4.1 INTERNAL POTENTIAL

by (1-49). The result is (4-10) with

$$\begin{split} K_{0}(q) &= \frac{4\pi G}{3} \int_{0}^{q} \rho(q) \frac{d}{dq} \left[A_{0}(q) q^{3} \right] dq \quad , \\ K_{2}(q) &= \frac{4\pi G}{25} \int_{0}^{q} \rho(q) \frac{d}{dq} \left[B_{2}(q) q^{5} \right] dq \quad , \end{split}$$

$$\begin{split} K_{4}(q) &= \frac{4\pi G}{63} \int_{0}^{q} \rho(q) \frac{d}{dq} \left[C_{4}(q) q^{7} \right] dq \quad . \end{split}$$

$$\end{split}$$

Here we have omitted the prime in the integration variable q' as we did before. The argument q of $K_i(q)$, of course, is identical with the upper limit of the integral (but not with the integration variable!).

4.1.3 Potential of Shell E_P

We now consider the potential of the "shell" E_P bounded by the surfaces S_P and S. We apply the same trick as before (sec. 4.1.1., Fig. 4.3). We calculate V_e first not at P, but at a point P_i situated on the radius vector of P in such a way that r < r' is always satisfied and the series corresponding to (4-8),



FIGURE 4.4: Illustrating the computation of V.

$$\frac{1}{l} = \sum_{n=0}^{\infty} \frac{r^n}{r'^{n+1}} P_n(\cos\psi) \quad , \tag{4-27}$$

always converges (Fig. 4.4). For this "harmless" point we have

$$V_{e}(P_{i}) = G \iiint_{E_{P}} \frac{\rho}{l} dv = \sum_{n=0}^{\infty} r^{n} \cdot G \iiint_{E_{P}} \frac{\rho}{r'^{n+1}} P_{n}(\cos\psi) dv \quad , \qquad (4-28)$$