

FIGURE 5.1: Ellipsoidal coordinates. Top: View from the front. Bottom: View from above.

whose axis coincides with the z-axis, and whose linear excentricity has the constant value E. The coordinate u is the semiminor axis of this "coordinate ellipsoid", $\bar{\theta}$ is the complement of the "reduced latitude" β of P with respect to this ellipsoid (for its definition cf. sec. 1.4), and λ is the geocentric longitude in the usual sense.

The ellipsoidal coordinates $u, \bar{\theta}, \lambda$ are related to x, y, z by the equations

$$\begin{aligned} x &= \sqrt{u^2 + E^2} \sin \bar{\theta} \cos \lambda &, \\ y &= \sqrt{u^2 + E^2} \sin \bar{\theta} \sin \lambda &, \\ z &= u \cos \bar{\theta} &, \end{aligned}$$
 (5-1)

which can be read from the figure, considering that $\sqrt{u^2 + E^2}$ is the semimajor axis of the ellipsoid whose surface passes through P.