

# **DIPLOMA THESIS**

## **Parameter Estimation Based on Back Analysis of Measured Displacement Data in the Inntal Tunnel Project**

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## **Declaration**

I declare in lieu of oath that I did this thesis in hand by myself using only literature cited at the end of this work.

Graz, June 2010

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# ABSTRACT

The Convergence-Confinement Method has been used with success in tunnel design and it is nowadays considered a useful tool for the assessment of system behaviour. The method allows an approximate transformation of a four dimensional (spatial and temporal) problem, into a graphical, two-dimensional description of the system behaviour by using a Ground reaction Curve (GRC), Support Characteristic Curve (SCC) and the Longitudinal Deformation Profile (LDP). Its applicability is limited to conditions of high overburden and weak rock masses.

This study represents a practical application of the Convergence-Confinement Method for back analysis of rock mass properties. It is assumed that the rock mass satisfies the Mohr Coulomb failure criterion. The MATLAB code developed for the back analysis accounts for different support systems and their combinations, including shotcrete, non grouted bolts–cables, grouted bolts, open displacement gaps, lining stress controllers and steel profiles. The measured displacements are used as input values, and the rock mass parameters are varied until the final displacements and the longitudinal displacement profile are best fitting the measured data. This procedure was implemented in Matlab allowing several calculations for different values of Young's modulus ( $E$ ), cohesion ( $c$ ), and friction angle ( $\varphi$ ) to take place relatively fast. Combined values, which are in agreement with the measured displacements, are saved and later put to scrutiny.

The Inntal tunnel was used to apply the model. The project was selected based on the amount and quality of convergence data.

At the end of this study a discussion and conclusions are presented, mainly focusing on the usage of the convergence-confined method, comparisons of the proposed model with the formulation from Feder & Arwanitakis [1] and Finite Element (FE) simulations, comparisons between support systems, influence of

Young's moduli on the back analyzed parameters and the results for the specific study case.

# Kurzfassung

Das Kennlinienverfahren wird seit vielen Jahren erfolgreich in der Planung von Tunnelbauten eingesetzt und stellt ein nützliches Element zur Bestimmung des Systemverhaltens dar. Es ermöglicht ein vierdimensionales Problem (in Raum und Zeit) in eine graphische zweidimensionale Darstellung unter Verwendung von Gebirgskennlinie (Ground Reaction Curve GRC), Ausbaukennlinie (Support Characteristic Curve SCC) und der Tunnellängsentwicklung der radialen Verformungen (Longitudinal Deformation Profile LDP) zu transformieren. Das Verfahren ist jedoch nur begrenzt anwendbar in Fällen mit hoher Überlagerung und schwachem Gebirge.

In dieser Arbeit wird eine praktische Anwendung zur Rückrechnung der Gebirgsparameter mittels Kennlinienverfahren vorgestellt, wobei angenommen wird, dass das Gebirge dem Mohr Coulomb'schen Fehlerkriterium folgt. Der für die Rückrechnung entwickelte Matlab Code ist für verschiedene Stützmittel wie Spritzbeton, Freispielanker, Verbundanker, offene Verformungsschlitzte, Stauchelemente, Stahlprofile und deren Kombinationen anwendbar. Die Verschiebungsmessdaten werden als Eingangparameter verwendet, unter Variation der Gebirgsparameter wird versucht jene Kombination zu finden, bei der die errechneten Verschiebungen und das LDP (Longitudinal Deformation Profile) jenen gemessenen Verschiebungsdaten entsprechen. Diese Prozedur wurde in eine Matlab Entwicklung implementiert, die es erlaubt sämtliche Rechnungen für verschiedene Werte von Elastizitätsmodul ( $E$ ), Kohäsion ( $c$ ) und Reibungswinkel ( $\varphi$ ) in kurzer Zeit durchzuspielen. Die Parameter aus Kombinationen, die jene, den gemessenen Daten entsprechenden, Verschiebungen erzeugen, werden für weitere Untersuchungen gespeichert.

Das erarbeitete Modell wurde am Inntal Tunnel Projekt angewandt, welches aufgrund der Qualität und Quantität der Messdaten ausgewählt wurde.

Diese Arbeit konzentriert sich auf die Anwendung des Kennlinienverfahrens, den Vergleich jenes Modells mit Formulierung nach Feder et al. [17] mit Finite Elemente Simulationen, den Vergleich unterschiedlicher Stützmittel, den Einfluss von Elastizitätsmodul auf die rückgerechneten Parameter und die Ergebnisse der speziellen Studie.

# Abbreviations

|             |  |
|-------------|--|
| $\varphi_r$ | Residual friction angle  |
| $\tau$      | Shear strength / stress  |
| E           | Young's Modulus  |
| c           | Cohesion   |
| $\varphi$   | Friction angle   |
| $\psi$      | Creep coefficient  |
| $R_{adm}$   | Admissible error   |
| $K_o$       | lateral earth pressure coefficient   |
| H           | Overburden   |
| GRC         | Ground Reaction Curve  |
| SCC         | Support Characteristic Curve   |
| DBBA        | Displacement Based Back Analysis   |
| UDEC        | Universal Distinct Element Code  |
| FDM         | Finite Difference Method   |
| FEM         | Finite Element Method  |
| BEM         | Boundary Element Method  |
| SVM         | Support Vector Machines  |
| SMO         | Sequential Minimal Optimization  |
| NATM        | New Austrian Tunneling Method  |
| LSC         | Lining Stress Controller   |
| BAA         | Back Analysis Algorithm  |
| DEM         | Displacement Evaluation Model  |
| DBAP        | Direct Back Analysis Program   |
| BANSJI      | Back Analysis of Non-Linear Strains for<br>Jointed rock mass in Incremental form |



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# 1. Introduction

## 1.1. Problem description and aim of this work

Engineering means constantly searching and developing new methods and models in order to approach problems in a better and more accurate way. For the specific case of tunneling and underground constructions all project phases – especially design and construction- are filled with a wide range of uncertainties, which add more complexity to the problem. Engineers, in pursuit of both technical and economical solutions are driven into simplifications that often mislead to non-optimal solutions. Strong effort has been made to minimize this simplifications and uncertainties, better approach, sampling methods, monitoring, laboratory testing, numerical methods, higher order models, etc. are used for this purpose, but does one obtain accurate ground condition?

Displacement Based Back Analysis (DBBA) in tunneling is an indirect technique that attempts to find ground conditions (properties), based on monitored data. Clear advantages of this technique are to be seen. On the one hand, engineers are able to evaluate and predict equivalent mechanical constants of the ground that reflect the effects of cracks, joints and the non-linearity of the tunnel movements [2] and on the other hand, parameters can be continuously adjusted throughout a project. Based on the above written and due to its simplicity and maturity the DBBA has become a strong and widely used tool in tunneling and underground construction.

The main purpose of this thesis is to compare the Young's modulus, cohesion and internal friction angle considered for design – often based on laboratory and In situ testing - with those back calculated through DBBA; this is done by using the convergence-confinement method to implement the DBBA technique in the Inntal Tunnel project located in Austria, where a good monitoring program took place.

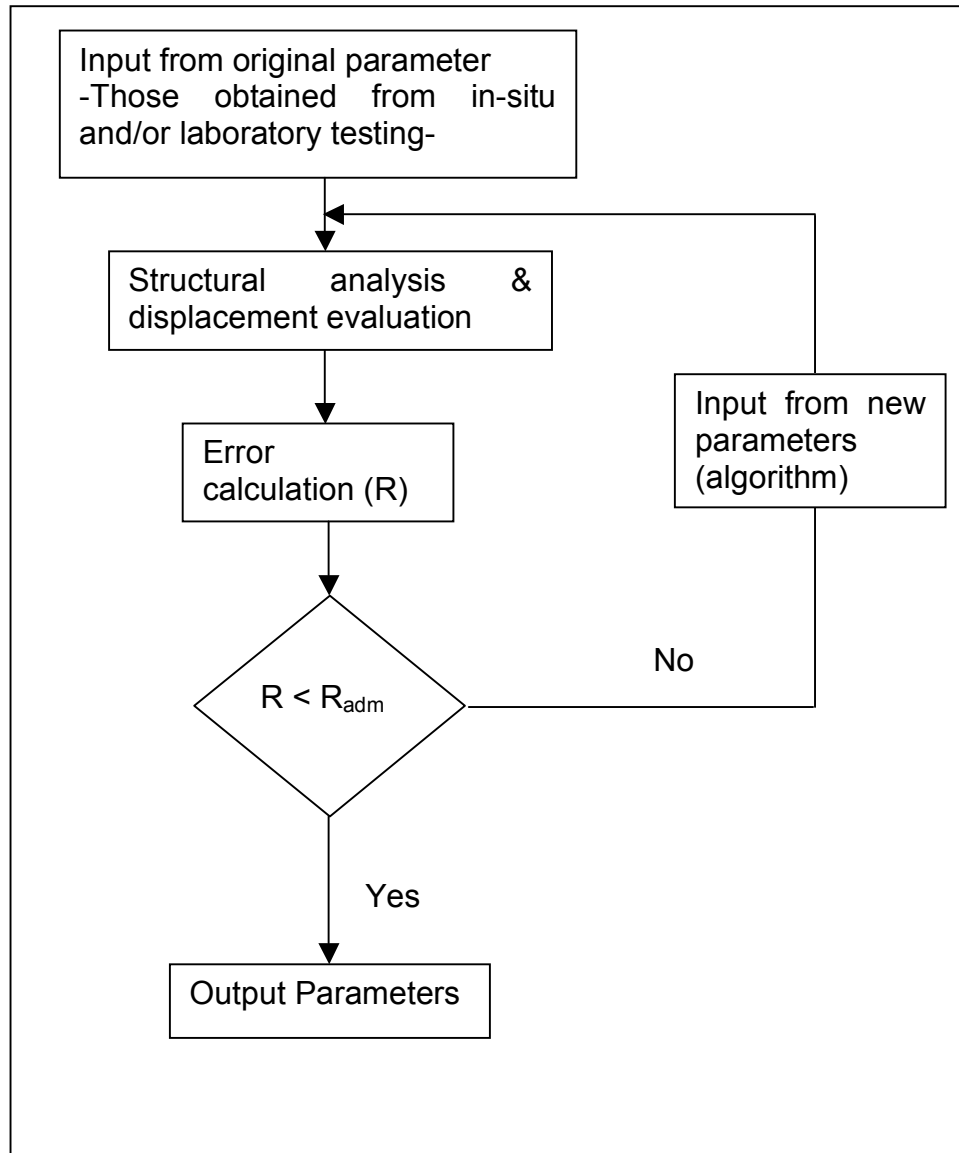
Xia-Ting et al. [3] and Fakhimi et al. [4] stated the importance of quantity and quality of monitoring data for the DBBA to work, it is shown that accuracy increases in a high degree with the quantity of monitored data, in order to avoid extrapolation and engineering judgments.

## 1.2. Literature review

Tunneling design is based on in-situ stresses as well as behavior and mechanical properties of surrounding rock masses, complications arise due to the fact that only small samples (cores) are tested to represent rock mass parameters and in situ stresses are calculated by using geological investigation and bore hole testing, leaving plenty of uncertainties behind. DBBA represents an interesting tool to optimize this rock mass properties - obtained by laboratory or in-situ testing - on projects where displacement data is available, as written by Oreste [5], DBBA can only be performed during or/and after the construction of the tunnel itself or of a pilot tunnel, since only in these stages it is possible to obtain a complete evaluation of the behavior of the rock mass based on displacements. Many researches have been made and papers have been written on DBBA for tunneling. [6] A wide range of Back Analysis procedures is available for tunnel engineering and one can say that all procedures follow the flow chart shown in Fig. 1. Differences lie in the selection of displacement evaluation model, the method used for the error calculation and the Back Analysis Algorithm (BAA) selected in order to minimize the error.

Regarding Displacement Evaluation Model, the error calculation and the BAA a number of models are proposed, for instance Shang et al. in [7] and [8] use the computational program BMP90 based on the Boundary Element Method (BEM) for the displacement calculation, the least square method for the error calculation and an intelligent back analysis algorithm which is based on the experiences of a tunnel expert or regulation grouping. Even though this method has shown good results one can observe disadvantages when comparing it to algorithms used by other

authors, as an expert or a board has to be present when the new input parameters are to be selected, giving this method less performance compared to other proposed methods.



**Fig. 1: Back Analysis Flow Chart**

Vardakos et al. [9] use the convergence-confinement method and transform it to be implemented in the Discrete Element Method (DEM) based Program UDEC (Universal Distinct Element Code), the computational program corrects itself by

means of the so called Loss Factor “ $\lambda_i$ ”. This factor is linked to the displacements and rock mass properties therefore when equilibrium is reached in between predicted displacements and measured displacements the process stops and the output parameters are read out. Due to the non-continuous model form UDEC and the convergence-confinement method a good representation of faults, fractures, joints, bending planes as well as support and construction stages can be realized, however this calculation is time-consuming.

Hisatake & Hieda in [2] used a 3D Finite Element Method (3DFEM), the error calculation and new parameter selection is performed by using the secant method. The method has only been used for elastic ground models, nevertheless it enables prediction of mechanical characteristics of the material ahead of the tunnel face.

The computational Program FLAC, based on the Finite Difference Method (FDM) is used by Fakhimi et al. [4]. The error calculation was performed by the least square method while the correction for the input parameters was done by an expert. Despite some data collection problems, that the authors had to face in this specific project (Resalat Tunnel), good approximations were obtained.

Amusin et al. [10] used the computational program NEDRA based on theoretical empirical method. The proposed back analysis method has three empirical correction factors “ $X_i$ ” based on the measured displacements, each factor has to be multiplied with a specific parameter:  $X_1$  with “ $Q$ ” (in-situ stresses),  $X_2$  with “ $R$ ” (rock mass strength) and  $X_3$  with “ $\psi$ ” (creep coefficient). The iteration of this procedure leads to the output parameters.

A combination of the observational method and computational algorithms is used by Shunsuke et al. [6]. The so called Direct Back Analysis Program (DBAP) allows the engineer to roughly approximate ground parameters by using a linear elastic material to associate measured displacements and normalized in-situ stress components. By using this program one can calibrate the model; the second



algorithm is the so called Back Analysis of Non-Linear Strains for Jointed rock mass in Incremental form (BANSJI). Using this algorithm the designer can achieve a more realistic approach to the rock mass behavior. A significant feature of this procedure is the implementation of the observational method, which enables not only to calibrate the parameters but also the model itself.

Oreste in [5] and [11] utilizes the convergence-confinement method and the secant method for displacement prediction and the least square method is used to calculate the error. The approach proposed by Oreste for the DBBA uses vectorial formulation, the gradient method and successive approximations, through these techniques the new input parameters are recalculated. There are pros and cons regarding the convergence-confinement method. On the one hand certain parameters can make the back analysis very long or even impossible if numerical methods are implemented instead of the convergence-confinement method and on the other hand unique solutions are rarely obtained and depend on amount and type of uncertain parameters.

The so called Support Vector Machines (SVM) and numerical analysis with FEM and a Sequential Minimal Optimization (SMO) learning algorithm were developed by Xia-Ting et al. [3] for the Three Gorges Project in China. As written by the authors the SMO is a simple algorithm that can solve quadratic programming problems without any extra matrix storage and without using numerical quadratic programming optimization steps at all. This makes the computational requirements low, allowing the user to execute multiple calculations in a short period of time and to use the numerical analysis by the means of FEM only for verification purposes. This method is proposed for large projects where enough data is gathered for the genetic algorithms to evolve.

In [12] Zhang et al. use the three-dimensional finite element pattern technique (3-D FEPT) to analyze the measured displacements near the tunnel face. The model proposed by the authors is aimed on searching not more than two parameters, the

horizontal stress ( $P$ ) and the Rock mass modulus ( $E$ ). Taking this into account they implemented two techniques for the parameter's search. The first one is a direct search technique, where continuous search of  $P$  is done through DBBA and the parameter  $E$  is calculated from the final  $P$  estimation. The second is the damping least square technique, which compares the field measured displacements with those obtained from the DBBA. Back-analyzed results of  $E$  and  $P$  can then be optimized by minimizing the error function. Minimization requires a great amount of calculation by the 3-D FEM making the model time-consuming.

## 2. Inntal tunnel description

[13] The Inntal tunnel is one of the main components from the “Innsbruck freight railway bypass”. This bypass is a 14.8 km double-track electrified rail line, which connects the so called lower Inn tall railway with the Brenner railway, by-passing Innsbruck. It was opened on May 29<sup>th</sup> 1994 and has as major components:

- The Fritzens-Wattens 1 junction,
- A 488 meter-long bridge over the Inn river,
- The Innsbruck 1 junction and
- 12,696 meter-long Inntal tunnel.
  - Tunnel approx. costs €120 million to build



**Photograph 1.: Inntal tunnel\_Excavation in heavily squeezing rock<sup>1</sup>**

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<sup>1</sup> Photographer: Prof. DI Dr. Wulf Schubert

The Inntal tunnel is a two line tunnel between Inntal and Wipptal, its construction started in September 1989, by December 1992 the two excavation fronts broke through and the tunnel was completed in July 1993. After track laying, wiring of the overhead electrical line and the installation of signaling in the tunnel operations started in May 1994

The tunnel was built using the New Austrian Tunneling method. The distance between the tracks is 4.70 m, corresponding with high-speed lines and in contrast to other new tunnels, it is not built with slab tracks but instead is equipped with conventional ballasted tracks and concrete sleepers. The excavated cross-section goes from 95 to 108 square meters depending on the lining.

## 3. Parameters and data obtained in the tunnel

### 3.1. Analyzed cross sections

For the present master thesis a total of nine cross sections (see Fig. 2 and Table 1) were analyzed. The cross section selection was based on the final measured displacements and ground homogeneity. All analyzed cross section are modeled having a  $113.1\text{-m}^2$  cross section (6 m tunnel radius).

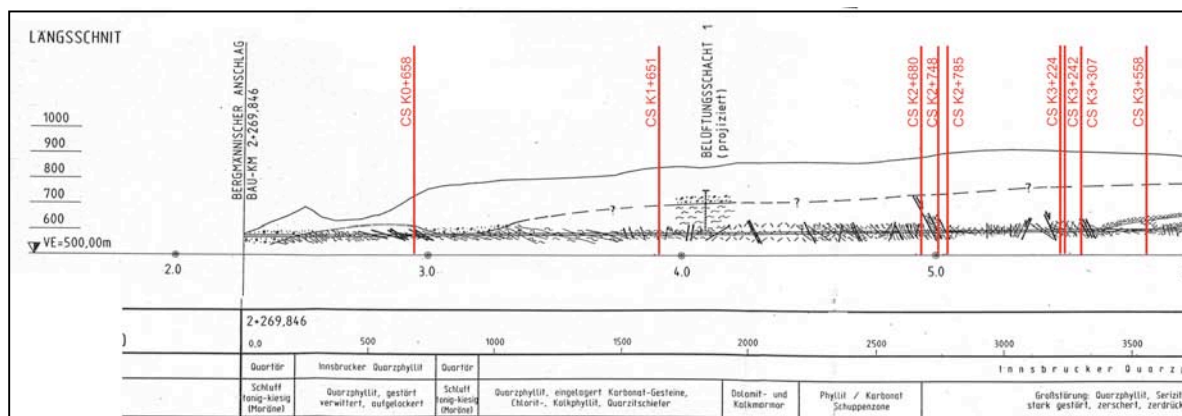


Fig. 2: Inntal tunnel longitudinal section

| Csection | Geology  |
|----------|--|
| 0+685    | Quarzphyllite, disturbed, weathered, loose - low permeability - Faulted (mylonite)           |
| 1+651.4  | Quarzphyllite, embedded with carbonate rock, Chloritphyllite, limephyllite, schist quarzitte |
| 2+680    | Phyllite / carbonate rock scalezone  |
| 2+748    |  |
| 2+785    |  |
| 3+224    | Masive Faults: Quarzphyllite, Serizitphyllite, Chloritphyllite, schist quarzitte disturbed,  |
| 3+242    | pulverized - brittle - partially plasticized - low permeability                              |
| 3+307    |  |
| 3+558    |  |

Table 1: Geological description from the analyzed cross sections

Although Kainrath et al. [14] recommend the convergence-confinement method for great depths and/or poor quality rock masses, the cross section 1+651.4 with relative low overburden inducing small displacements was analyzed for comparison reasons.

As written before the Inntal tunnel was constructed using the NATM, which assigns characteristic support systems based on rock mass behaviors along the tunnel axis. Therefore, often the same support system was found for more than one cross section. Table 2 presents the support systems installed in each cross section, Table 3 shows the properties for each support material.

| Csection | Displac.<br>(cm) | Displac.(2)<br>(cm) | Overburden<br>(m) | Shotcrete         | Bolts   |                      |        |               | Steelribs (Profiles) |                       |
|----------|------------------|---------------------|-------------------|-------------------|---------|----------------------|--------|---------------|----------------------|-----------------------|
|          |                  |                     |                   | thickness<br>(mm) | Type    | long. Spacing<br>(m) | #Bolts | Length<br>(m) | Type                 | Steel. Spacing<br>(m) |
| 0+685    | 14.8             | 6.7                 | 180-190           | 200               | SN      | 1.5                  | 9      | 3.9-6         | HEA 120              | 1.5                   |
| 1+651.4  | 7.6              | 3.2                 | 340-350           | 200               | SN      | 2.2                  | 9      | 3.9-6         | HEA 120              | 2.2                   |
| 2+680    | 24.5             | 14.0                | 380               | 200               | SN      | 1                    | 10     | 6             | HEA 120              | 1                     |
| 2+748(1) | 75.0             | 41.4                | 400               | 200               | SN      | 1                    | 29     | 8             | Alpine               | 1                     |
| 2+785(1) | 58.6             | 33.8                | 410-420           | 200               | SN      | 1                    | 29     | 8-6.0B        | Alpine               | 1                     |
| 3+224(1) | 81.2             | 57.8                | 405-415           | 200               | SN      | 1                    | 22     | 6.0-8.0       | Alpine               | 1                     |
| 3+242(1) | 86.0             | 52.7                | 405-410           | 200               | SN      | 1                    | 22     | 6.0-8.0       | Alpine               | 1                     |
| 3+307(1) | 69.5             | 41.9                | 395-405           | 200               | SN      | 1                    | 22     | 6             | Alpine               | 1                     |
| 3+558(1) | 29.3             | 17.3                | 385-395           | 200               | GEWI-SN | 1                    | 29     | 8-6.0B        | Alpine               | 1                     |

(1) Open displacement gaps

(2) Non time dependent displacements

**Table 2: Installed support and registered displacements for the analysed cross section**

| Shotcrete            |                    |               |                     |                    |                   |               |
|----------------------|--------------------|---------------|---------------------|--------------------|-------------------|---------------|
| Type                 | Elasticity Modulus |               |                     | Poisson            |                   |               |
|                      | (GPa)              |               |                     |                    |                   |               |
| Wet                  | 5 - 20.            |               |                     | 0.25               |                   |               |
| Steelribs (Profiles) |                    |               |                     |                    |                   |               |
| Type                 | Steel. Spacing     | Flange width  | Depth steel section | Cross-section area | Moment of inertia |               |
|                      | (m)                | (mm)          | (mm)                | (m <sup>2</sup> )  | (m <sup>4</sup> ) |               |
| HEA 120              | 1.5                | 120           | 114                 | 2.53E-03           | 2.31E-06          |               |
| Alpine               | 1                  | 124           | 105.5               | 3.70E-03           | 6.16E-06          |               |
| Bolts                |                    |               |                     |                    |                   |               |
| Type                 | Bar. Diameter      | Hole Diameter | E. Moduli Bar       | E. Moduli Grout    | Poisson           | Ultimate Load |
|                      | (m)                | (m)           | (GPa)               | (GPa)              |                   | (MN)          |
| SN                   | 0.025              | 0.052         | 210                 | 25                 | 0.15              | 0.3           |

**Table 3: Support material properties**

Displacements shown in Table 2 are the result of systematic measurements of the convergences for several days by means of electronic total stations and reflective targets. This system satisfies accuracy requirements and enables the evaluation of displacements in three-dimension. There are numerous ways for graphically displaying and interpreting the behavior along the tunnel surface. For this purpose the program Geofit, developed by 3G GRUPPE Geotechnik Graz was used. Fig. 3 shows a typical measured data analysis done by Geofit. The black dots represent the measured data on site and the blue and red lines are the fitted data for the top heading and bench respectively. The  $u_{eq}$  value (see Fig. 6) is represented by the end of the red line, where no further displacements are registered. Regarding the equilibrium point  $u_{eq}$  it is worth mentioning that time dependent displacements are not taken into account for the present study, for this reason only displacements up to 80m of distance to the face are considered.

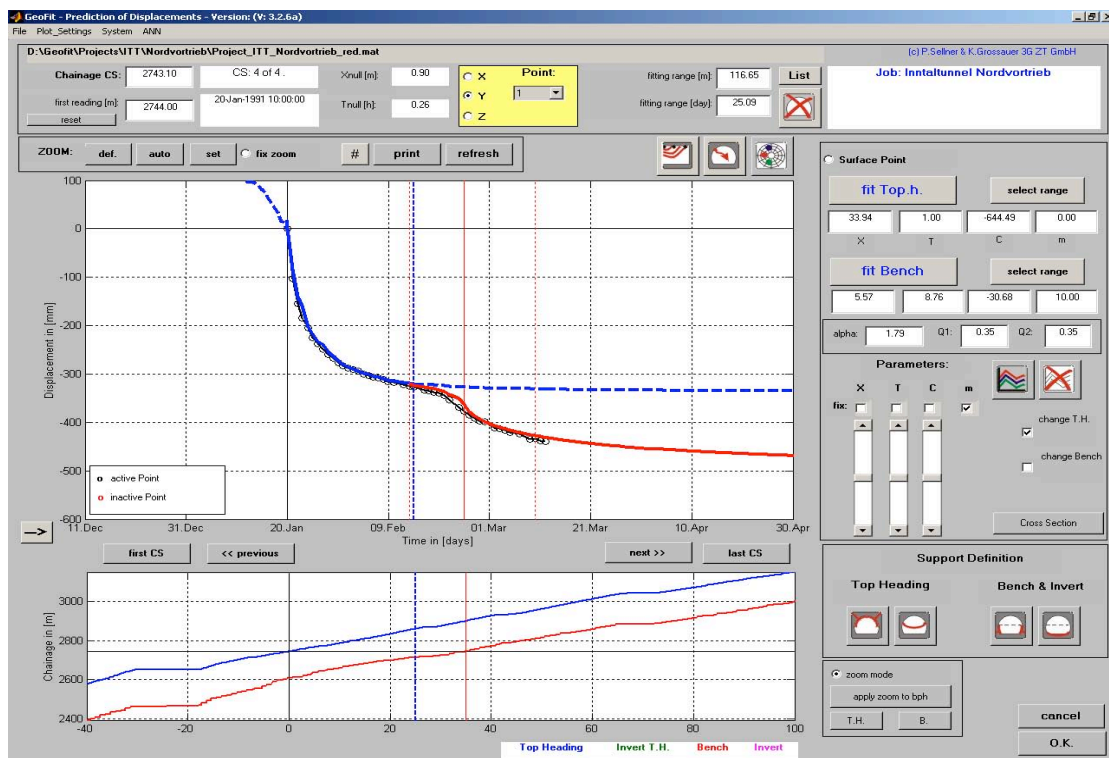


Fig. 3: Geofit screen shot, Software for displacement prediction\_Cross section k2+743\_\_Open gaps

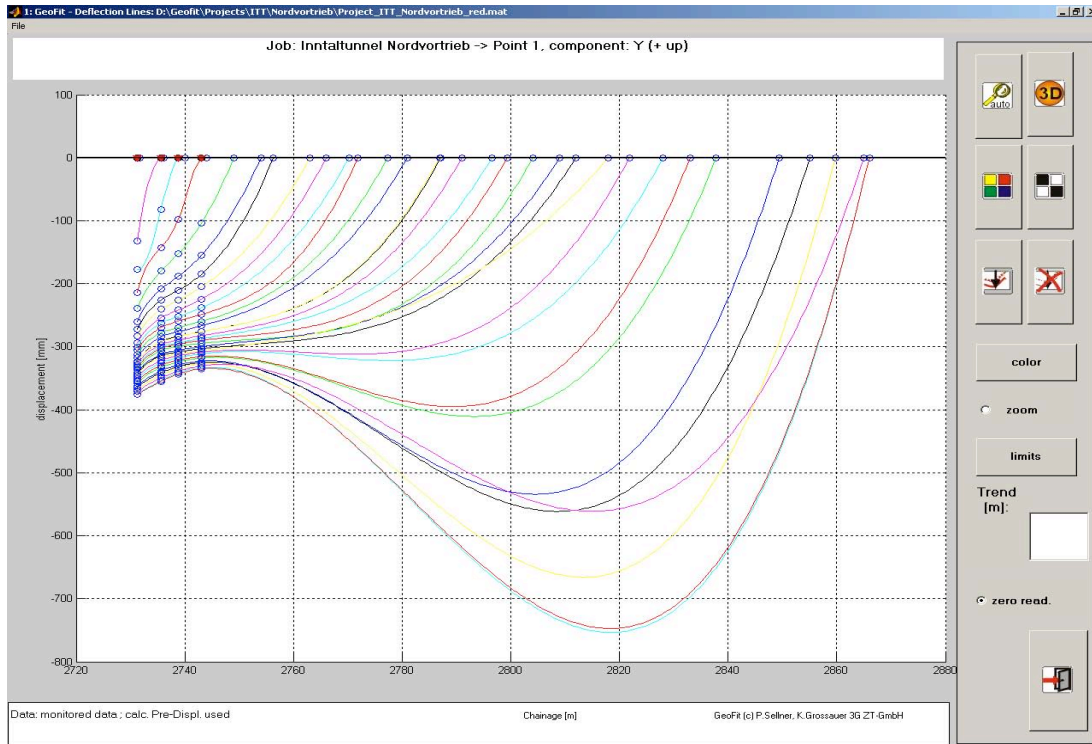


Fig. 4: Geofit Trendlines plot\_Chainages K2+731.2 to K2+743.1

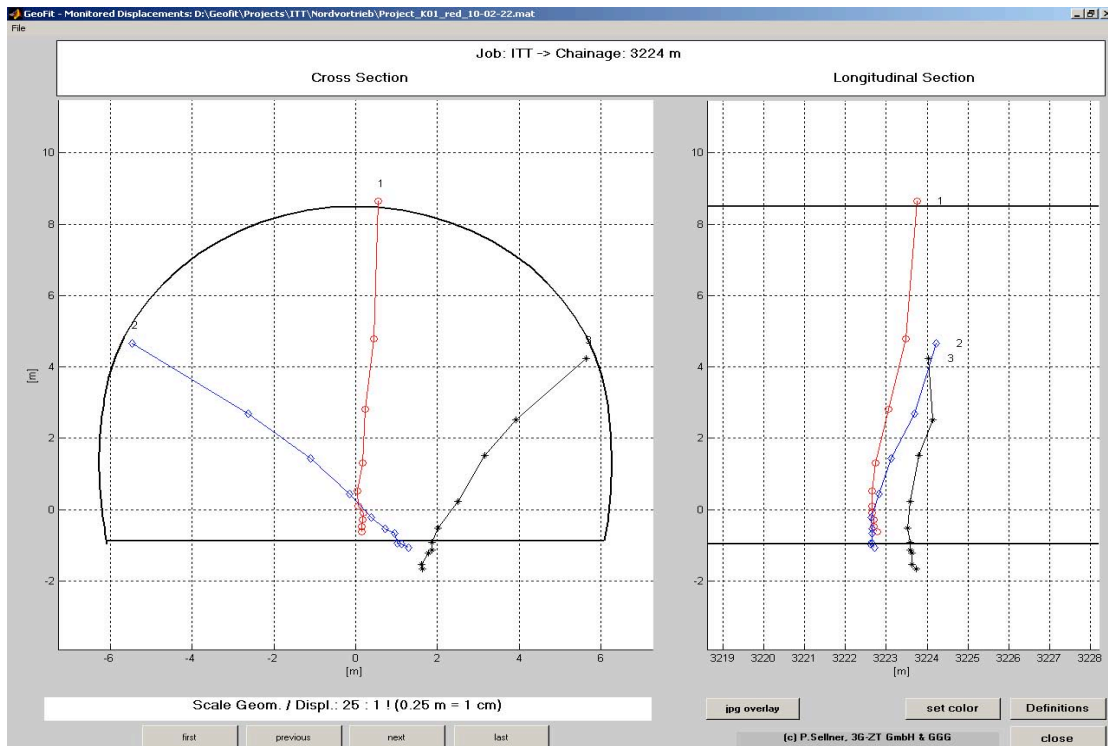


Fig. 5: Geofit's Cross- and Longitudinal-section\_Cross section k3+224\_open Gaps



Fig. 4 presents the development of the crown settlements between the chainages K2+731.2 and K2+743.1. Blue dots show the systematic measurements in the top heading for each cross section in between this chainages. The red path in Fig. 5 presents the crown displacements, which are used for the present study.

## 4. Proposed model for back analysis

### 4.1. Model overview

To carry out the back analysis, data regarding displacements and support system is necessary.

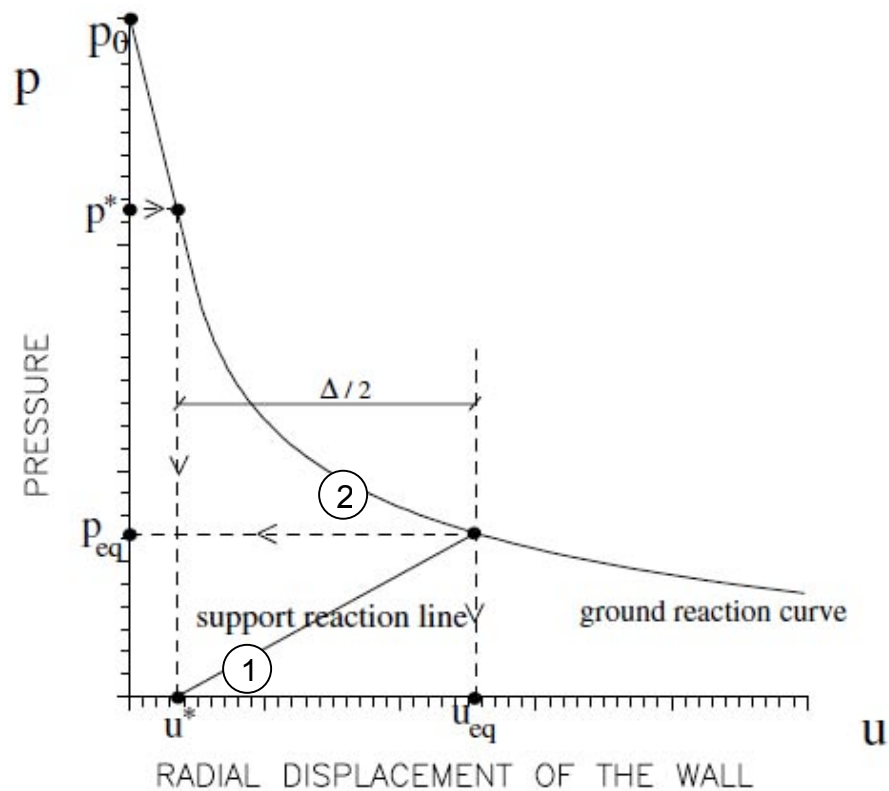


Fig. 6: Convergence-Confinement Method [5]

The proposed back analysis has the following procedure:

- 1) Determination of  $E_b$ ,  $c_b$ ,  $\varphi_b$  and  $E_t$ ,  $c_t$ ,  $\varphi_t$

Where: the sub index b and t refer to bottom and top respectively and will limit the analysis range.

- 2) Determination of the GRC for  $E$ ,  $c$ ,  $\varphi$  according to Feder & Arwanitakis [1] formulation see curve 2 Fig. 6.

Where:  $E_1 = E_b$ ,  $c_1 = c_b$  and  $\varphi_1 = \varphi_b$  for the first analysis and,

$E_n = E_t$ ,  $c_n = c_t$  and  $\varphi_n = \varphi_t$  for the last analysis

- 3) Calculation of pre-displacements after Hoek & Carranza-Torres [15] for the support installation (see  $u^*$  in Fig. 6.)
- 4) Determination of the support characteristic curve (given by the support system installed) see curve 1 Fig. 6.
- 5) Determination of the equilibrium pressure point  $u_{eq}$ . see Fig. 6.
- 6) Comparison between  $u_{eq}$  and the final measured displacements - Error calculation (R).
- 7) When the calculated error (R) is smaller than the admissible error ( $R_{adm}$ ), the values of  $E$ ,  $c$  and  $\varphi$  for the specific GRC are saved in a matrix.
- 8) The new input parameters are calculated as following:  
 $E_i = E_{i-1} + E_{\Delta}$  and so on for  $c$  and  $\varphi$  values  
Delta is the increment value, calculated based on the partition given by the user.
- 9) The same procedure goes on until  $E_t$ ,  $c_t$  and  $\varphi_t$  values are reached

The Flow chart from Fig. 7 summarizes the procedure.

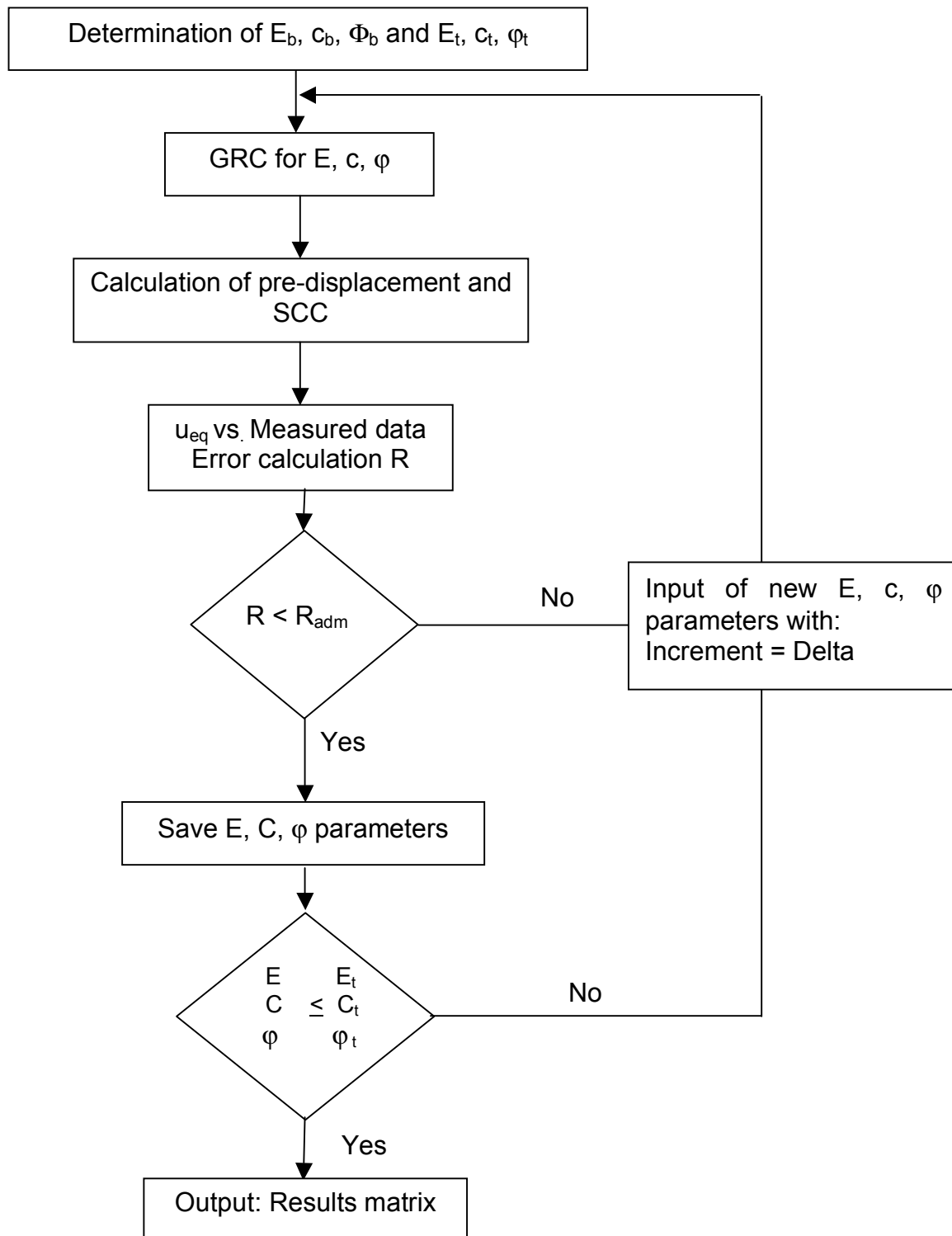


Fig. 7: Flow Chart Proposed Back Analysis

One has to be careful when making the initial assumption of  $E_b$ ,  $c_b$ ,  $\phi_b$  and  $E_t$ ,  $c_t$  and  $\phi_t$  hence they are not arbitrary values but rather have to be selected based on experience. This is due to the fact that mathematically speaking, it is possible to have combinations that fulfill the admissible error, but such combinations do not exist in most common rock masses.

It is worth mentioning that unlike [2], [3], [6], [9], [10] and [12] principal stresses are not calculated through back analysis but considered as known and estimated as a function of the overburden having  $K_0=1$ .

## 4.2. Model Basics

### 4.2.1. Ground Reaction curve (GRC)

The Convergence-Confinement method is a procedure that allows the calculation of the load imposed on a support installed behind the face of a tunnel. It is a practical tool but some considerations have to be taken into account. For the analytical solution delivered by the model used in the present study the following assumptions were made:

- 2D plate of infinite extend
- All deformations occur on a plane perpendicular to the tunnel axis
- Circular opening
- Homogeneous rock mass
- Side pressure coefficient  $K_0=1$ , (uniform stress field)
- No construction sequences
- Time-dependent weakening is not considered

The GRC was made according to the formulation from Feder & Arwanitakis [1]. In his research he stated that the final deformation for a circular tunnel has three different components: an elastic one, a plastic one and a volume increase in the plastic zone.

In the first part of Feder & Arwanitakis [1] present a formulation to mathematically describe the stress field for Mohr Coulomb material parameters, for a circular opening subjected to a uniform far-field (i.e. hydrostatic field) stress and uniform internal pressure, an example of this is shown in Fig. 8.

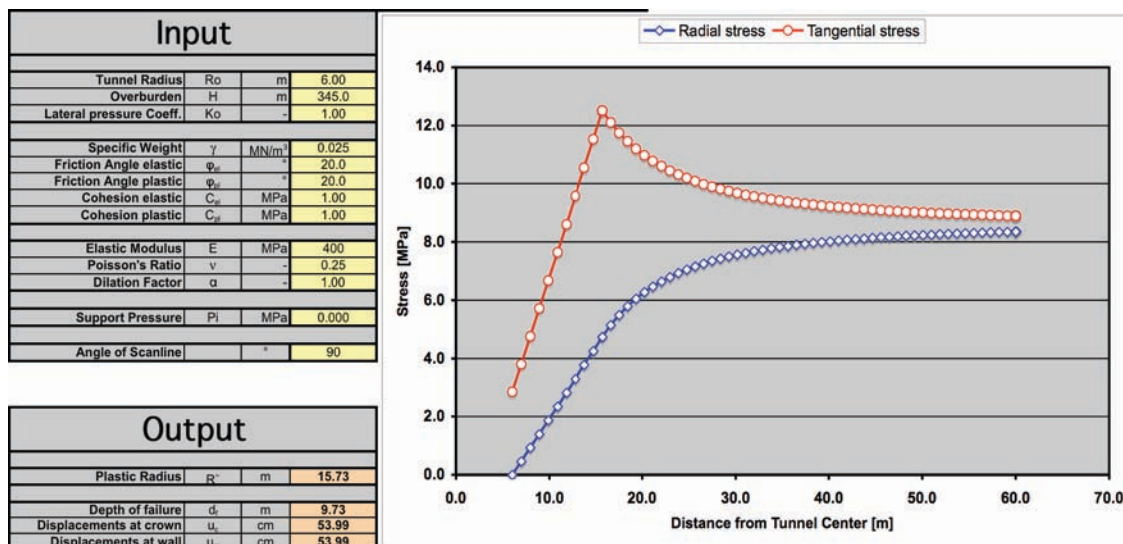


Fig. 8: Feder & Arwanitakis [1] stress field for a circular tunnel  $K_o=1$

In order to construct the GRC based on the formulation of Feder & Arwanitakis [1] one has to gradually change the inner support pressure  $P_i$  as follow:

1. Set  $P_{i\_max} = \gamma * H = P_o$ , as seen in Fig. 9 Model.
2. Gradually reduce the Internal pressure, up to a value  $P_{i\_min}=0$  (see Fig. 9. Step 2: No internal pressure), by doing this the analysis remains on the tunnel surface, as it is required for the GRC calculation. Analyzing equilibrium on one point of the tunnel intrado.

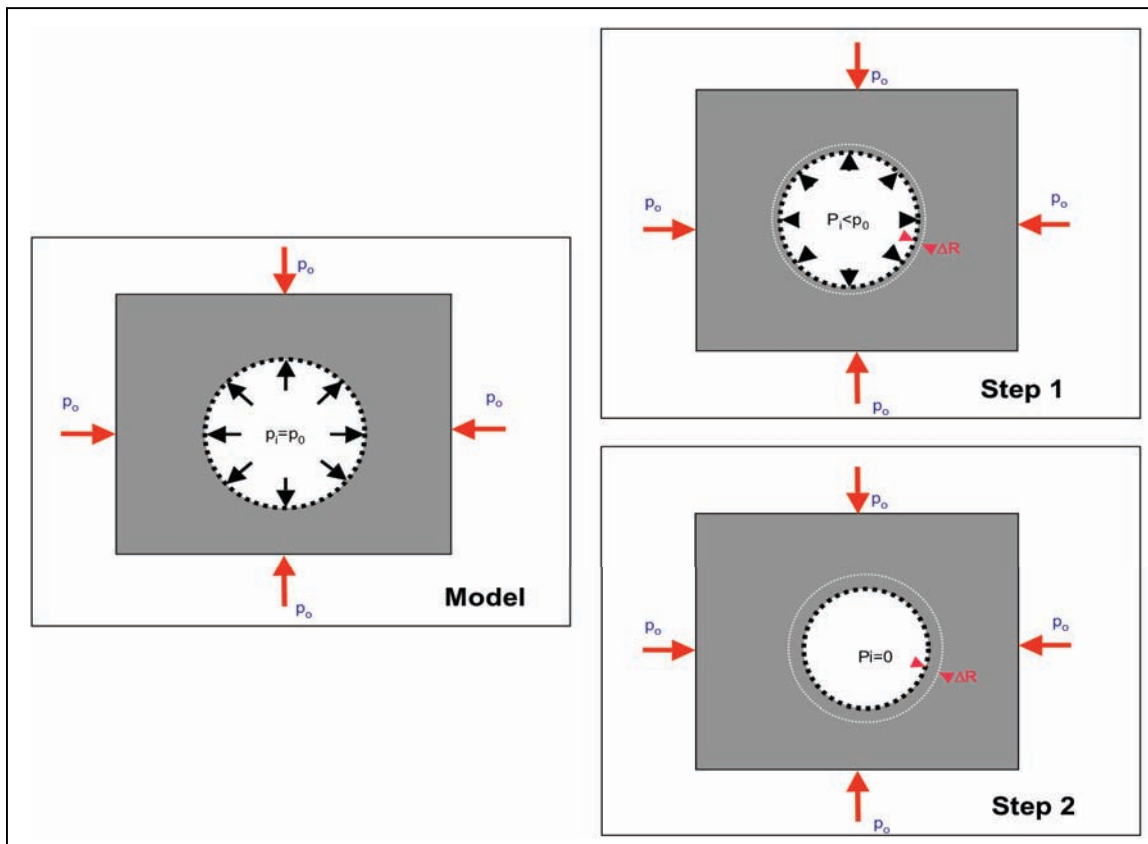


Fig. 9: GRC based on the formulation from Feder & Arwanitakis [1]

As explained before there are three main stress states in the formulation from Feder & Arwanitakis [1], for this reason for every  $P_i$  value a new Plastic radius has to be calculated and then the stress state verification can take place. Once the stress state is calculated the formulas for the specific scenario have to be implemented resulting on the given stress value  $P_i$  and a calculated displacement value  $u$ .

#### 4.2.2. Ground Reaction Curve with improvement intervention

Improvement interventions refer to the use of grouted bolts, which themselves are not considered to establish any radial support pressure on the rock surface, therefore cannot be calculated as simple bars or cables. Forces in a grouted bolt have to be calculated depending on the rock mass deformation, these forces do not develop in a specific point but throughout the whole bar.

Authors have faced the problem by describing the bolt/ground interaction. For instance Indraratna and Kaiser in [16] and Oreste in [17] presented a solution based on a convergence control and the congruence of bolt-ground displacements respectively. Both authors modify the general elasto-plastic solution for the design of underground openings and extend it to accommodate the influence of bolt/ground interaction, size of opening and the bolt pattern on yielding and tunnel wall displacements.

For the present thesis expression (1) introduced in the literature by Grasso and Pelizza and mentioned by Oreste [17] was used. It shows the effect of the rock bolting on improving of the yielding zone around the tunnel in terms of effective cohesion.

$$c^* = c + \frac{1 + \sin \varphi}{2 \cos \varphi} \Delta \sigma_3 \quad (1)$$

where  $\Delta \sigma_3$  is the confinement produced by the action of the grouted bolts, equal:

$$\Delta \sigma_3 = \frac{T_m}{S_T + S_L} \quad (2)$$

where  $T_m$  is the mean force along each bolt,  $S_T$  and  $S_L$  are transversal and longitudinal spacing of the bolting pattern.

The mean force value was calculated using the finite difference calculation procedure proposed by Oreste [17]. Oreste's method is divided in 7 main steps:

1. Setting out a value of  $|t_B|$  (shear stress between the bolt and the rock in the anchorage zone.  $|t_B|$  is calculated based on the  $T_0$  value which is the discharge of the bolt onto the tunnel walls and the  $T_{max}$  value which is the Maximum traction force in the bolt that will later be recalculated.

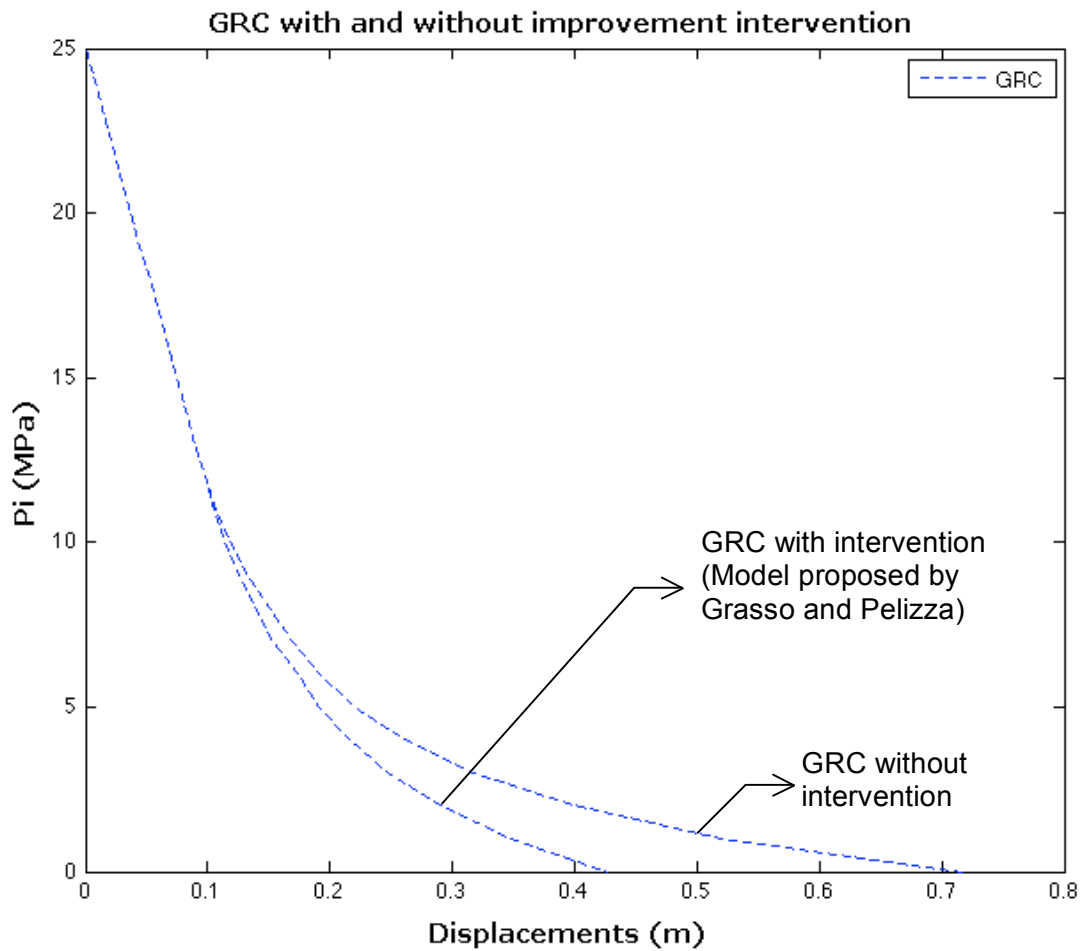


2. Determination of the circumferential stress and of the radial displacement in each point of the bolt (at a known distance from the centre of the tunnel) with variation of radial stress in the same point
3. Calculation of stresses and strains in the reinforced rock, until the group of values from circumferential stress, radial displacement and plastic radius is calculated for each term
4. Selection of the group of values for which the circumferential stress is more approximated to the given internal pressure of the tunnel perimeter
5. Determination of stresses and displacements in the reinforced rock for the distance  $R_i$
6. Congruence verification between the deformation of the rock and the deformation of the bolt
7. Estimation of the  $T_{\max}$  value

Once the  $T_{\max}$  value is calculated for the found shear stress  $|t_B|$  the  $T_{\text{mean}}$  value can be calculated by means of expression (3):

$$T_{\text{mean}} = \frac{T_{\max}}{2} \left[ 1 + \chi \left( \frac{1}{2} - \frac{\eta}{L} \right) \right] \quad (3)$$

where  $\eta$  is the distance of the location of the maximum force from the median point of the bolt and  $\chi$  is the ratio between  $T_0$  and  $T_{\max}$ , from the numerical modeling presented by Oreste [17], one can conclude that  $\eta$  and  $\chi$  vary in a narrow interval, and the mean values  $\eta=1/3L$  (where  $L$  is the length of the bolt) and  $\chi=1/3$  can be taken when a perfect constrain is obtained on the bolt head.



**Fig 10: Ground reaction curve with and without improvement intervention after Oreste [17]**

Fig. 10 shows Oreste's approach implemented in Matlab and an example of the ground reaction curve modification

There are two main remarks from Fig. 10:

1. Since it is assumed that by the time the bolts are installed elastic displacements have taken place, it is visible that the GRC modification only occurs in the plastic zone.

2. The original formulation made by Oreste in [17] had to be modified. The reason for that was the great reduction of displacements. Several calculations were made and it could be seen that, when significant displacements are taking place (i.e., Displacements in Inntal tunnel) the original formulation overestimates ground conditions. Through the calculations one could notice that the tensile force  $T_{max}$  in each bolt was not limited carrying out the mentioned overestimation. The problem was easily fixed by establishing a max. tensile load of 300 kN. The mentioned value was selected taking into account the diameter and type of bolts used in the Inntal tunnel.

#### 4.2.3. Support Characteristic Curve

The principles of the SCC are well explained by Carranza & Fairhurst in [18] and by Stille et al. in [19] the original formulation has Hoek & Brown (1980) and Brady & Brown (1985) as authors. The principle for the construction of the SCC is based on the elastic relationship between the applied stress  $P_s$  and the resulting closure  $u_r$  for a unit length section of the support in the direction of the tunnel (longitudinal spacing). An elastic stiffness of the support “ $K_s$ ” ought to be determined. The elastic part see curve 1 Fig. 6 of the SCC can be calculated after the following expression:

$$P_s = K_s * u_r \quad (4)$$

The plastic part of the SCC is defined by the maximum pressure  $P$  that the specific support system can bear before collapse.

#### 4.2.3.1. Shotcrete or concrete rings

Considering the closed ring of shotcrete or concrete represented in Figure 11, the maximum pressure provided by the support is:

$$p_s^{\max} = \frac{\sigma_{cc}}{2} \left[ 1 - \frac{(R-t_c)^2}{R^2} \right] \quad (5)$$

The elastic stiffness is:

$$K_s = \frac{E_c}{(1-\nu_c)R} \left[ \frac{R^2 - (R-t_c)^2}{(1-2\nu_c)R^2 + (R-t_c)^2} \right] \quad (6)$$

where:

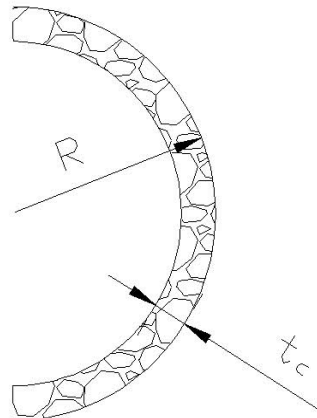
$\sigma_{cc}$  is the unconfined compressive strength of the shotcrete or concrete [MPa];

$E_c$  is Young's Modulus for the shotcrete or concrete [MPa];

$\nu_c$  is Poisson's ratio for the shotcrete or concrete;

$t_c$  is the thickness of the ring/shotcrete [m];

$R$  is the external radius of the support [m]



**Fig. 11: Schematic representation of sections of shotcrete/concrete rings adapted from Brady and Brown (1983).**

#### 4.2.3.2. Steel profile sets

Regarding the Steel profiles a change had to be carried out due to the fact that the formulas presented by the authors supposed, that the profiles are tightened against the rock by using wood blocks, which is a common practice in North and Latin America. Common practice in Europe is to set the profiles directly against the shotcrete. Comparison between wood blocks and shotcrete were evaluated and the conclusion is that the contribution from the wood blocks in terms of maximum pressure is too low. Therefore the part of the equation where block sets are considered does not form part of the present study.

Considering steel sets spaced a unit length apart in the direction of the tunnel axis and tightened against the rock by shotcrete the maximum pressure that the system can sustain is:

$$p_s^{\max} = \frac{3 \sigma_{ys}}{2 S R} + \frac{A_s I_s}{3 I_s + D A_s [R - 0.5 D]} \quad (7)$$

The elastic stiffness is:

$$K_s = \frac{E_s A_s}{S_c R^2} \quad (8)$$

Where:

- B is the flange width of the steel set [m];
- D is the depth of the steel section [m];
- $A_s$  is the cross-sectional area of the section [m<sup>2</sup>];
- $I_s$  is the moment of inertia of the section [m<sup>4</sup>];
- $E_s$  is Young's modulus for the steel [MPa];
- $\sigma_{ys}$  is the yield strength of the steel [MPa];

- S is the steel set spacing along the tunnel axis [m];  
 R is the tunnel radius [m].

#### 4.2.3.3. UngROUTED bolts and cables

The sketches in Fig. 12 represent mechanically anchored bolts installed in the rock-mass surrounding a circular tunnel of radius R. Assuming that the bolts are equally spaced in the circumferential direction, the maximum support pressure provided by this support system is:

$$p_s^{\max} = \frac{T_{bf}}{S_c + S_l} \quad (9)$$

The stiffness is:

$$\frac{1}{K_s} = S_c S_l \left[ \frac{4l}{\pi d_b^2 E_s} + Q \right] \quad (10)$$

Where:

- $d_b$  is the bolt or cable diameter [m];  
 $l$  is the free length of the bolt or cable [m];  
 $T_{bf}$  is the ultimate load obtained from a pull-out test [MN];  
 $Q$  is a deformation-load constant for the anchor and head [m/MN];  
 $E_s$  is Young's Modulus for the bolt or cable [MPa];  
 $S_c$  is the circumferential bolt spacing [m];  
 $S_l$  is the longitudinal bolt spacing [m].

The equation presented for the non grouted bolts supposes that the reaction forces developed by the bolt are concentrated at the ends of the bar; therefore the equation should not be applied in the case of grouted bolts, for which the load transfer is distributed throughout the length of the shank.

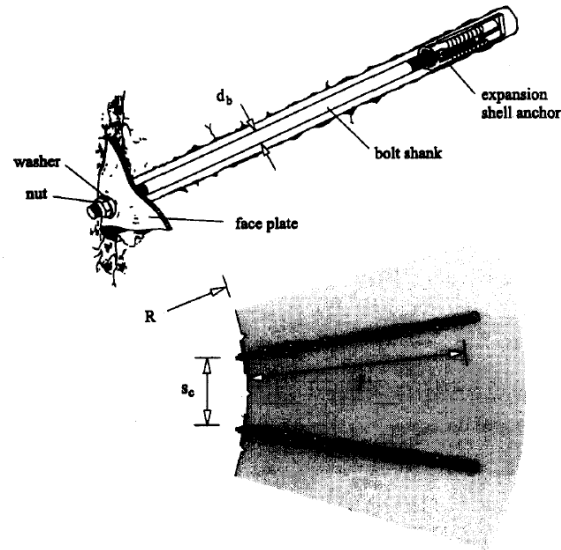


Fig. 12: Ungrouted mechanical-anchored bolt (adapted from Stillborg 1994 and Hoek and Brown 1980).

#### 4.2.3.4. Lining stress controllers

[20] The SCC for integrating yielding elements can be approximated by a bi-linear relationship (or as a combination of bi-linear relationships). The initial branch of resistance mobilization is of great importance since the young shotcrete still has a very low strength. The mobilized support resistance  $P_A$  in this phase can be derived with Equation 11.

$$P_A = \frac{2u_{Ausbau}\pi}{R \left[ \frac{2R\pi - n_{St}l_{St}}{E_{SpB}t_{SpB}} + \frac{n_{St}}{K_{St}} \right]} \quad (11)$$

where:

- $u_{Ausbau}$  is the radial displacement of the support [m];
- $n_{St}$  is the number of yielding elements in the cross section;

|           |  |
|-----------|--|
| $l_{St}$  | is the length of the yielding element gap in the shotcrete lining [m]; |
| $E_{SpB}$ | is the secant Young's modulus of the young shotcrete [MPa];            |
| $t_{SpB}$ | is the thickness of the shotcrete shell [m];                           |
| $K_{St}$  | is the initial stiffness of the yielding element [kN/m];               |
| $R$       | is the tunnel radius [m].  |

As recommended by [20] Radonicic, Schubert and Moritz, a secant Young's modulus of 5,000 MPa should be assumed, since the relationship shown in Equation 11 would give unsafe results if the shotcrete stiffness was assessed too low. The radial displacement at which the yielding occurs is calculated as following (Equation 12):

$$u_{pl} = u_0 + \frac{1}{2\pi} \left[ \Delta l_{pl} n_{St} + \frac{F_{pl}}{E_{SpB} t_{SpB}} (2R\pi - l_{St} n_{St}) \right] \quad (12)$$

where

- $F_{pl}$  is the force in the yielding element when the yield is reached [kN];  
 $u_{pl}$  is the shortening when the yield is reached [m];

The support resistance mobilized in this phase is calculated from the yield load of the elements (Equation 13).

$$P_{A,pl} = \frac{F_{pl}}{R} \quad (13)$$

Most yielding elements feature a second increase in the mobilized loads after a certain compressive displacement  $\Delta l_{AN}$  is reached. By using simple geometrical considerations, the radial displacement  $u_{AN}$ , at which the support resistance curve starts to increase again, can be calculated through equation 14.



$$u_{AN} = u_0 + \frac{\Delta l_{AN} 2\pi}{n_{St}} \quad (14)$$

Since the shotcrete is already cured at this moment, the compressive strain increments in this phase can be neglected. Thus, the support resistance can be calculated in a straightforward manner, and added to the already mobilized resistance from the plastic phase by means of equation 15.

$$p = p_{A,pl} + \frac{(u_{Ausbau} - u_{AN}) K_{St,AN}}{n_{St}} \quad (15)$$

where:

$K_{St,AN}$  is the stiffness of the yielding element in the phase of load increase.

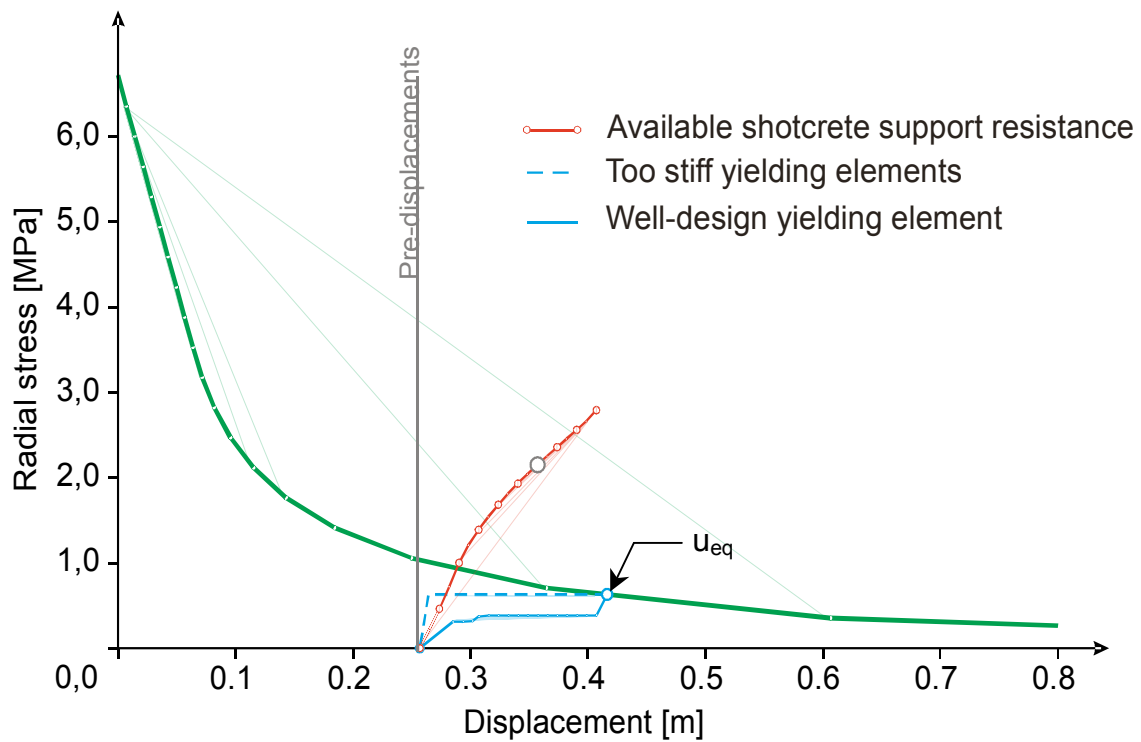


Fig. 13: GRC and SCC for Lining Stress Controllers\_Taken from [20]

The equilibrium displacement  $u_{eq}$  (see Fig. 13) is given by intersecting the ground convergence curve with the support resistance curve obtained by applying the equations above.

#### 4.2.4. Pre-displacement calculation

Hoek et al. in [21] and Carranza & Fairhurst in [18] presented Hoek's empirical best-fit relationship between radial displacements of the tunnel and distance to the face (see expression 16). Hoek's empirical approach was based on convergence measurements made in the Mingham Power Cavern project by Chern et al. (1998), these measurements were fitted into the following equation:

$$\frac{u_r}{u_r^M} = \left[ 1 + e \left( -\frac{x/R}{1.10} \right)^{-1.7} \right] \quad (16)$$

where:

- x is the distance to the tunnel face [m];
- $u_r^M$  is the maximal radial displacement [m];
- R is the tunnel radius [m];
- $u_r$  is the predicted displacement [m].

Based on Hoek's equation Carranza and Fairhurst made the following observations:

- The maximum radial displacement occurs at approximately 8 tunnel radii behind the face of the tunnel.
- The radial deformation is zero at approximately 4 tunnel radii ahead of the face.
- At the face itself, the radial displacement is approximately 30% of the maximum displacement value.

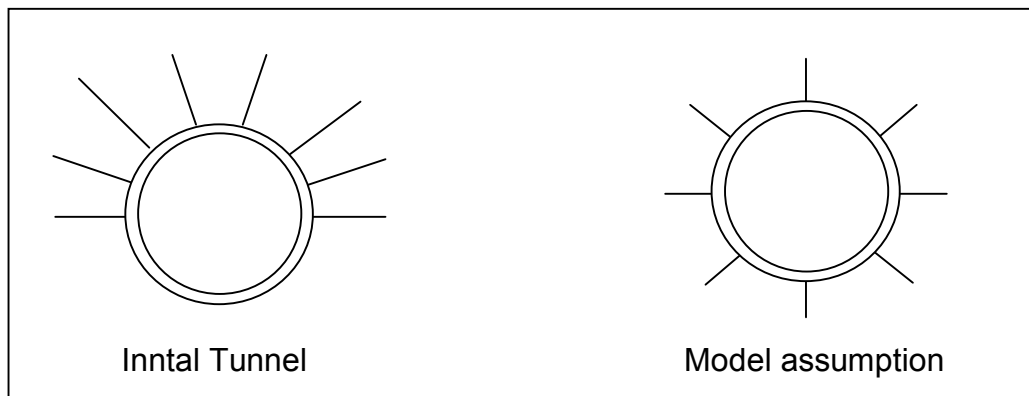
### 4.3. Model Shortcomings

#### 4.3.1. Ground Reaction Curve and Support Characteristic Curve

For the GRC construction the present study considers rock masses that satisfy Mohr Coulomb failure criteria, only peak values from  $E$ ,  $c$  and  $\phi$  are handled, post failure behavior is not considered.

The SCC in the model does not consider installation time and excavation sequences, it is assumed that the used support system for each cross section is installed at the same time. It is worth mentioning that minor changes have to be made in order to take these considerations into account, but due to the lack of information regarding installation timing this assumption was necessary.

The plastic part of the SCC in Figure 6 i.e., the horizontal segment, is defined by the maximum pressure that the support can accept before collapse, no post-failure consideration was made for the materials used as support.



**Fig. 14: Bolting distribution found on site and for the proposed model**

The time dependency of shotcrete in terms of strength is not included in the present model. Shotcrete is always considered as “young”. Therefore values in between 5 and 10 MPa were handled.

Bolting distribution in each cross section is assumed to be equidistant and bolts to have the same length. Fig. 14 shows an example of a bolting system (8 bolts) on a cross section.

Bolts installation is assumed to occur after elastic displacements have taken place, as seen in Fig. 10 the GRC is only modified on its plastic part.

As described in the introduction the presented model allows the user to select a range of Young’s modulus, cohesion and friction angles where the back analysis will take place. However these values have to be determined by the user based on experience, since it is possible to find combinations that are mathematically correct but are rarely found in rock masses.

### **4.3.2. Dilatancy**

Dilatancy is a major shortcoming of the presented model. As described by Alejano and Alonso in [22] difficulties associated “with a model that adequately reflects observed complete stress–strain curves have affected the possibilities of developing suitably valid approaches for handling post-failure strength behavior and dilatancy”, this mainly happens because problems in rock mechanics avoid failure and the inherent difficulty of calculating dilatancy.

The formulation from Feder & Arwanitakis [1] does not take into account dilatancy. Due to the fact that it plays an important role in rock mechanics where shear strains occur (i.e. along fault zones and discontinuities) further studies should be made regarding this matter. Setting dilatancy into the model would imply a change

in the whole GRC since dilatancy develops only as the deformation (displacements) process unfolds.

Further studies ought to be done regarding dilatancy influence on the grouted bolts behavior. For the present study dilatancy was set ( $\psi=0$ ), Oreste in [17] remarked dilatancy mayor role in the bolts performance since it only fully unfolds in a post-failure rock state.

#### 4.3.3. Consideration for the Inntal tunnel

A final consideration had to be made in order to handle the support design made for the Inntal tunnel where heavily squeezing rock was found. The support design in those areas involved the usage of the so called open displacement gaps as seen in Photograph 1. The model modification for this scenario was divided in two parts:

1. **Shotcrete contribution ratio:** Though, Pöttler in [23] carry out a study on shotcrete contribution by presence of open gaps, this approach was not included in the present study, mainly because parameters describing the interaction ground-shotcrete are not available. Nevertheless a simulation was performed on the program Phase<sup>2</sup>, developed by RocScience in order to find a shotcrete contribution ratio, which allows inferring the open gaps by minimizing the parameters of the closed shotcrete ring.

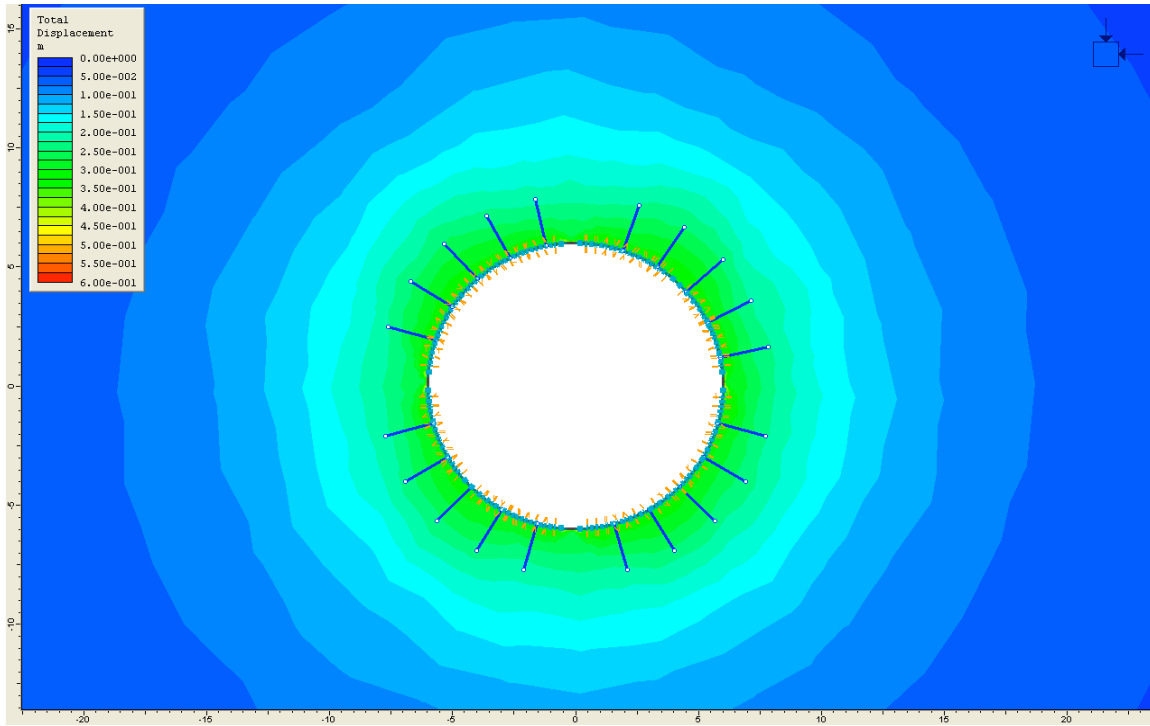


Fig. 15: Phase<sup>2</sup> displacements prediction\_Cross section with open gaps

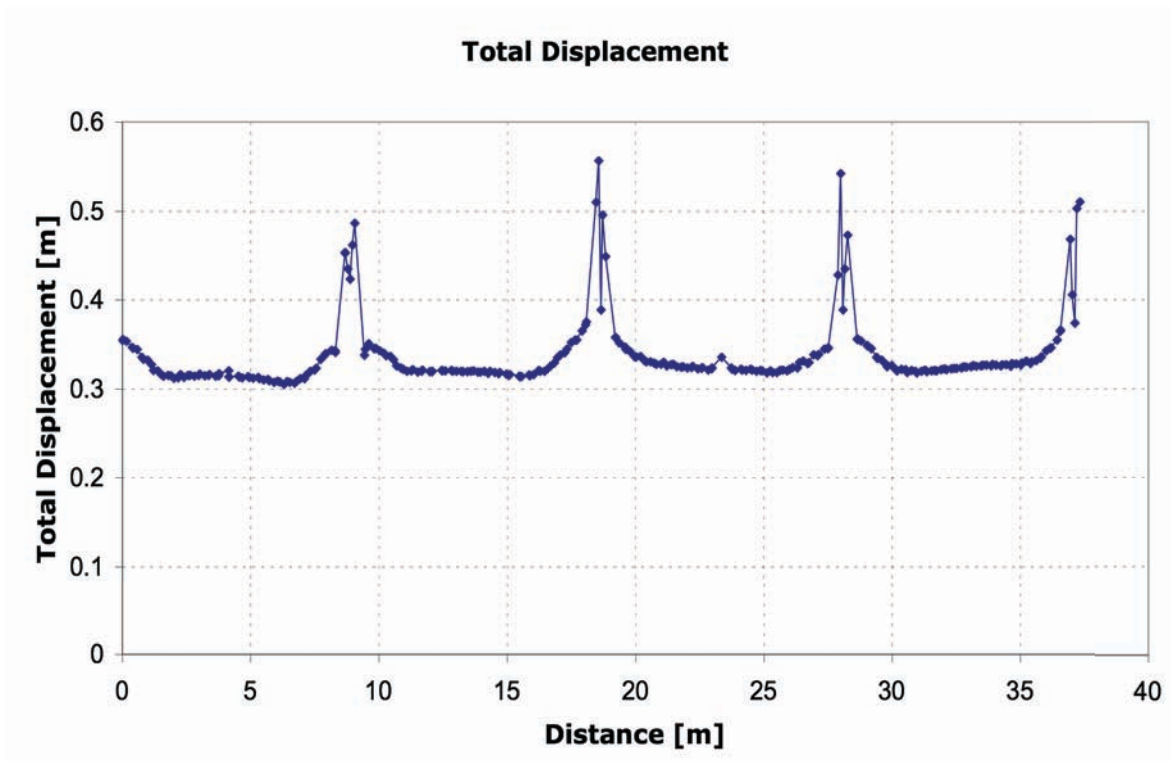


Fig. 16: Phase<sup>2</sup> displacements prediction\_Cross section with open gaps along unbound cross section

Fig. 15 and Fig. 16 show the total displacements delivered by Phase<sup>2</sup>. In order to find the concrete contribution ratio, two scenarios were calculated and compared in terms of the internal pressure delivered by the shotcrete<sup>1</sup>, one with the open gaps and one without them. A ratio was calculated by means of equation 17.

$$\text{Shotcrete contribution ratio} = \frac{\text{Support pressure with open gaps}}{\text{Support pressure without gaps}} \times 100 \quad (17)$$

The output of that simulation was a ratio of 10% of the support pressure delivered by the shotcrete under normal condition, when using the open displacement gaps. (See Fig. 16)

2. **Open gaps closure:** the open gaps aperture for a given cross section is taken as an input value, which allows the model to estimate the distance to the face in which the open gap closes, once the gap closes the system acts as a closed-ring, as seen in Fig. 17 (red line) there is a load increment starting in the point where the gaps close. It is assumed that the tunnel closes in radial direction at a constant rate.

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<sup>1</sup> Data taken from phase<sup>2</sup> refer to displacements values, which had to be transferred into Feder's worksheet (see Fig. 8) in order to calculate the internal pressure  $P_i$  (see Fig. 9) needed to reach this displacement value.

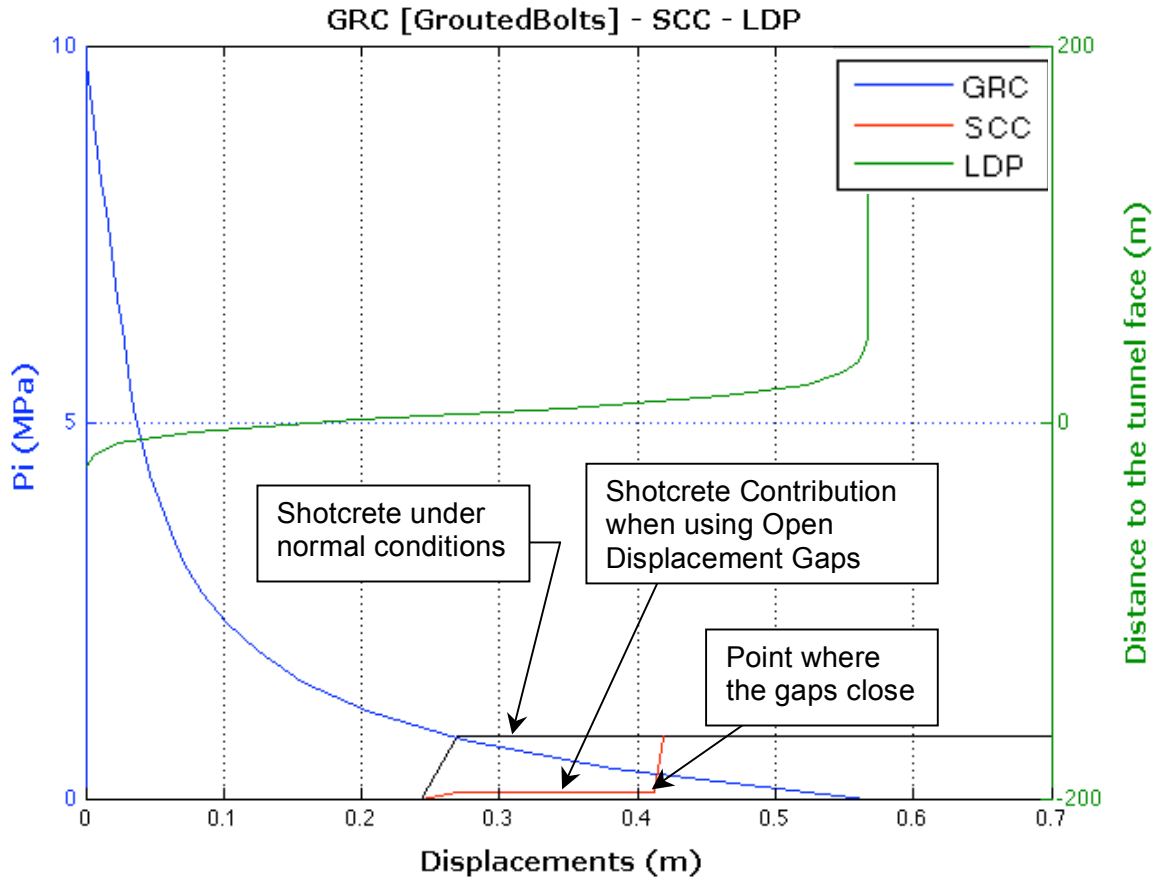


Fig. 17: Shotcrete contribution for support systems with open gaps



## 5. Results

### 5.1. Back analyzed parameters

Table 4 shows the input parameters and the limit values for E, c and  $\phi$  for each analysis. Table 5 summarizes the back-analyzed parameters with the minimum, maximum and mean value for each parameter in each one of the nine cross sections.

| Cross Section | Overburden | Messured Displa. | Back analysis limits |       |       |       |         |         |
|---------------|------------|------------------|----------------------|-------|-------|-------|---------|---------|
|               |            |                  | E_min                | E_max | c_min | c_max | Phi_min | Phi_max |
|               | [m]        | [m]              | MPa                  |       | MPa   |       | [°]     |         |
| 0+685         | 190        | 0.095            | 500                  | 4500  | 0.1   | 2.1   | 20      | 30      |
| K1+651        | 345        | 0.048            | 800                  | 7800  | 0.1   | 3.6   | 20      | 40      |
| k2+680        | 380        | 0.199            | 500                  | 6500  | 0.5   | 3.5   | 20      | 35      |
| k2+748        | 400        | 0.564            | 300                  | 1800  | 0.1   | 1.6   | 15      | 22.5    |
| k2+785        | 415        | 0.445            | 300                  | 1300  | 0.1   | 1.6   | 15      | 22.5    |
| k3+224        | 410        | 0.704            | 300                  | 1800  | 0.1   | 1.6   | 15      | 22.5    |
| K3+242        | 410        | 0.659            | 300                  | 1800  | 0.1   | 1.6   | 15      | 22.5    |
| k3+307        | 400        | 0.574            | 300                  | 1800  | 0.1   | 1.6   | 15      | 22.5    |
| k3+558        | 390        | 0.227            | 300                  | 2300  | 0.1   | 2.1   | 15      | 25      |

**Table 4: Summary Back-analyzed limits for the Inntal Tunnel**

Analysis limits shown in Table 4 were chosen in order to calibrate the model. Through this process the need of expertise for the selection of such limits is noticed.

| Cross Section | Overburden | Measured Displa. | Backed Analyzed parameters |       |        |       |       |        |         |         |          |
|---------------|------------|------------------|----------------------------|-------|--------|-------|-------|--------|---------|---------|----------|
|               |            |                  | E_min                      | E_max | E_mean | c_min | c_max | c_mean | Phi_min | Phi_max | Phi_mean |
|               | [m]        | [m]              | MPa                        |       |        | MPa   |       |        | [°]     |         |          |
| 0+685         | 190        | 0.095            | 500                        | 2500  | 1194   | 0.1   | 0.8   | 0.34   | 15      | 29.5    | 20.6     |
| K1+651        | 345        | 0.048            | 1400                       | 6600  | 2508   | 0.1   | 3.6   | 1.52   | 20      | 40      | 28.9     |
| K2+680        | 380        | 0.199            | 500                        | 2900  | 916    | 0.2   | 1.7   | 0.73   | 20      | 35      | 26.2     |
| K2+748        | 400        | 0.564            | 300                        | 1800  | 938    | 0.1   | 1.3   | 0.53   | 15      | 22.5    | 18.3     |
| K2+785        | 415        | 0.445            | 300                        | 1800  | 874    | 0.2   | 1.6   | 0.81   | 15      | 22.5    | 18.6     |
| K3+224        | 410        | 0.704            | 300                        | 1800  | 794    | 0.2   | 1.4   | 0.68   | 15      | 22.5    | 18.4     |
| K3+242        | 410        | 0.659            | 300                        | 1800  | 865    | 0.2   | 1.5   | 0.68   | 15      | 22      | 18.5     |
| K3+307        | 400        | 0.574            | 300                        | 1800  | 863    | 0.2   | 1.6   | 0.76   | 15      | 22.5    | 18.9     |
| K3+558        | 390        | 0.227            | 500                        | 2300  | 1207   | 0.3   | 2.1   | 1.06   | 15      | 25      | 20.1     |

**Table 5: Summary Back-analyzed values for the Intal Tunnel**

The mean values seen in Table 5 have to be handled with carefulness, since they only depend on the limits chosen for the analysis. Regarding Table 5 it is important to emphasize the back-analyzed cohesion values. They move in a rather small range compared to the E and  $\phi$  values. It was also observed that the cohesion upper limit is fixed, regardless of the E and  $\phi$ . This behavior is not seen for  $\phi$ , which are clearly related to the Young's modulus.

Fig. 18 and 19 graphically summarize the back-analyzed parameters for the cross section k1+651 and k3+307 respectively. As expected for high Young's moduli, lower  $c$  and  $\varphi$  parameters are needed in order to accomplish the same displacement values  $u_{eq}$  (see Fig. 6), this trend is seen in all the back-analyzed cross sections. A linear trend is also observed in these figures for each Young's modulus. This was also expected, since the formulations used for the present thesis describe rock masses with linearly elastic - ideally plastic material behaviour.

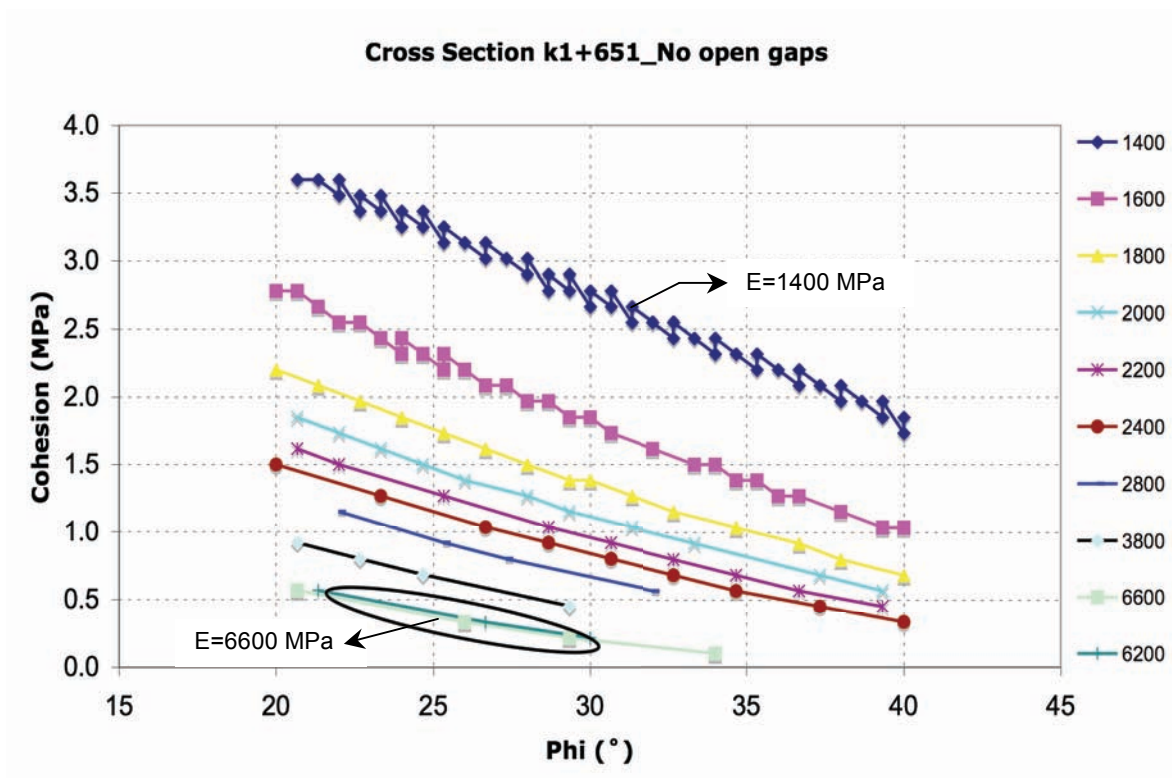


Fig. 18: Results Cross section K 1+651\_No open gaps

The limits selection for the back analysis was made based on experience. It is noticed that the value used for the cross section without open displacement gaps are significantly higher than those chosen for the cross section without them, this was made in order to be in agreement with the observed displacement values.

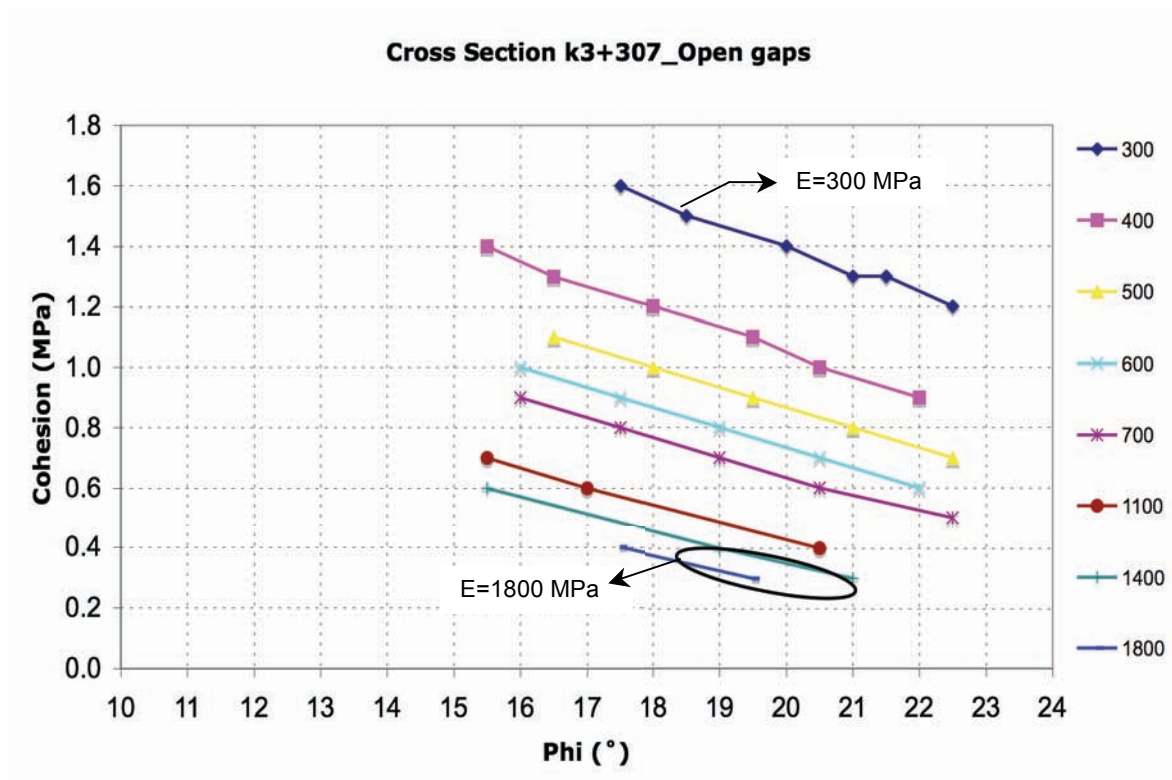


Fig. 19: Results Cross section K 3+307\_Open gaps

## 5.2. E, c and $\phi$ range selection

As written before, the results of the back analysis itself delivered a wide range of values that fulfill the measured displacements, in an attempt to reduce this range two different approaches were implemented into the model: Axisymmetric modelling and convergence analysis from Panet & Guenot formulation [24].

### 5.2.1. Axisymmetric modeling

Using the FE computational program Phase<sup>2</sup> one can simulate an advance rate and its influence on the displacements for a given cross section. Fig. 20 and 21 show the models assembled for the cross section k0+685 and k2+748 respectively. For each cross section a model was made considering the following points:

- **Distance to the face of min. 80m:** this distance was selected, based on the measured displacements, in order not to take into account time dependent displacements. Each model was divided into stages simulating the excavation rate given by the design.
- **Support systems:** Axisymmetric models in Phase<sup>2</sup> do not allow the user to implemented a support system itself, but rather simulate it as an internal pressure value “Pi”, The internal pressure value was calculated for each cross section based on the support design and implemented into the model as the excavation stages were taking place (See excavation red arrows Fig. 20)
- **Open displacement gaps:** For the cross section with open displacements gaps a special consideration was made regarding the support system since the gaps have a max. closure distance. With the help of the longitudinal deformation profile (LDP) it was possible to establish the distance to the tunnel face in which this closure takes place and from that point on set a higher internal pressure “Pi” representing the closed shotcrete lining (see Fig. 21).
- **Displacement development:** As explained in chapter 3. displacement data was measured using reflective targets located at a know cross section, the same principle was implemented in the Phase<sup>2</sup> model, one point was defined in order to estimate the displacement development related to advance excavation (see point “A” Fig. 20).

Fig. 22 shows the displacements results for point “A”, this example is the simulation in cross section 2+785\_Open gaps, where each stage simulates an excavation step. The buckle in the curve takes place in the stage where the gaps close, starting in this point a higher inner pressure is simulated.

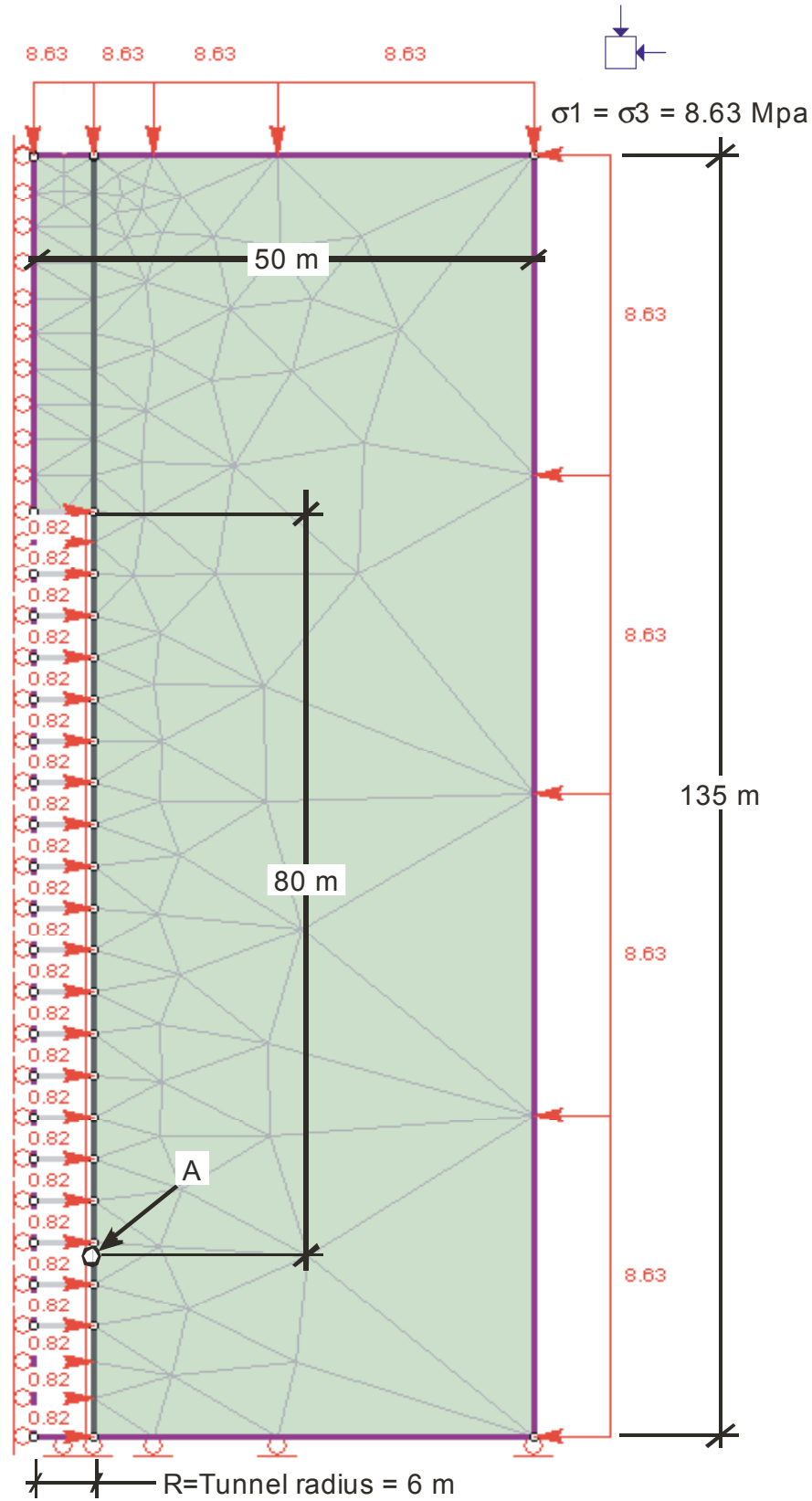


Fig. 20: Axisymmetric model K 0+685\_ No open gaps

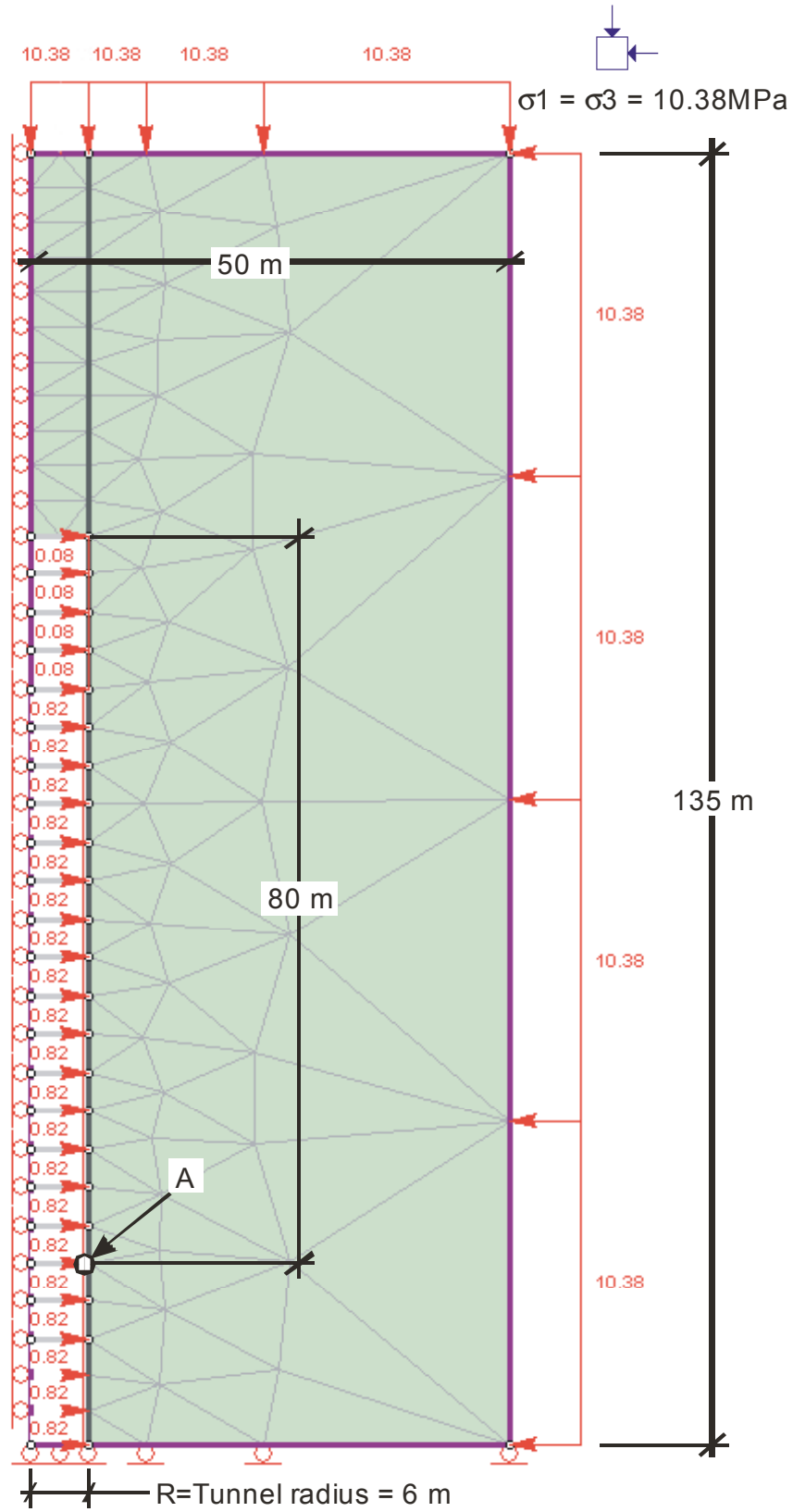
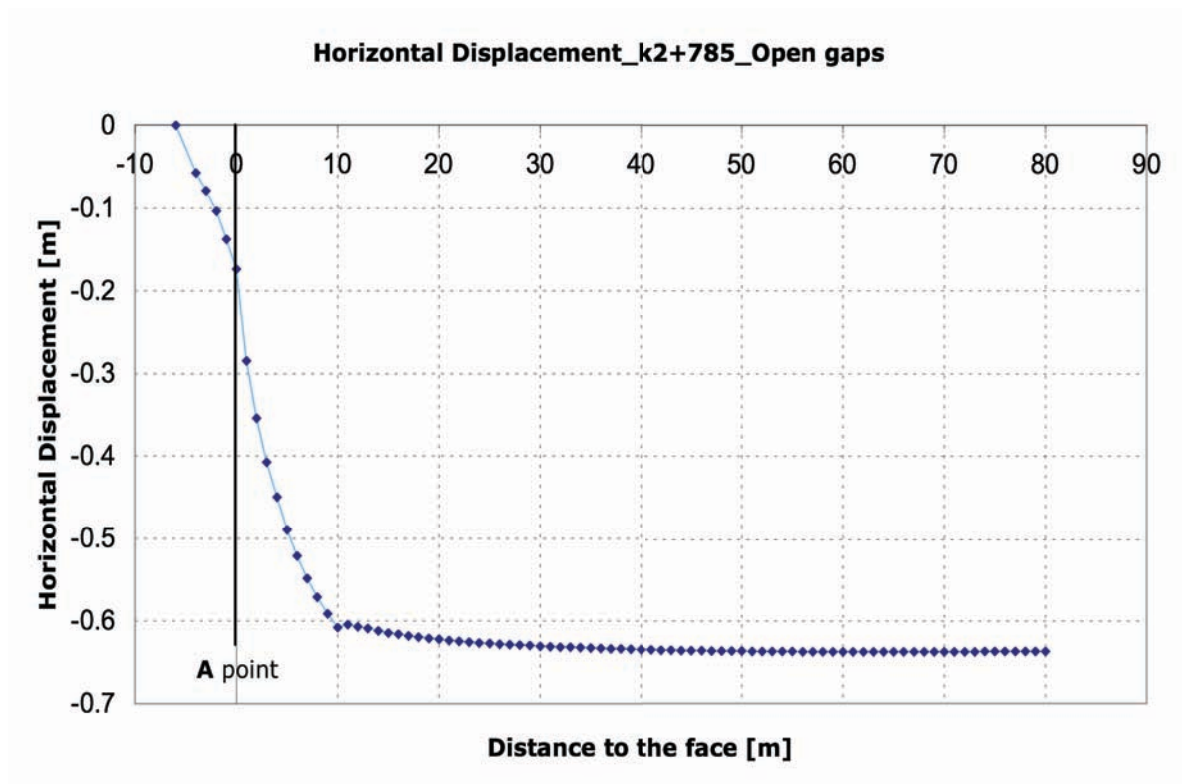


Fig. 21: Axisymmetric model K 2+748\_ Open gaps



**Fig. 22: Resulting displacements of the Axisymmetric model K 2+785\_ Open gaps**

The purpose of the simulation was to establish the displacement developed with the excavation advance for each set of parameters ( $E$ - $c$ - $\phi$ ) delivered by Matlab and then compare it to the one registered in situ (Geofit curves). An example of this process is shown in Fig. 23.

Even though the simulation would show a good “fitting” for some set of parameters, after several simulation it was concluded that, when the grouted bolts have big influence (large displacements are taking place) the model would not deliver the expected final displacement and therefore a wrong displacement path comes as a result.



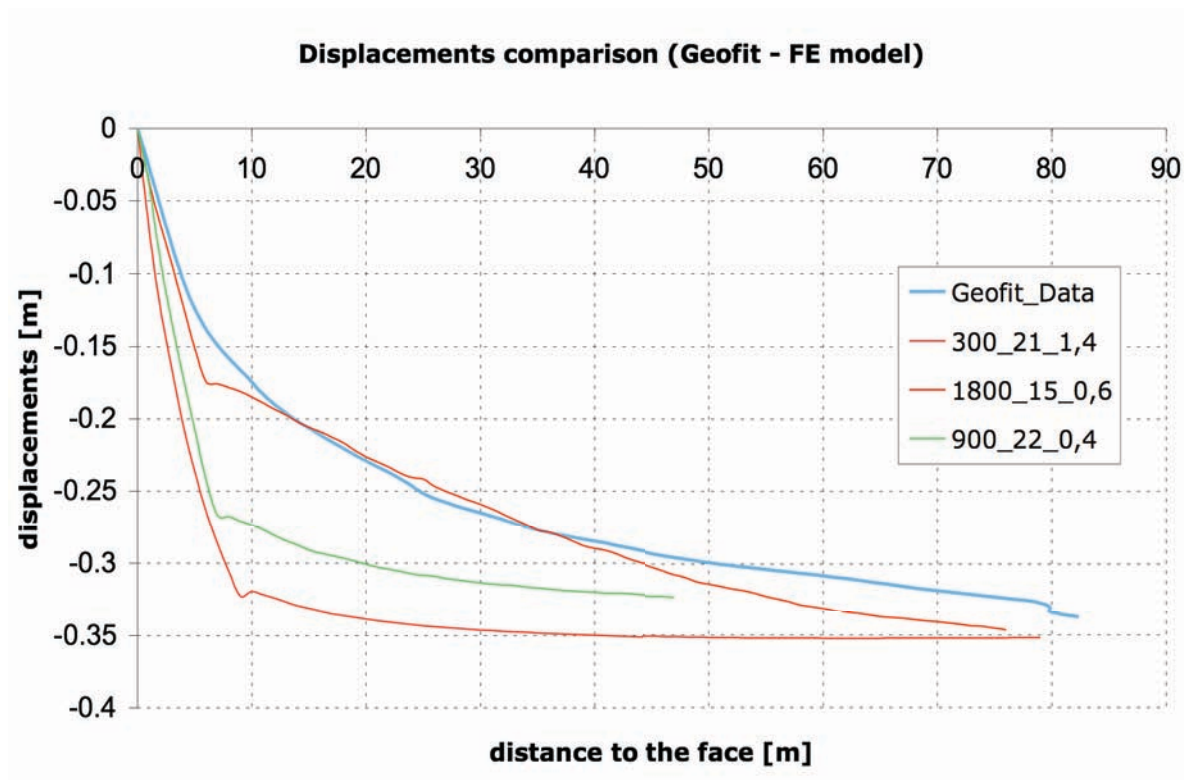


Fig. 23: Displacement development comparison\_FE\_K 2+785\_ Open gaps

### 5.2.2. Formulation after Panet & Guenet [24]

The convergence analysis from Panet & Guenet [24] has the same conditions as the convergence-confinement method: circular cross section, homogeneous, isotropic and an elastic medium. The researchers studied the progressive closure behind the face as the face advances, basically a three-dimensional problem that through some simplification and uncertainties could be approached as an equivalent plane strain problem. Following expression (18) concludes their work, varying the closure of the tunnel as a function of the distance to the face and the plastic radius:

$$c(x) = c_{\infty} \left[ 1 - \left( \frac{1}{1 + \frac{x}{0.84r_p}} \right)^2 \right] \quad (18)$$

where:

- x is the distance to the tunnel face [m];
- $C_{\infty}$  is the maximal radial displacement [m];
- $r_p$  is the plastic radius [m].

Taking the formulation of Panet & Guenet [24] and the plastic radius delivered by the Matlab back analysis, as a starting point, one could see the set of parameters that fit better to the measured displacements. As seen in Fig. 24, 25 and 26, for the cross sections k0+685, k2+748 and k3+307 respectively, the measured displacements and the ones calculated by the formulation from Panet & Guenet [24] show good fitting. It is worth mentioning that the cross section with the lowest overburden (k1+651) had the worst fitting when compare to the other cross sections.

Once the plastic radii that fit best to the measured displacements were identified, the corresponding set of E-c- $\phi$  is known, through this process it was possible to minimize the range of the back calculated values. Table 6 summarizes these values.

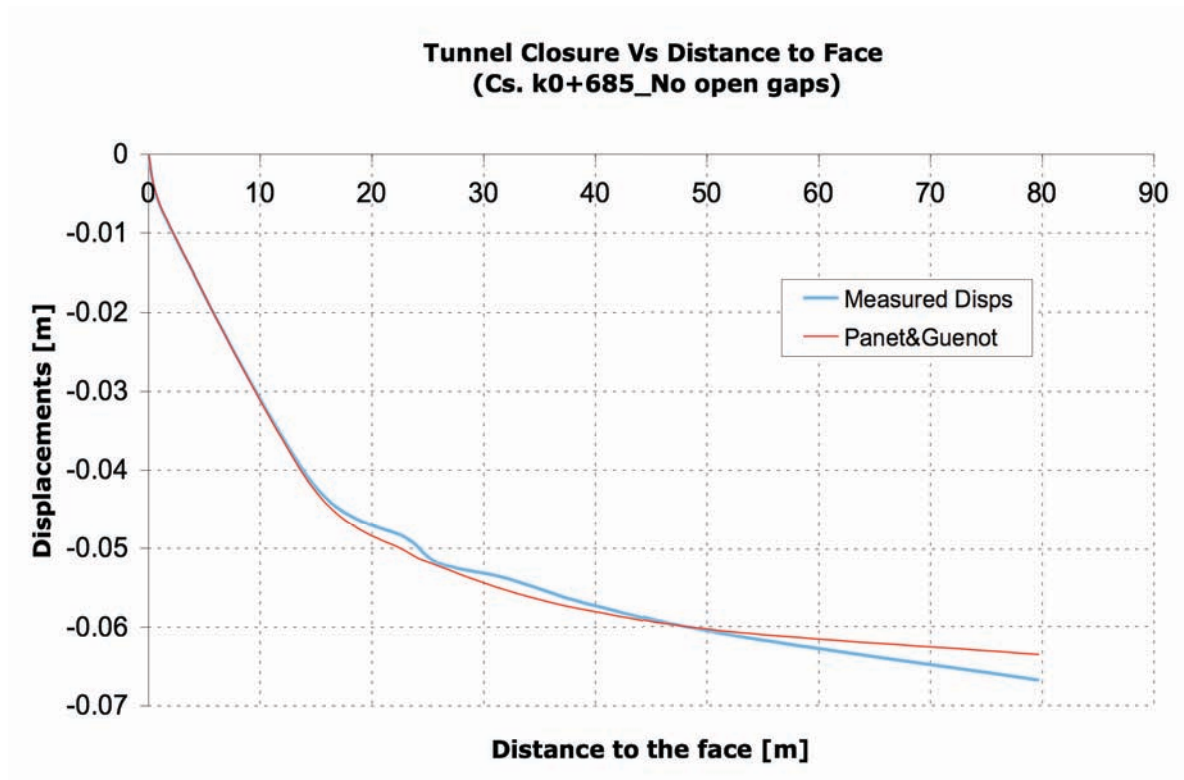


Fig. 24: Displacement development comparison\_Panet & Guenot [24]  
k 0+685\_No open gaps

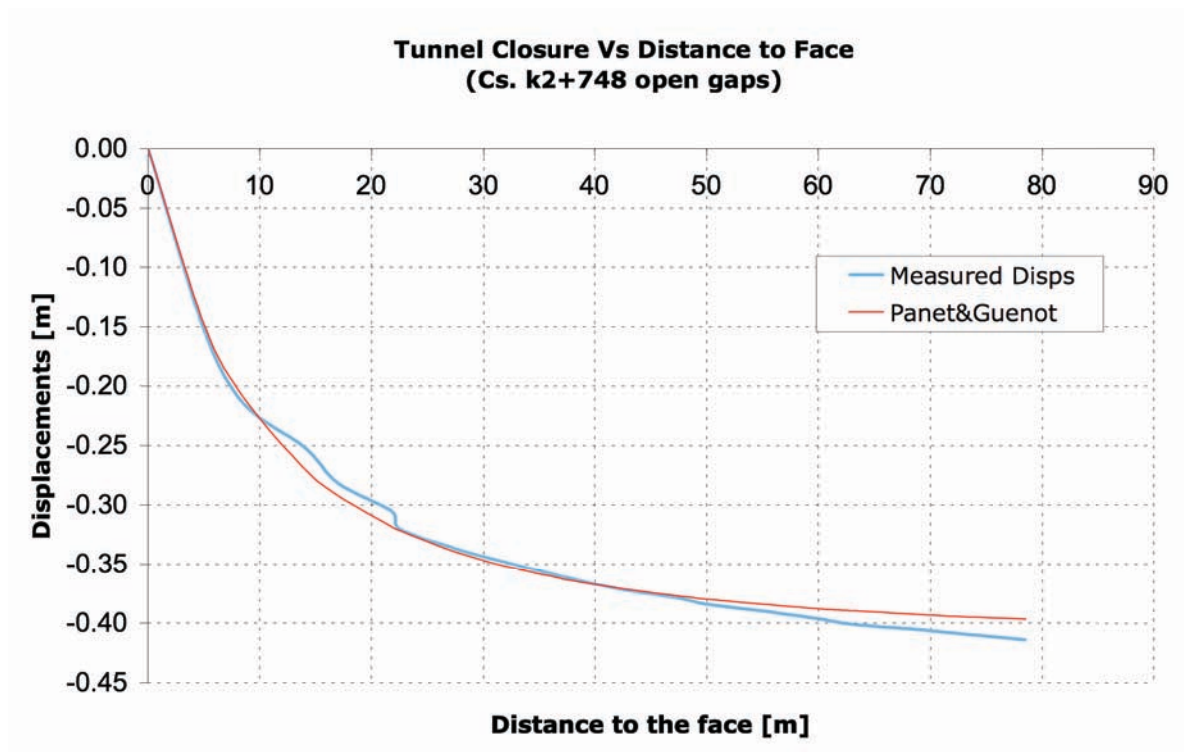


Fig. 25: Displacement development comparison\_Panet & Guenot [24]  
k 2+748\_Open gaps

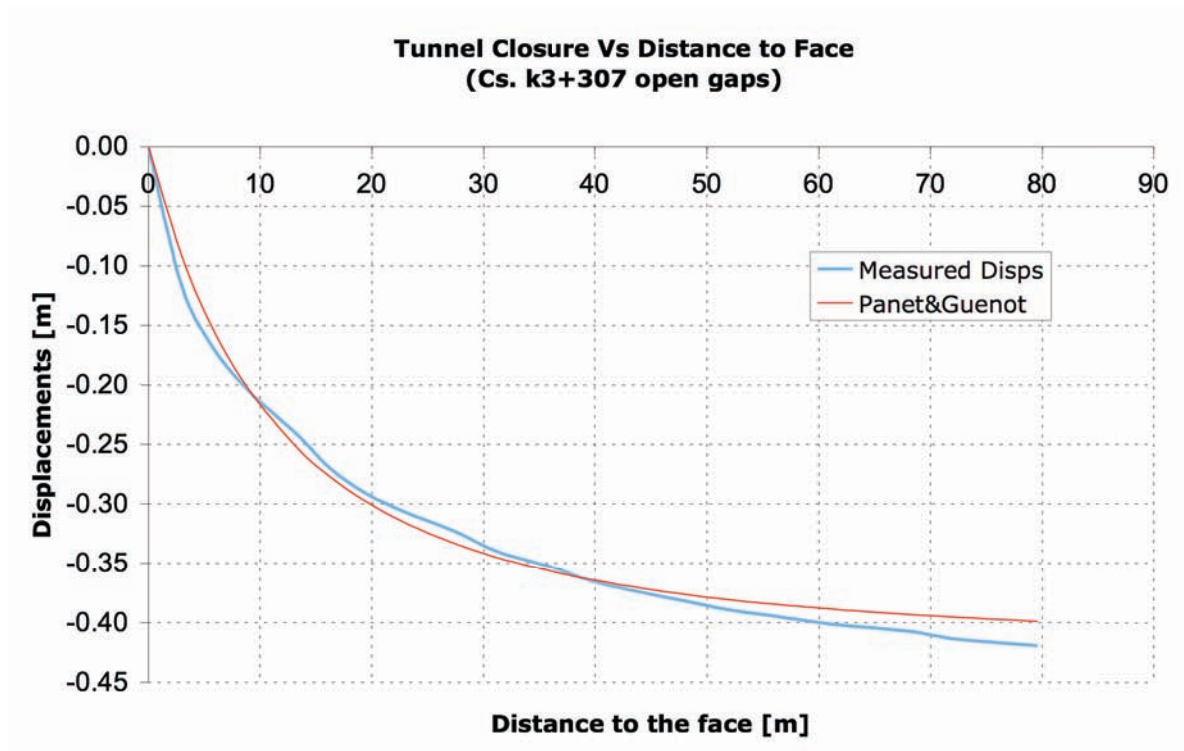


Fig. 26: Displacement development comparison\_Panet & Guenot [24]  
k 3+307\_Open gaps

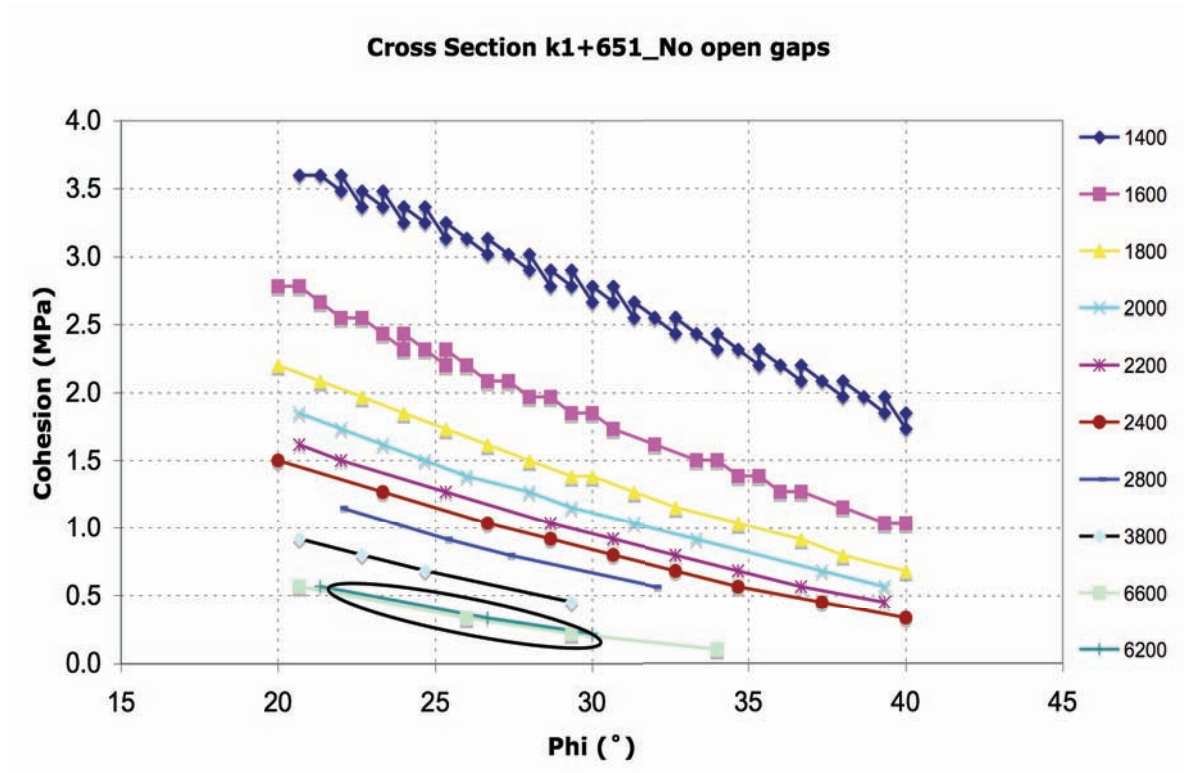


Fig. 27: Back analyzed range values\_K 1+651\_No open gaps

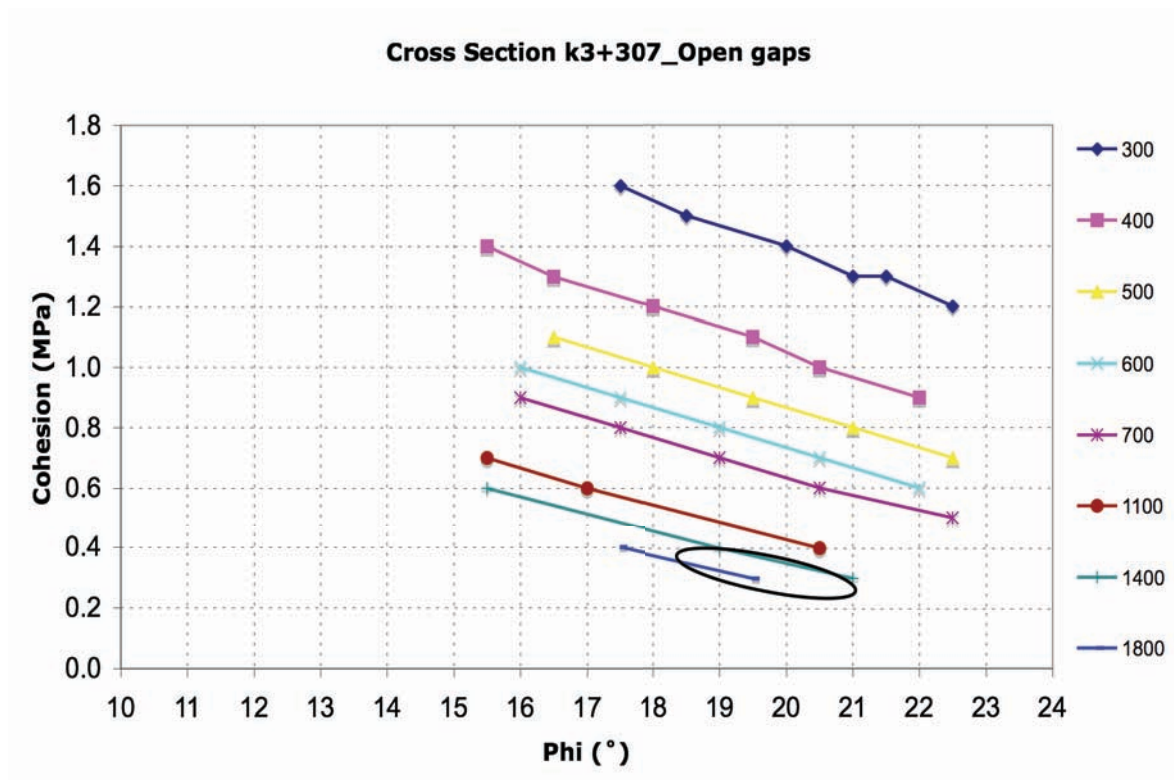


Fig. 28: Back analyzed range values\_K 3+307\_Open gaps

Fig. 27 and 28 are shown as an example for the range of values' selection in cross sections k1+651 and k3+307 respectively. It is worth mentioning that the values shown in Table 6 are to be considered as range therefore all E-c- $\phi$  values between those ranges fulfill the displacements (Matlab simulation) and Plastic Radius (Panet & Guenet [24] formulation) conditions.

|        | E (MPa) | Phi (°) | C (MPa) | PlasticRadius (m) |
|--------|---------|---------|---------|-------------------|
| k0+685 | 1200    | 19.0    | 0.3     | 25.52             |
|        | 1300    | 18.5    | 0.3     | 26.89             |
|        | 1300    | 20.5    | 0.2     | 26.56             |
| k1+651 | 6200    | 21.3    | 0.6     | 16.05             |
|        | 6600    | 20.7    | 0.6     | 16.77             |
|        | 6600    | 26.0    | 0.3     | 16.43             |
|        | 6600    | 29.3    | 0.2     | 16.28             |
| k2+680 | 2900    | 20.0    | 0.3     | 27.62             |
|        | 2900    | 22.5    | 0.2     | 27.22             |
| k2+748 | 1100    | 19.5    | 0.3     | 24.27             |
|        | 1100    | 21.5    | 0.2     | 24.02             |
|        | 1200    | 19.0    | 0.3     | 25.52             |
|        | 1200    | 21.0    | 0.2     | 25.23             |
| k2+785 | 1700    | 19.5    | 0.3     | 25.07             |
|        | 1800    | 19.0    | 0.3     | 26.39             |
| k3+224 | 700     | 20.0    | 0.5     | 19.56             |
|        | 800     | 19.0    | 0.5     | 21.26             |
|        | 900     | 20.0    | 0.4     | 22.62             |
| k3+242 | 1400    | 20.0    | 0.3     | 27.10             |
|        | 1500    | 19.5    | 0.3     | 28.56             |
|        | 1600    | 21.5    | 0.2     | 28.88             |
| k3+307 | 1400    | 21.0    | 0.3     | 24.05             |
|        | 1500    | 18.5    | 0.4     | 25.53             |
|        | 1800    | 19.5    | 0.3     | 27.94             |
| k3+558 | 2000    | 22.5    | 0.4     | 16.14             |
|        | 2200    | 20.0    | 0.5     | 17.15             |

**Table 6: Summarized Range values for the Inntal Tunnel.**

### 5.3. Influence of Young's modulus

In order to find out the influence of the Young's modulus, the back analyzed parameters were studied towards E-c- $\phi$  combination behavior. To accomplish this purpose a linear regression was calculated for every single E in a given cross section. From this procedure the parameters *a* and *b* from the formulation of a linear function  $y = ax + b$  were calculated (Table 7) these parameters *a* and *b* describe the influence of different Young's moduli. Therefore the graphics in Fig. 29, 30 and 31 show the resulting *a* and *b* values and depict a quadratic function in order to describe this data. These graphics are not to be compared, as they are from different cross sections with different overburdens and support systems, that is why no trend can be detected analyzing the different *a* and *b* values.

| Cross Section k1+651 |        |       |        | Cross Section k2+748 |        |       |        | Cross Section k3+307 |        |       |        |
|----------------------|--------|-------|--------|----------------------|--------|-------|--------|----------------------|--------|-------|--------|
| E                    | a      | b     | Correl | E                    | a      | b     | Correl | E                    | a      | b     | Correl |
| 1400                 | -0.094 | 5.589 | -0.994 | 300                  | -0.076 | 2.543 | -0.999 | 300                  | -0.078 | 2.948 | -0.995 |
| 1600                 | -0.090 | 4.552 | -0.996 | 400                  | -0.073 | 2.233 | -1.000 | 400                  | -0.076 | 2.565 | -0.998 |
| 1800                 | -0.085 | 3.887 | -0.998 | 700                  | -0.067 | 1.767 | -1.000 | 500                  | -0.067 | 2.200 | -1.000 |
| 2000                 | -0.068 | 3.194 | -0.996 | 800                  | -0.067 | 1.700 | -1.000 | 600                  | -0.067 | 2.067 | -1.000 |
| 2200                 | -0.063 | 2.875 | -0.997 | 1000                 | -0.067 | 1.600 | -1.000 | 700                  | -0.062 | 1.889 | -0.998 |
| 2400                 | -0.059 | 2.622 | -0.996 | 1100                 | -0.055 | 1.375 | -0.999 | 900                  | -0.067 | 1.833 | -1.000 |
| 2600                 | -0.056 | 2.472 | -0.995 | 1200                 | -0.055 | 1.348 | -0.999 | 1000                 | -0.057 | 1.614 | -1.000 |
| 2800                 | -0.058 | 2.401 | -0.996 | 1300                 | -0.055 | 1.320 | -0.999 | 1100                 | -0.059 | 1.618 | -0.999 |
| 3000                 | -0.051 | 2.182 | -0.996 | 1600                 | -0.050 | 1.175 | -1.000 | 1200                 | -0.055 | 1.503 | -0.999 |
| 3200                 | -0.050 | 2.065 | -0.997 |                      |        |       |        | 1300                 | -0.054 | 1.452 | -0.998 |
| 3400                 | -0.049 | 2.028 | -0.995 |                      |        |       |        | 1400                 | -0.055 | 1.448 | -0.999 |
| 3800                 | -0.054 | 2.017 | -0.999 |                      |        |       |        | 1500                 | -0.057 | 1.457 | -1.000 |
| 4000                 | -0.054 | 1.982 | -0.999 |                      |        |       |        | 1800                 | -0.050 | 1.275 | -1.000 |
| 4200                 | -0.052 | 1.905 | -0.999 |                      |        |       |        |                      |        |       |        |
| 4800                 | -0.035 | 1.388 | -0.991 |                      |        |       |        |                      |        |       |        |
| 5400                 | -0.035 | 1.342 | -0.991 |                      |        |       |        |                      |        |       |        |
| 5800                 | -0.035 | 1.318 | -0.991 |                      |        |       |        |                      |        |       |        |
| 6200                 | -0.041 | 1.430 | -0.998 |                      |        |       |        |                      |        |       |        |
| 6600                 | -0.035 | 1.271 | -0.991 |                      |        |       |        |                      |        |       |        |

Table 7: Linear regression data.

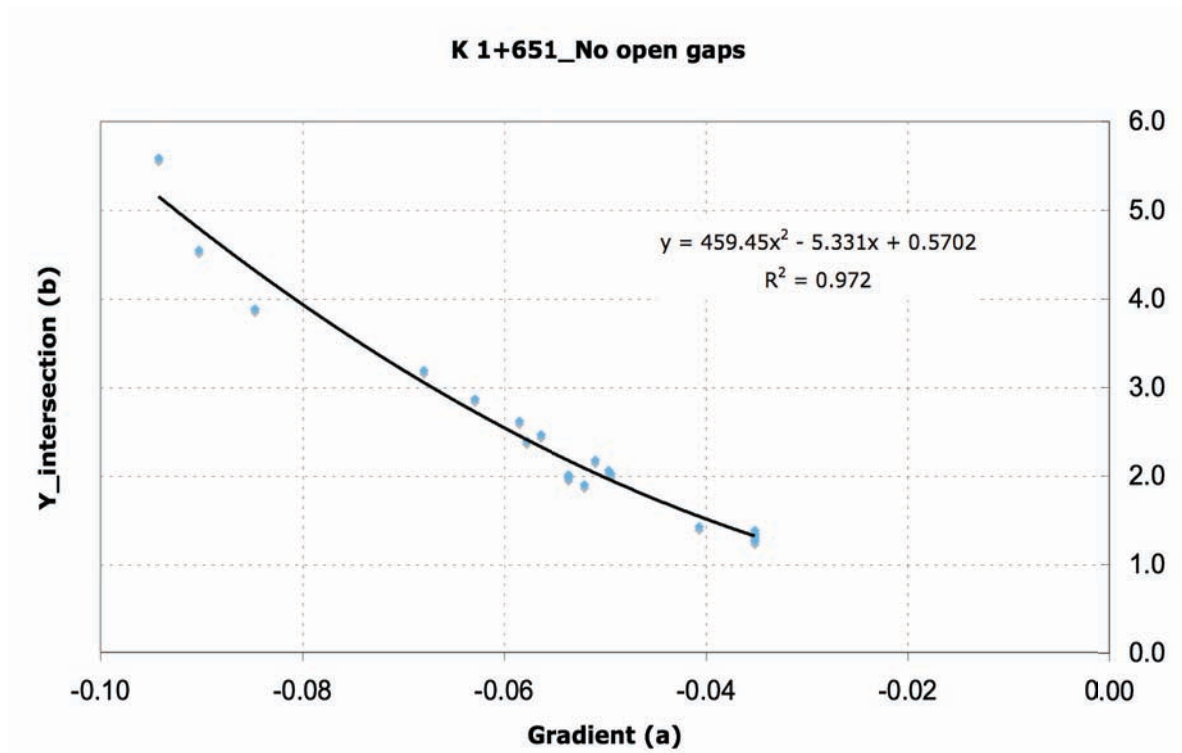


Fig. 29: Quadratic regression for the back analyzed parameter\_Cross section k 1+651\_No open gaps

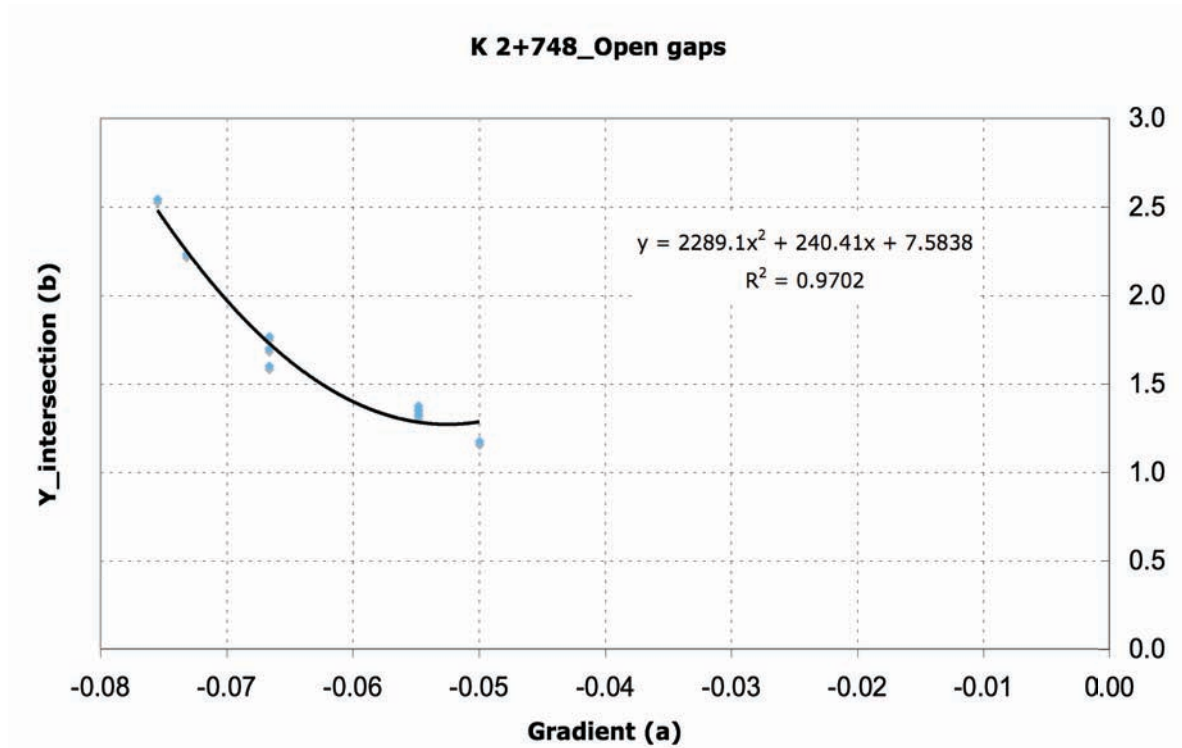
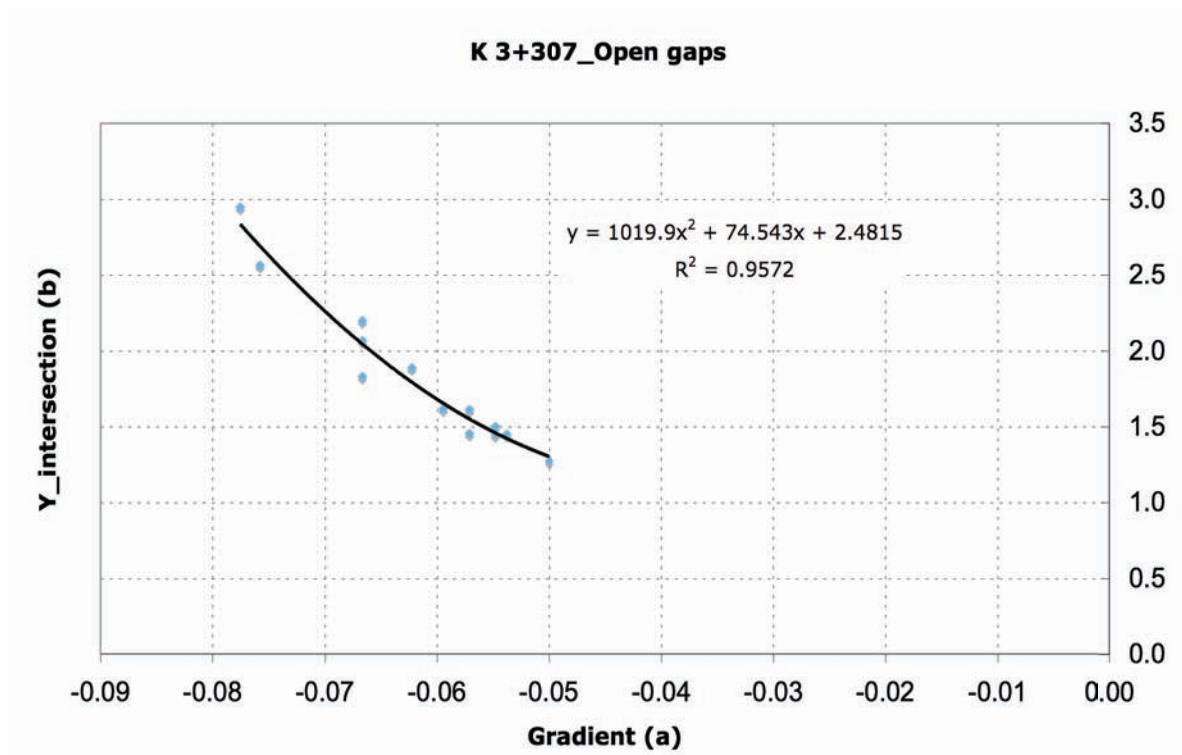


Fig. 30: Quadratic regression for the back analyzed parameter\_Cross section k 2+748\_Open gaps





**Fig. 31: Quadratic regression for the back analyzed parameter\_Cross section k 3+307\_No open gaps**

Fig. 29, 30 and 31 show a trend that follows a quadratic equation in each cross section. It was observed that the Young's moduli are inversely proportional to the  $a$  values (gradient) and  $b$  values (intersection with the  $y$ -axis) in almost all cross sections where open gaps were used. In cross sections with no open gaps a trend can also be detected but only for low Young's moduli, the higher the Young's moduli are the more complicated to establish a trend. This can also be seen in Fig. 27 where high Young's moduli (bottom of the graphic) tend to have different gradients and intersect each other.

## 6. Discussion

### 6.1. Comparison to FE and Feder & Arwanitakis [1] calculations

The back calculated values were compared to the closed form solution after Feder & Arwanitakis [1] and to numerical FE simulations with Phase<sup>2</sup>, both calculations proved the successful operation of the developed Matlab tool. Fig. 32 shows the cross section K0+685, which does not consider open gaps, implemented in phase<sup>2</sup>. The displacements calculated from the formulation from Feder & Arwanitakis [1] as well as FE simulation, are in the same order of magnitude with the proposed model (see Table 8).

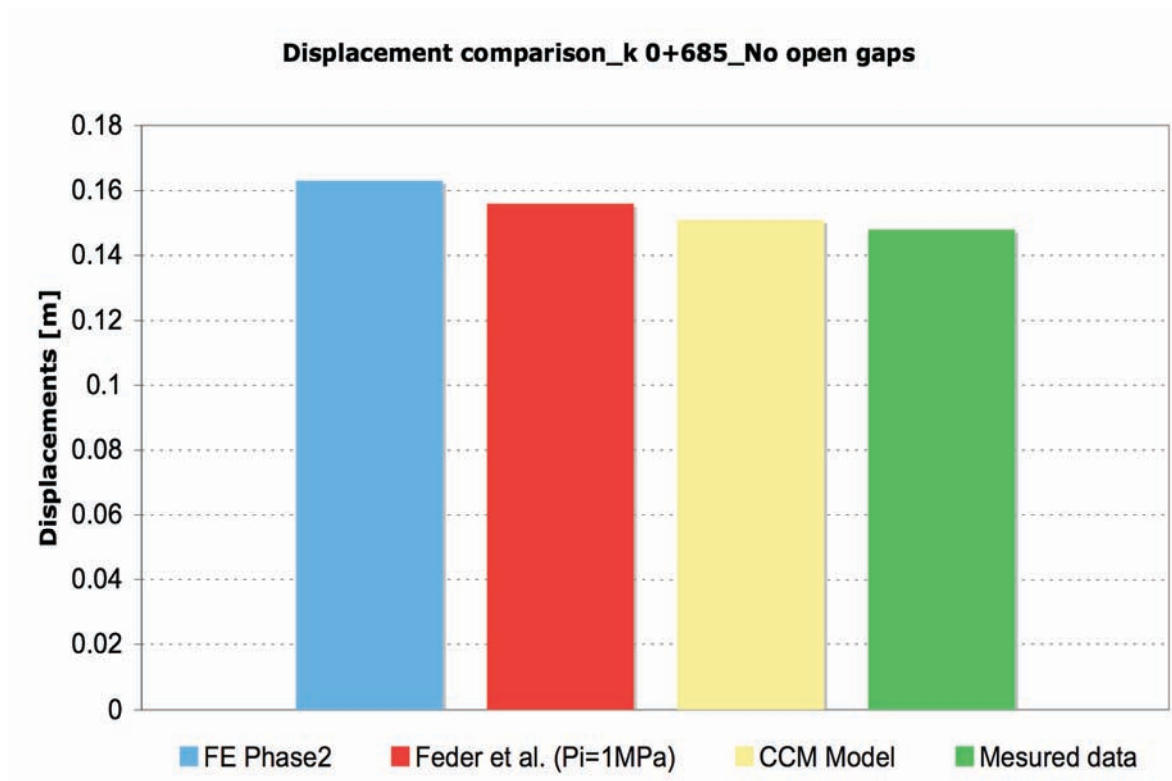


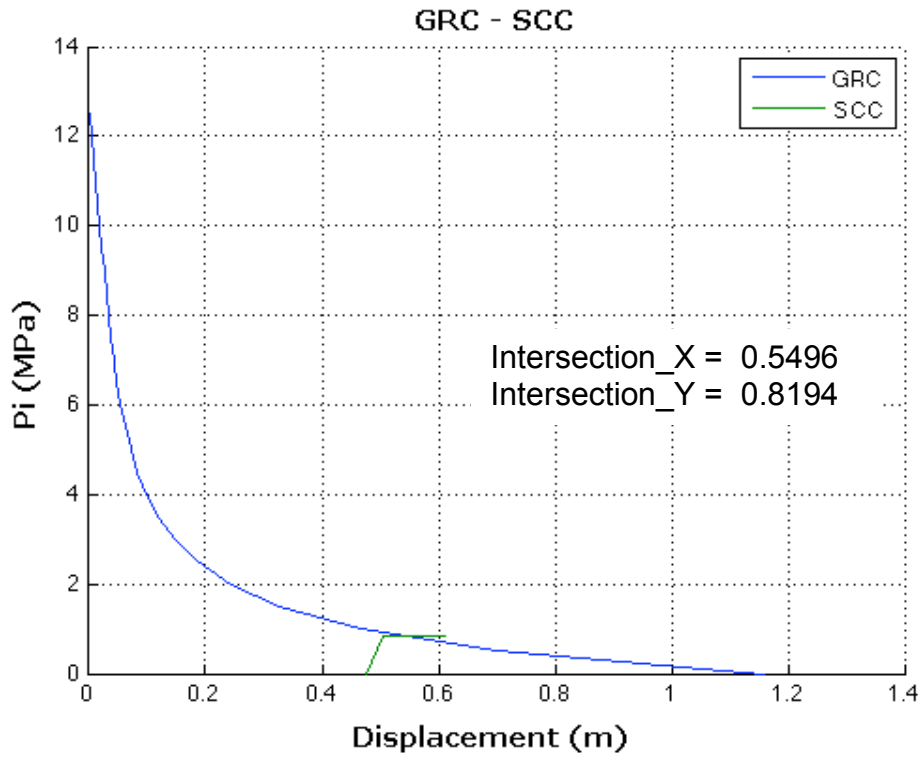
Fig. 32: Comparison of displacements of the used models

| Cross section: k 0+685_No open gaps |                  |
|-------------------------------------|------------------|
| Model                               | Displacement [m] |
| FE Phase2                           | 0.163            |
| Feder et al. (Pi=1MPa)              | 0.156            |
| CCM Model                           | 0.151            |
| Mesured data                        | 0.148            |

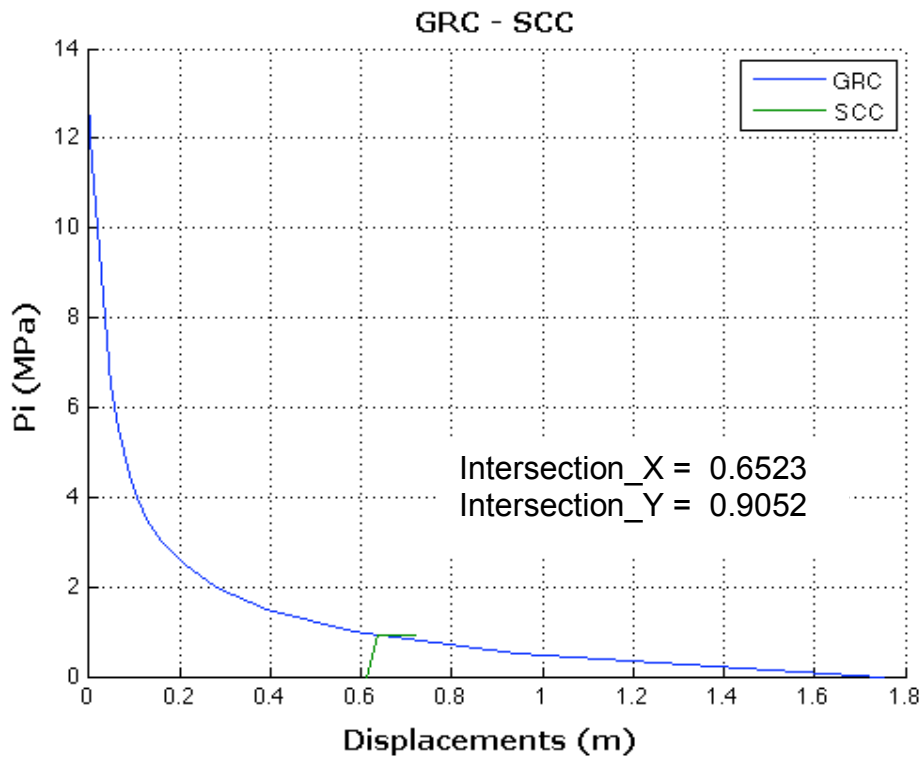
**Table 8:** Comparison of displacements of the used models.

## 6.2. Comparison between grouted and non grouted bolts

Even though the use of non-grouted bolts and cables is not a common practice in tunneling nowadays, the Matlab code developed for this thesis allows the user to simulate a SCC considering this kind of support. Taking this into account the present study compares the usage of grouted and non-grouted bolts. For this purpose several analysis were made varying the amount, longitudinal spacing, length and diameter of the bolts, as well as the  $E$ ,  $c$  and  $\phi$  rock mass parameter. It has to be considered that the diameter of a non grouted bolt was always smaller compared to a grouted bolt. In the case of grouted bolts the external diameter of the grouting is also an input value for the model.



**Fig. 33: GRC and SCC for support with Grouted bolts**



**Fig. 34: GRC and SCC for support with Non-Grouted bolts**

It was seen that when using the same number, length and diameter of bolts for a specific rock mass defined by  $E$ ,  $c$  and  $\varphi$  the final displacement values are always lower in the case of the grouted bolts (see in Fig. 33 and 34).

For the specific case shown in Fig. 33 and 34 an overburden of 500m,  $E=1000\text{MPa}$ ,  $c=0.5\text{MPa}$ ,  $\varphi=20^\circ$  and a support system consisting of 20cm shotcrete and a total of 25 bolts were selected (steel profiles are not considered in this section).

Comparing the two scenarios a ratio of  $\approx 1.2$  was calculated, that would hypothetically imply that  $\approx 30$  non-grouted bolts would reach the same final displacement as 25 grouted bolts. This ratio applies only for this specific case, since, for the grouted bolt case, the load is transferred and distributed throughout the length of the bolt and proportional to the rock mass displacements. But the same trend can be seen in all analyzed calculations.

Comparing different cases of grouted bolts and cases without any bolts the dependency of the grouted bolts on the rock mass displacements was also seen in this analysis. The perceptual difference in the final displacement (equilibrium point) increases inversely proportional to the rock quality and overburden, in other words the less competent the rock mass the better is the effect or contribution of the grouted bolts.

The presented model does not consider dilatancy for grouted bolt cases, nevertheless it is worth mentioning that dilatancy contributes to stability as mentioned in the previous chapter.

## 7. Conclusions

There are many reasons why back analysis models are used more frequently e.g. better and more reliable algorithms are available, the possibility of implementing them in simple personal computers in which one can produce large amounts of data, quick response to unexpected events and low cost among others.

The proposed model gives the possibility to assemble the convergence-confinement method for rock masses that satisfy Mohr Coulomb failure criteria in short time and with low computational requirements, almost all support systems in tunneling are available and results are presented in a simple and comfortable manner.

The specific study for the Inntal tunnel, as expected, gives a wide range of values that fulfill the final displacement condition, due to the mathematical formulation used in the model, however as in the back-analysis techniques presented by Shang et al. in [7] and Yang et al. in [8] the analyzed data has to be selected based on experience. In order to decrease the range two approaches were implemented, the approach based on the formulation after Panet & Guenot [24] fits best to support system design for the specific case. Through the formulation presented by Panet & Guenot [24] the presented model is able to deliver quality data regarding  $E$ ,  $c$  and  $\phi$  peak values based on observed displacements.

It was seen that proposed model do not show a good fitting for cross sections with low overburden and small displacements, further studies regarding this subject should be done, since only one cross section (k1+651) with these characteristics was analyzed in the present study.

One important consideration comes into mind when analyzing a further application of the presented model. As a common practice laboratory and in situ testing

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focuses mainly on  $c$ ,  $E$  and  $\varphi$  peak values making these values relatively easy and inexpensive to obtain. However, as explained by Alejano and Alonso in [22], dilatancy and strength parameters in residual conditions are most difficult to estimate from preliminary investigations. In this scenario the back analysis model could be used to calculate dilatancy or an equivalent parameter, which describes the strain behaviour of the rock mass in plastic conditions, having  $E$ ,  $c$  and  $\varphi$  values as input parameters.

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