527,5 | 0,99537412 | 548 | 0,94416624 | 568,5 | 0,87763952 |
| 507,5 | 0,98856745 | 528 | 0,9946039 | 548,5 | 0,94177078 | 569 | 0,87627495 |

| X | у | х | у | х | у | х | у |
|-------|------------|-------|------------|-------|------------|-------|------------|
| 569,5 | 0,87473392 | 590 | 0,77461699 | 610,5 | 0,69647516 | 631 | 0,61546999 |
| 570 | 0,87198433 | 590,5 | 0,77208583 | 611 | 0,69592488 | 631,5 | 0,61346841 |
| 570,5 | 0,86936626 | 591 | 0,76937811 | 611,5 | 0,69293872 | 632 | 0,61157311 |
| 571 | 0,86694708 | 591,5 | 0,76670762 | 612 | 0,69083567 | 632,5 | 0,60926058 |
| 571,5 | 0,86381157 | 592 | 0,76229151 | 612,5 | 0,68975422 | 633 | 0,60757064 |
| 572 | 0,86103442 | 592,5 | 0,75941551 | 613 | 0,68907131 | 633,5 | 0,60614211 |
| 572,5 | 0,85876809 | 593 | 0,75710474 | 613,5 | 0,68849249 | 634 | 0,60382029 |
| 573 | 0,85607276 | 593,5 | 0,7549342 | 614 | 0,68862091 | 634,5 | 0,60151119 |
| 573,5 | 0,85353594 | 594 | 0,75240077 | 614,5 | 0,68534709 | 635 | 0,59908909 |
| 574 | 0,85028439 | 594,5 | 0,75101202 | 615 | 0,68214134 | 635,5 | 0,59540083 |
| 574,5 | 0,84679051 | 595 | 0,74934642 | 615,5 | 0,68147713 | 636 | 0,59164515 |
| 575 | 0,84414396 | 595,5 | 0,747443 | 616 | 0,68098258 | 636,5 | 0,59065795 |
| 575,5 | 0,84316124 | 596 | 0,74517542 | 616,5 | 0,67809951 | 637 | 0,58967585 |
| 576 | 0,84128642 | 596,5 | 0,74432215 | 617 | 0,67553139 | 637,5 | 0,58766428 |
| 576,5 | 0,83853238 | 597 | 0,74240549 | 617,5 | 0,67378072 | 638 | 0,58506191 |
| 577 | 0,83496869 | 597,5 | 0,74107856 | 618 | 0,6717841 | 638,5 | 0,58134794 |
| 577,5 | 0,83165409 | 598 | 0,7402797 | 618,5 | 0,66720925 | 639 | 0,57768402 |
| 578 | 0,8292567 | 598,5 | 0,73638311 | 619 | 0,66360967 | 639,5 | 0,57582908 |
| 578,5 | 0,82650169 | 599 | 0,73481973 | 619,5 | 0,66189848 | 640 | 0,57482352 |
| 579 | 0,82427942 | 599,5 | 0,73368828 | 620 | 0,66095916 | 640,5 | 0,57298523 |
| 579,5 | 0,8240997 | 600 | 0,73228161 | 620,5 | 0,6593932 | 641 | 0,57083314 |
| 580 | 0,82259124 | 600,5 | 0,72925532 | 621 | 0,65848722 | 641,5 | 0,57011501 |
| 580,5 | 0,81944556 | 601 | 0,72662252 | 621,5 | 0,65743958 | 642 | 0,56866488 |
| 581 | 0,81617982 | 601,5 | 0,72231519 | 622 | 0,65571756 | 642,5 | 0,56391976 |
| 581,5 | 0,81358714 | 602 | 0,71893299 | 622,5 | 0,65349849 | 643 | 0,55975168 |
| 582 | 0,81253161 | 602,5 | 0,7178324 | 623 | 0,65113899 | 643,5 | 0,55827537 |
| 582,5 | 0,81092228 | 603 | 0,71774234 | 623,5 | 0,64779128 | 644 | 0,55696742 |
| 583 | 0,80918959 | 603,5 | 0,71715464 | 624 | 0,64540404 | 644,5 | 0,55486183 |
| 583,5 | 0,80835986 | 604 | 0,71606747 | 624,5 | 0,64356557 | 645 | 0,55290461 |
| 584 | 0,80724644 | 604,5 | 0,71335187 | 625 | 0,64184439 | 645,5 | 0,54954845 |
| 584,5 | 0,80434819 | 605 | 0,71118451 | 625,5 | 0,64051255 | 646 | 0,54643536 |
| 585 | 0,80118419 | 605,5 | 0,71070014 | 626 | 0,63930243 | 646,5 | 0,54365787 |
| 585,5 | 0,79840197 | 606 | 0,71056614 | 626,5 | 0,63698865 | 647 | 0,54084088 |
| 586 | 0,79638309 | 606,5 | 0,70805009 | 627 | 0,6337415 | 647,5 | 0,53808688 |
| 586,5 | 0,79412478 | 607 | 0,70471279 | 627,5 | 0,63020066 | 648 | 0,53535218 |
| 587 | 0,79180315 | 607,5 | 0,70337348 | 628 | 0,62751887 | 648,5 | 0,53276871 |
| 587,5 | 0,78946722 | 608 | 0,70231882 | 628,5 | 0,62591307 | 649 | 0,52995311 |
| 588 | 0,78687961 | 608,5 | 0,69917919 | 629 | 0,62428808 | 649,5 | 0,52835212 |
| 588,5 | 0,7834166 | 609 | 0,69665487 | 629,5 | 0,62365497 | 650 | 0,52735027 |
| 589 | 0,78064497 | 609,5 | 0,69691986 | 630 | 0,62280069 | 650,5 | 0,52354548 |
| 589,5 | 0,77808803 | 610 | 0,69712509 | 630,5 | 0,6195407 | 651 | 0,51949896 |

| X | у | Х | у | Х | у | Х | у |
|-------|------------|-------|------------|-------|------------|-------|------------|
| 651,5 | 0,51762594 | 672 | 0,41996585 | 692,5 | 0,34662317 | 713 | 0,30334257 |
| 652 | 0,51493878 | 672,5 | 0,418343 | 693 | 0,34395031 | 713,5 | 0,30195234 |
| 652,5 | 0,51220786 | 673 | 0,41617892 | 693,5 | 0,34439339 | 714 | 0,29943126 |
| 653 | 0,51000472 | 673,5 | 0,41387729 | 694 | 0,34466448 | 714,5 | 0,29655853 |
| 653,5 | 0,50712114 | 674 | 0,41153193 | 694,5 | 0,34370933 | 715 | 0,29113679 |
| 654 | 0,50346637 | 674,5 | 0,40833641 | 695 | 0,34262399 | 715,5 | 0,28940514 |
| 654,5 | 0,50154226 | 675 | 0,40579048 | 695,5 | 0,34126215 | 716 | 0,28929235 |
| 655 | 0,49965706 | 675,5 | 0,404173 | 696 | 0,33865475 | 716,5 | 0,28647343 |
| 655,5 | 0,49560226 | 676 | 0,40213725 | 696,5 | 0,33758003 | 717 | 0,28403835 |
| 656 | 0,49217514 | 676,5 | 0,39955626 | 697 | 0,33665644 | 717,5 | 0,2845175 |
| 656,5 | 0,49125604 | 677 | 0,39776025 | 697,5 | 0,33393246 | 718 | 0,28383367 |
| 657 | 0,48978098 | 677,5 | 0,39586873 | 698 | 0,33085498 | 718,5 | 0,27950783 |
| 657,5 | 0,48645855 | 678 | 0,39403116 | 698,5 | 0,32864257 | 719 | 0,27567601 |
| 658 | 0,48296907 | 678,5 | 0,39290018 | 699 | 0,32679873 | 719,5 | 0,27682827 |
| 658,5 | 0,47929994 | 679 | 0,39158957 | 699,5 | 0,32551716 | 720 | 0,27857326 |
| 659 | 0,47519963 | 679,5 | 0,38886871 | 700 | 0,3249992 | 720,5 | 0,27911966 |
| 659,5 | 0,47200553 | 680 | 0,38645026 | 700,5 | 0,32658129 | 721 | 0,28064649 |
| 660 | 0,46916755 | 680,5 | 0,38466472 | 701 | 0,32777531 | 721,5 | 0,2800922 |
| 660,5 | 0,46740837 | 681 | 0,3827873 | 701,5 | 0,32725236 | 722 | 0,27894781 |
| 661 | 0,46657649 | 681,5 | 0,38205699 | 702 | 0,32632654 | 722,5 | 0,27751121 |
| 661,5 | 0,46307351 | 682 | 0,38183135 | 702,5 | 0,32327231 | 723 | 0,27724215 |
| 662 | 0,45970032 | 682,5 | 0,37871574 | 703 | 0,32027738 | 723,5 | 0,27536396 |
| 662,5 | 0,45808897 | 683 | 0,37554937 | 703,5 | 0,32136386 | 724 | 0,27331927 |
| 663 | 0,45650031 | 683,5 | 0,37428823 | 704 | 0,32237538 | 724,5 | 0,2744369 |
| 663,5 | 0,45516194 | 684 | 0,37266022 | 704,5 | 0,31993323 | 725 | 0,27536169 |
| 664 | 0,45314005 | 684,5 | 0,37068274 | 705 | 0,31571837 | 725,5 | 0,26972396 |
| 664,5 | 0,45088701 | 685 | 0,36971031 | 705,5 | 0,31343651 | 726 | 0,26518003 |
| 665 | 0,44895068 | 685,5 | 0,36801031 | 706 | 0,31128361 | 726,5 | 0,26733064 |
| 665,5 | 0,4448571 | 686 | 0,36646342 | 706,5 | 0,30895477 | 727 | 0,26843919 |
| 666 | 0,44096362 | 686,5 | 0,36517155 | 707 | 0,30890841 | 727,5 | 0,26527322 |
| 666,5 | 0,43991595 | 687 | 0,36398455 | 707,5 | 0,31018955 | 728 | 0,26357003 |
| 667 | 0,43932909 | 687,5 | 0,36234075 | 708 | 0,31108616 | 728,5 | 0,26367556 |
| 667,5 | 0,43758499 | 688 | 0,36084495 | 708,5 | 0,3093768 | 729 | 0,26394444 |
| 668 | 0,4358635 | 688,5 | 0,35749145 | 709 | 0,30743201 | 729,5 | 0,26346416 |
| 668,5 | 0,43399499 | 689 | 0,35449607 | 709,5 | 0,30719473 | 730 | 0,26164468 |
| 669 | 0,43074921 | 689,5 | 0,35492102 | 710 | 0,30566761 | 730,5 | 0,25998896 |
| 669,5 | 0,42871658 | 690 | 0,35580121 | 710,5 | 0,30642759 | 731 | 0,25600533 |
| 670 | 0,42738076 | 690,5 | 0,35489473 | 711 | 0,30754561 | 731,5 | 0,25182393 |
| 670,5 | 0,424096 | 691 | 0,35363693 | 711,5 | 0,30359769 | 732 | 0,24759435 |
| 671 | 0,42175227 | 691,5 | 0,35156672 | 712 | 0,30058804 | 732,5 | 0,24715566 |
| 671,5 | 0,42118099 | 692 | 0,3492493 | 712,5 | 0,30223054 | 733 | 0,24671639 |

| X | у | X | у | Х | у | Х | у |
|-------|------------|-------|------------|-------|------------|-------|------------|
| 733,5 | 0,24627712 | 754 | 0,22826711 | 774,5 | 0,2102571 | 795 | 0,19224709 |
| 734 | 0,24583785 | 754,5 | 0,22782784 | 775 | 0,20981783 | 795,5 | 0,19180782 |
| 734,5 | 0,24539858 | 755 | 0,22738857 | 775,5 | 0,20937856 | 796 | 0,19136856 |
| 735 | 0,24495931 | 755,5 | 0,2269493 | 776 | 0,2089393 | 796,5 | 0,19092929 |
| 735,5 | 0,24452004 | 756 | 0,22651004 | 776,5 | 0,20850003 | 797 | 0,19049002 |
| 736 | 0,24408078 | 756,5 | 0,22607077 | 777 | 0,20806076 | 797,5 | 0,19005075 |
| 736,5 | 0,24364151 | 757 | 0,2256315 | 777,5 | 0,20762149 | 798 | 0,18961148 |
| 737 | 0,24320224 | 757,5 | 0,22519223 | 778 | 0,20718222 | 798,5 | 0,18917221 |
| 737,5 | 0,24276297 | 758 | 0,22475296 | 778,5 | 0,20674295 | 799 | 0,18873295 |
| 738 | 0,2423237 | 758,5 | 0,22431369 | 779 | 0,20630369 | 799,5 | 0,18829368 |
| 738,5 | 0,24188443 | 759 | 0,22387443 | 779,5 | 0,20586442 | 800 | 0,18785441 |
| 739 | 0,24144517 | 759,5 | 0,22343516 | 780 | 0,20542515 | 800,5 | 0,18741514 |
| 739,5 | 0,2410059 | 760 | 0,22299589 | 780,5 | 0,20498588 | 801 | 0,18697587 |
| 740 | 0,24056663 | 760,5 | 0,22255662 | 781 | 0,20454661 | 801,5 | 0,1865366 |
| 740,5 | 0,24012736 | 761 | 0,22211735 | 781,5 | 0,20410734 | 802 | 0,18609733 |
| 741 | 0,23968809 | 761,5 | 0,22167808 | 782 | 0,20366807 | 802,5 | 0,18565807 |
| 741,5 | 0,23924882 | 762 | 0,22123881 | 782,5 | 0,20322881 | 803 | 0,1852188 |
| 742 | 0,23880955 | 762,5 | 0,22079955 | 783 | 0,20278954 | 803,5 | 0,18477953 |
| 742,5 | 0,23837029 | 763 | 0,22036028 | 783,5 | 0,20235027 | 804 | 0,18434026 |
| 743 | 0,23793102 | 763,5 | 0,21992101 | 784 | 0,201911 | 804,5 | 0,18390099 |
| 743,5 | 0,23749175 | 764 | 0,21948174 | 784,5 | 0,20147173 | 805 | 0,18346172 |
| 744 | 0,23705248 | 764,5 | 0,21904247 | 785 | 0,20103246 | 805,5 | 0,18302245 |
| 744,5 | 0,23661321 | 765 | 0,2186032 | 785,5 | 0,20059319 | 806 | 0,18258319 |
| 745 | 0,23617394 | 765,5 | 0,21816393 | 786 | 0,20015393 | 806,5 | 0,18214392 |
| 745,5 | 0,23573467 | 766 | 0,21772467 | 786,5 | 0,19971466 | 807 | 0,18170465 |
| 746 | 0,23529541 | 766,5 | 0,2172854 | 787 | 0,19927539 | 807,5 | 0,18126538 |
| 746,5 | 0,23485614 | 767 | 0,21684613 | 787,5 | 0,19883612 | 808 | 0,18082611 |
| 747 | 0,23441687 | 767,5 | 0,21640686 | 788 | 0,19839685 | 808,5 | 0,18038684 |
| 747,5 | 0,2339776 | 768 | 0,21596759 | 788,5 | 0,19795758 | 809 | 0,17994758 |
| 748 | 0,23353833 | 768,5 | 0,21552832 | 789 | 0,19751832 | 809,5 | 0,17950831 |
| 748,5 | 0,23309906 | 769 | 0,21508906 | 789,5 | 0,19707905 | 810 | 0,17906904 |
| 749 | 0,2326598 | 769,5 | 0,21464979 | 790 | 0,19663978 | 810,5 | 0,17862977 |
| 749,5 | 0,23222053 | 770 | 0,21421052 | 790,5 | 0,19620051 | 811 | 0,1781905 |
| 750 | 0,23178126 | 770,5 | 0,21377125 | 791 | 0,19576124 | 811,5 | 0,17775123 |
| 750,5 | 0,23134199 | 771 | 0,21333198 | 791,5 | 0,19532197 | 812 | 0,17731196 |
| 751 | 0,23090272 | 771,5 | 0,21289271 | 792 | 0,1948827 | 812,5 | 0,1768727 |
| 751,5 | 0,23046345 | 772 | 0,21245344 | 792,5 | 0,19444344 | 813 | 0,17643343 |
| 752 | 0,23002418 | 772,5 | 0,21201418 | 793 | 0,19400417 | 813,5 | 0,17599416 |
| 752,5 | 0,22958492 | 773 | 0,21157491 | 793,5 | 0,1935649 | 814 | 0,17555489 |
| 753 | 0,22914565 | 773,5 | 0,21113564 | 794 | 0,19312563 | 814,5 | 0,17511562 |
| 753,5 | 0,22870638 | 774 | 0,21069637 | 794,5 | 0,19268636 | 815 | 0,17467635 |

| х | у | Х | у | х | у | х | у |
|-------|------------|-------|------------|-------|------------|-------|------------|
| 815,5 | 0,17423708 | 836 | 0,15622708 | 856,5 | 0,13821707 | 877 | 0,12020706 |
| 816 | 0,17379782 | 836,5 | 0,15578781 | 857 | 0,1377778 | 877,5 | 0,11976779 |
| 816,5 | 0,17335855 | 837 | 0,15534854 | 857,5 | 0,13733853 | 878 | 0,11932852 |
| 817 | 0,17291928 | 837,5 | 0,15490927 | 858 | 0,13689926 | 878,5 | 0,11888925 |
| 817,5 | 0,17248001 | 838 | 0,15447 | 858,5 | 0,13645999 | 879 | 0,11844999 |
| 818 | 0,17204074 | 838,5 | 0,15403073 | 859 | 0,13602073 | 879,5 | 0,11801072 |
| 818,5 | 0,17160147 | 839 | 0,15359147 | 859,5 | 0,13558146 | 880 | 0,11757145 |
| 819 | 0,17116221 | 839,5 | 0,1531522 | 860 | 0,13514219 | 880,5 | 0,11713218 |
| 819,5 | 0,17072294 | 840 | 0,15271293 | 860,5 | 0,13470292 | 881 | 0,11669291 |
| 820 | 0,17028367 | 840,5 | 0,15227366 | 861 | 0,13426365 | 881,5 | 0,11625364 |
| 820,5 | 0,1698444 | 841 | 0,15183439 | 861,5 | 0,13382438 | 882 | 0,11581437 |
| 821 | 0,16940513 | 841,5 | 0,15139512 | 862 | 0,13338511 | 882,5 | 0,11537511 |
| 821,5 | 0,16896586 | 842 | 0,15095585 | 862,5 | 0,13294585 | 883 | 0,11493584 |
| 822 | 0,16852659 | 842,5 | 0,15051659 | 863 | 0,13250658 | 883,5 | 0,11449657 |
| 822,5 | 0,16808733 | 843 | 0,15007732 | 863,5 | 0,13206731 | 884 | 0,1140573 |
| 823 | 0,16764806 | 843,5 | 0,14963805 | 864 | 0,13162804 | 884,5 | 0,11361803 |
| 823,5 | 0,16720879 | 844 | 0,14919878 | 864,5 | 0,13118877 | 885 | 0,11317876 |
| 824 | 0,16676952 | 844,5 | 0,14875951 | 865 | 0,1307495 | 885,5 | 0,11273949 |
| 824,5 | 0,16633025 | 845 | 0,14832024 | 865,5 | 0,13031023 | 886 | 0,11230023 |
| 825 | 0,16589098 | 845,5 | 0,14788097 | 866 | 0,12987097 | 886,5 | 0,11186096 |
| 825,5 | 0,16545171 | 846 | 0,14744171 | 866,5 | 0,1294317 | 887 | 0,11142169 |
| 826 | 0,16501245 | 846,5 | 0,14700244 | 867 | 0,12899243 | 887,5 | 0,11098242 |
| 826,5 | 0,16457318 | 847 | 0,14656317 | 867,5 | 0,12855316 | 888 | 0,11054315 |
| 827 | 0,16413391 | 847,5 | 0,1461239 | 868 | 0,12811389 | 888,5 | 0,11010388 |
| 827,5 | 0,16369464 | 848 | 0,14568463 | 868,5 | 0,12767462 | 889 | 0,10966462 |
| 828 | 0,16325537 | 848,5 | 0,14524536 | 869 | 0,12723536 | 889,5 | 0,10922535 |
| 828,5 | 0,1628161 | 849 | 0,1448061 | 869,5 | 0,12679609 | 890 | 0,10878608 |
| 829 | 0,16237684 | 849,5 | 0,14436683 | 870 | 0,12635682 | 890,5 | 0,10834681 |
| 829,5 | 0,16193757 | 850 | 0,14392756 | 870,5 | 0,12591755 | 891 | 0,10790754 |
| 830 | 0,1614983 | 850,5 | 0,14348829 | 871 | 0,12547828 | 891,5 | 0,10746827 |
| 830,5 | 0,16105903 | 851 | 0,14304902 | 871,5 | 0,12503901 | 892 | 0,107029 |
| 831 | 0,16061976 | 851,5 | 0,14260975 | 872 | 0,12459974 | 892,5 | 0,10658974 |
| 831,5 | 0,16018049 | 852 | 0,14217048 | 872,5 | 0,12416048 | 893 | 0,10615047 |
| 832 | 0,15974122 | 852,5 | 0,14173122 | 873 | 0,12372121 | 893,5 | 0,1057112 |
| 832,5 | 0,15930196 | 853 | 0,14129195 | 873,5 | 0,12328194 | 894 | 0,10527193 |
| 833 | 0,15886269 | 853,5 | 0,14085268 | 874 | 0,12284267 | 894,5 | 0,10483266 |
| 833,5 | 0,15842342 | 854 | 0,14041341 | 874,5 | 0,1224034 | 895 | 0,10439339 |
| 834 | 0,15798415 | 854,5 | 0,13997414 | 875 | 0,12196413 | 895,5 | 0,10395412 |
| 834,5 | 0,15754488 | 855 | 0,13953487 | 875,5 | 0,12152486 | 896 | 0,10351486 |
| 835 | 0,15710561 | 855,5 | 0,1390956 | 876 | 0,1210856 | 896,5 | 0,10307559 |
| 835,5 | 0,15666634 | 856 | 0,13865634 | 876,5 | 0,12064633 | 897 | 0,10263632 |

| Х | у |
|-------|------------|
| 897,5 | 0,10219705 |
| 898 | 0,10175778 |
| 898,5 | 0,10131851 |
| 899 | 0,10087925 |
| 899,5 | 0,10043998 |
| 900 | 0,10000071 |