# Statistical analysis of maximal cardiac exercise stress testing 

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## Statutory Declaration

I declare that I have authored this thesis independently, that I have not used other than the declared sources/resources, and that I have explicitly marked all material which has been quoted either literally or by content from the used sources.

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#### Abstract

Maximal cardiac stress exercise testing is one of the common health checks especially for heart diseases. One of the crucial results is the maximal workload which a patient achieves during the examination. The aim of this thesis is to derive normal values of the maximal workload using a regression analysis with variables selection. This is done with the data from the medical institute ZARG and ProDoc, which include in total 28,625 ergometries. The resulting normal values are compared with the normal values, which are currently recommended in the guidelines of Austria. The newly calculated normal values have a better goodness of fit, especially for women, than the currently used normal values. Furthermore, the analysis of in total 1,453 ergometries at entry examinations of stage II and stage III of cardiac out-patient rehabilitation is done to calculate the normal values of maximum workload. Finally, the improvement of maximum workload during stage II and stage III of cardiac out-patient rehabilitation is analyzed.


## Zusammenfassung

Die Ergometrie ist eines der Standard-Gesundheitschecks speziell bei Herzerkrankungen. Eine der wesentlichen Resultate ist die maximale Leistung, die ein Patient während der Untersuchung erreicht. Das Ziel dieser Arbeit ist es mit Hilfe einer Regressionsanalyse mit Variablenselektion Normalwerte für die maximale Leistung zu erhalten. Dies wird mit Hilfe der Daten des medizinischen Instituts ZARG gemacht. Insgesamt standen dafür Daten von 28.625 Ergometrien zur Verfügung. Die resultierenden Normalwerte werden mit den in Österreich momentan in den Praxisleitlinien empfohlenen Normalwerten verglichen. Die neu berechneten Normalwerte besitzen eine bessere Anpassungsgüte als die momentan verwendeten Normalwerte, speziell für Frauen. Weiters beinhaltet die Arbeit Normalwerte für die maximale Leistung wie auch Normalwerte für die Verbesserung der maximalen Leistung für Ergometrien während der Eingangsuntersuchung von Phase II und Phase III der ambulanten Rehabilitation. Für diese Analyse wurden insgesamt Daten von 1.453 Ergometrien verwendet.

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## List of abbreviations

AIC Akaike's Information Criterion
$\mathrm{AIC}_{c}$ Corrected Akaike's Information Criterion
ANOVA Analysis of Variance
BIC Bayesian Information Criterion
BMI body mass index
BSA body surface area
$\mathrm{C}_{p}$ Mallow's $C_{p}$
CAD Coronary Artery Disease
CP complexity parameter
Cr creatinine
DBP diastolic blood pressure
DBP $_{\text {max }}$ diastolic blood pressure at maximum workload
DBP $_{r}$ resting diastolic blood pressure
DIAG diagnosis
EDA Explorative Data Analysis
FBS fasting blood sugar level
HDL high density lipoprotein
HR heart rate
$\mathbf{H R}_{\text {max }}$ heart rate at maximum workload
$\mathbf{H R}_{r}$ resting heart rate
LDL low density lipoprotein
MED medication

MSE mean square error
MSR mean square regression
MST mean square total
Q-Q plot Quantile-Quantile plot
RSE residual standard error
SBP $_{\text {max }}$ systolic blood pressure at maximum workload
$\mathbf{S B P}_{r}$ resting systolic blood pressure
SSE sum of squares error
SSR sum of squares regression
SST sum of squares total
SBP systolic blood pressure
TC total cholesterol
TG triglyceride
UA urid acid
VLDL very low density lipoprotein
WHR waist to height ratio
WL maximum workload
WWR workload to weight ratio
ZARG Zentrum für ambulante Rehabilitation

## Chapter 1

## Introduction

Cardiovascular diseases are responsible for $45 \%$ of all deaths in Europe. In 2015, more than 85 million people across Europe were living with cardiovascular diseases, $48 \%$ of cases were in males and $52 \%$ in females. In that year, Austria had 399,912 females and 409,542 males suffering from cardiovascular diseases [Wilkins et al., 2017]. For more than six decades now, maximal cardiac exercise stress testing is used to evaluate the functional capacity of the heart non-invasively and is an efficient and a cost effective way. Moreover, it is useful in determining the risk and extent of coronary artery diseases (CAD), prognosis and prediction of cardiovascular events, and the effect of therapy [Fletcher et al., 2013]. The testing may involve ergometers such as stationary bicycles, treadmills, rowing machines, arm ergometer and monitoring of cardiac activities by electrocardiography and blood pressure monitoring (see e.g. [Pina et al., 1995]). Such tests involve exercising at several workloads or exercise intensities, during which cardiovascular and respiratory measurements are recorded. Depending on the rationale for testing, the type of test employed, and the health and fitness status of the individual taking part, exercise stress tests might terminate on volitional exhaustion or upon observation of a particular clinical symptom, or at some other predetermined outcome measure [Turner, 2013].

Cardiac rehabilitation is a multidisciplinary approach at physical, social and psychological levels to reduce the risk and secondary progression of cardiovascular diseases and reverse the disease progressions [Price et al., 2016]. Studies have shown the benefits of cardiac rehabilitation and it has been recommended by the European Society of Cardiology, American Heart Association and the American College of Cardiology for the treatment of cardiovascular diseases [Bjarnason-Wehrens et al., 2010]. Traditionally, cardiac rehabilitation is divided into three stages (I, II, III). Stage I is started when the patient is in the hospital whereas stage II (short-term stage) and stage III (long-term stage) are on outpatient or in-patient basis. Cardiac rehabilitation is provided through different models which differs across Europe depending upon local and national health guidelines [Bjarnason-Wehrens et al., 2010]. The assessment of physical activity using cardiac exercise stress test in clinical settings is an important task for the physicians involved in preventive cardiology [Piepoli et al., 2010]. According to Austrian outpatient rehabilitation guidelines, the cardiac exercise stress test (ergometry) is performed three times, initial (beginning of stage II), inter-
mediate (end of stage II or/and beginning of stage III) and final (end of stage III) [Niebauer et al., 2012].

One of the crucial measured parameters in ergometry is the maximum workload achieved. For the interpretation of the results of an ergometry, the normal values of maximum workload are used. These normal values are expected values, which a person should achieve. The literature for calculating the normal values of the maximum workload during an ergometry is scant. For Austria, Wonisch et al., 2008] suggested to continue using the same normal values as in the old guideline [Niederberger et al., 1974]. These normal values are dated back to [Arstila, 1972]. Unfortunately, it was not possible to obtain further information on the population and number of subjects used to develop a model for calculating the normal values. These normal values are still used, although they have not been updated for over 40 years. In last few decades, new mathematical models were developed to update the normal values by [Jones et al., 1985] and [Mohammad et al., 2012], however the sample sizes used to calculate normal values were very small ( 100 and 34 respectively).

The data used in this thesis is provided by Zentrum für ambulante Rehabilitation Graz (ZARG). ZARG is a center for out-patient rehabilitation. Currently, ZARG uses the suggested normal values for the maximum workload from [Wonisch et al., 2008], but they are interested in new approaches for normal values. Note that ZARG performs an extra ergometry in addition to suggested guidelines at intermediate examination of stage III.

The aims of this thesis are 1) to evaluate the presently used model in Austria and to develop new models to calculate the normal values of maximum workload ( $n=28625$ ) and 2) to calculate the normal values of maximum workload of the entry examination for stage II $(n=779)$ and stage III $(n=674)$ of cardiac out-patient rehabilitation and the expected improvement in maximum workload during these stages (stage II: $n=644$ and stage III: $n=787$ ).

For answering these questions, statistical methods are used. For getting an overview about the data, an exploratory data analysis is utilized. For deriving normal values, regression trees as well as a regression analysis is done. For finding the best model, variable selection is used.

In Chapter 2 there is an overview about the medical background. Chapter 3 gives an introduction about the statistical methods used in this thesis. Afterwards Chapter 4 deals with the data preparation and shows the final data which are analyzed in the further thesis. Chapter 5 gives an exploratory data analysis both univariate and multivariate. The first research question to derive normal values for the maximum workload, is answered in Chapter 6. Chapter 7 analyzes the data of cardiac out-patient rehabilitation. Finally, Chapter 8 contains a conclusion and outlook for further research.

## Chapter 2

## Medical literature overview

In this chapter, a short overview of the relevant medical topics is given. This starts with cardiovascular diseases, risk factors for cardiovascular diseases, cardiovascular stress testing and medications used in treatment of cardiovascular diseases.

### 2.1 Cardiovascular diseases

The cohort used for the analysis in this thesis consists of patients with different diagnoses such as coronary artery diseases, arrhythmias and fibrillation, conduction disorders and valvular heart diseases. Some of these diseases are explained here in short:

Coronary Artery Disease (CAD) ([DeSilva, 2013, Chapter 3]): Coronary artery disease or ischemic heart diseases are caused due to blockage or narrowing of coronary arteries due to plaques resulting in reduction or complete obliteration of blood to heart muscles. The disease diagnosis, which falls under this category in our cohorts are CAD, myocardial infarction, atherosclerosis, stenosis etc.

Cardiac arrhythmias ([DeSilva, 2013, Chapter 6]): The group of disorders due to irregular rhythm and rate of heartbeat. The heart rate could be too fast or too slow, or the rhythm is irregular. The diagnosis from our cohort, which falls under this category are ventricular tachycardia, atrial fibrillation, fibrillation arrhythmias etc.

Conduction disorders ([DeSilva, 2013, Chapter 6]): The group of cardiac disorders caused due to improper progression of electrical impulses through the heart, or complete blockage thereof. A diagnosis such as disturbance of conduction left bundle branch block, sinoatrial block, atrioventricular blocks from our cohort, falls under this category.

Valvular heart diseases ([DeSilva, 2013, Chapter 4]): It is caused by malfunctioning or nonfunctioning of one or more heart valves. This includes regurgitation - leakage of blood back into the heart chambers and stenosis - due to thickening, stiffening or fusion of valve flaps resulting in failure in the opening of heart valves completely. The diagnoses, which fall under this category are aortic insufficiency, aortic stenosis, mitral insufficiency, mitral regurgitation, tricuspid insufficiency, tricuspid stenosis etc.

### 2.2 Risk factors for cardiovascular diseases

Conventionally, older age is associated with an increased risk of heart diseases, over 45 years in men and 55 years in women. In addition, family history of early heart diseases put an individual at additional risk. Other risk factors for heart diseases are obesity, high blood pressure, high cholesterol level etc. Obesity is associated with increased risk of vascular risks. Waist circumference, waist-to-high-ratio (WHR) and body mass index (BMI) are the measures of obesity. The surveys indicate that there is a coherence between the waist circumference and the risk of getting a heart attack (see e.g. [De Koning et al., 2007]). Increasing risks arise for the waist circumference of more than 80 cm for women and more than 94 cm for men. A better measurement than the waist circumference is the WHR, which is the quotient between the waist circumference and the height. If this value is above 0.95 for men and above 0.8 for women, they will have a high cardiovascular risk. BMI is calculated from body weight and height by the formula

$$
B M I\left[k g / \mathrm{m}^{2}\right]=\frac{\text { weight }[\mathrm{kg}]}{\operatorname{size}[\mathrm{m}]^{2}}
$$

and is an estimate of body fat. Values above 25 identify overweight and above 30 obesity [Han et al., 1995].

High blood pressure is defined as systolic blood pressure $>140 \mathrm{mmHg}$ and diastolic blood pressure $>90 \mathrm{mmHg}$. It increases the risk for a variety of cardiovascular diseases. High levels of blood cholesterol are associated with greater risk of heart diseases. Total cholesterol level is the sum of three components HDL cholesterol, LDL cholesterol and $20 \%$ of triglycerides. HDL cholesterol is, because of its higher level of proteins, considered as good cholesterol. LDL and VLDL are considered as bad cholesterol because of their high level of cholesterol and increased levels are associated with a substantial increase in the risk of heart diseases. Total cholesterol level > $240 \mathrm{mg} / \mathrm{dL}$, LDL level $>160 \mathrm{mg} / \mathrm{dL}$ and triglycerides $>200 \mathrm{mg} / \mathrm{dL}$ are considered high whereas HDL levels $<40 \mathrm{mg} / \mathrm{dL}$ are considered as a major risk factor for heart diseases [Nelson, 2014].

### 2.3 Maximal cardiac exercise stress testing

Maximal exercise stress testing (ergometry) is a noninvasive way used to assess the diagnostic and prognostic information of cardiovascular diseases, specifically coronary artery disease (CAD). It studies the physical work activity, including that performed by specific muscles or muscle groups. The testing may involve ergometers such as stationary bicycles, treadmills, rowing machines, arm ergometer and monitoring of cardiac activities by electrocardiography and blood pressure monitoring [Pina et al., 1995]. Such tests involve exercising at several workloads or exercise intensities/difficulties, during which cardiovascular and respiratory measurements are recorded. Depending on the rationale for testing, the type of test employed, and the health and fitness status of the individual taking part, exercise stress tests might terminate at volitional exhaustion, upon observation of a particular clinical symptom, or at some other predetermined outcome measure [Turner, 2013].

### 2.4 Normal values for the maximum workload of maximal cardiac exercise stress testing

The articles addressing the normal values of parameters such as resting oxygen consumption, the maximal oxygen consumption, the maximum workload and the maximal heart rate obtained during the exercise stress testing are abundant (see e.g. [Koch et al., 2009], [Luks et al., 203] and [Brown et al., 2005]). Many articles focus on the prediction of the maximal oxygen consumption, while only few deal with the prediction of the maximum workload. However, this thesis explicitly deals with the maximum workload during ergometry.

In the Austrian practice guidelines for ergometry [Wonisch et al., 2008], the maximum workload is calculated separately for males and females using the following model. First the body surface area is calculated with the Du Bois formula (see [Du Bois and Du Bois, 1916])

$$
B S A\left[\mathrm{~m}^{2}\right]=0.007148 \text { workload }[\mathrm{kg}]^{0.425} \text { height }[\mathrm{cm}]^{0.725} .
$$

followed by actual calculation of the maximum workload.
Formula for the maximum workload for men

$$
W L_{\max }[W]=6.773+136.141 B S A\left[m^{2}\right]-0.916 B S A\left[m^{2}\right] \text { age }[\text { years }] .
$$

Formula for the maximum workload for women

$$
W L_{\max }[W]=3.933+86.641 B S A\left[m^{2}\right]-0.346 B S A\left[m^{2}\right] \text { age }[\text { years }] .
$$

In addition to the Du Bois formula, the body surface area can be calculated using other formulas; for the calculation of the body surface we refer to [Verbraecken et al., 2006].

There also exist other models to predict the maximum workload (see e.g. [Nogueira and Pompeu, 2006]), but most of them use just small sample sizes. In [Jones et al., 1985], the maximum workload is calculated using
$W L_{\max }[\mathrm{kpm} / \mathrm{min}]=20.4$ height $[\mathrm{cm}]-8.74$ age $[$ years $]-288$ gender ${ }^{1} 1-1.909 \mathrm{kpm} / \mathrm{min}^{1}$.
However, these values are calculated using 50 males and 50 females constituting 100 ergometries. In Mohammad et al., 2012] the maximum workload is predicted with a regression. They developed two formulas

$$
W L_{\max }[W]=-436-1.2 \text { age }[\text { years }]+1.8 \text { weight }[\mathrm{kg}]
$$

and

$$
W L_{\max }[W]=-436+3.6 \text { height }[\mathrm{cm}] .
$$

This study was a pilot study and involved only 34 participants from Iran.

[^0]
### 2.5 Medications used in the treatment of cardiovascular diseases

There are many medications used in the treatment of cardiovascular diseases, however, in this thesis only two main drugs, beta-blockers and statins are considered for further evaluation of normal values of maximum workload.

Beta blockers are the group of drugs used to manage high blood pressure and other cardiac ailments. Cardioselective beta blockers are Carvedilol, Dilatrend, Hemangiol, Inderal, Sotacor, Sotahexal and Sotastad. Non cardioselective beta blockers are Atehexal, Atenolan, Atenolol, Beloc, Bilokord, Bisocor, Bisoprolol, Bisostad, Brevibloc, Concor, Esmolol, Hypoloc, Lanoc, Metohexal, Metoprolol, Metoprololsuccinat, Nebivolol, Nomexor, Rapibloc, Rivacor, Seloken and Tenormin.

Statins are the group of compounds used to reduce the lipid levels hence reducing the risk of heart diseases. The types of statins are Atorvadivid, Atorvalan, Atorvastatin, Atozet, Crestor, Fluvastatin, Gerosim, Inegy, Lovastatin, Nyzoc, Panchol, Pravastatin, Simvastad, Simvarcana, Simvastatin, Simvatin, Sortis and Zocord.

## Chapter 3

## Statistical literature overview

The aim of this chapter is to provide an overview of basic statistics used in analysis of the data in this thesis. Theoretical description of each statistical topic is followed by an example in the statistical programming language $R$. The remainder of this chapter is organized as follows: Section 3.1 contains an introduction of R. Section ?? deals with the exploratory data analysis. Section 3.3 gives an overview of multiple linear regression. Finally in Section 3.4 the variable selection for multiple linear regression is clarified and in Section 3.5 dummy regression is explained. The following notation is used in this chapter: The observations are notated by $x_{1}, x_{2}, \ldots, x_{n}$ and the ordered observations are notated by $x_{(1)} \leq \cdots \leq x_{(n)}$.

### 3.1 Statistical programming language $\mathbf{R}$

$R$ is a free language and environment for statistical computing and graphics. There exist different implementations of R for Linux, Windows and MacOS. $R$ is a highly extendable environment used for linear and nonlinear modelling, timeseries analysis, classification and clustering etc. Moreover, R provides a high flexibility to plot well-designed publication-quality graphics including mathematical symbols and formulas ([R Core Team, 2017]).

There are several statistical books which use R. E.g. [Wollschläger, 2010] contains a good introduction and the installation guides. [Faraway, 2009] explains use of R to generate linear models. [Muche et al., 2011] uses Microsoft Excel combined with the Add-In 'RExcel', with which R can be used within Excel. [Ramachandran and Tsokos, 2014] provides computer examples of many statistical programs including R for each statistical topic. Additional information about R is available on [Cornelissen, 2018] and for information about the package ggplot2, which is used in this thesis, see [Wickham, 2009].

### 3.2 Exploratory data analysis

Exploratory data analysis (EDA) is a use of tools of the descriptive statistics to summarize and to find structures and coherences in the data. With the help of these methods, patterns and irregularities in one- and multidimensional data sets can be found, in addition, the information about the dispersion, symmetry,
concentration, and outliers can be obtained (see for example Akkerboom, 2008, Chapter 9], [Burkschat et al., 2012, Chapter 1] or [Fahrmeir et al., 2016, Chapter 2]).

The EDA can be classified in two different ways. The first approach is to classify the EDA in univariate and multivariate analysis. Often as a first step, an univariate analysis is performed in which, as the name suggests, each variable is investigated separately. In a second step the relationship between two or more variables can be analyzed by using multivariate analysis ([Fahrmeir et al., 2016, Chapter 2], [Cleff, 2014, Chapter 3]).

In the second approach, the EDA can be classified by graphical methods and methods involving the calculation of numerical summaries. Examples for graphical methods of the EDA are histograms, box plots, quantile-quantile plots and scatter plots. Examples for methods involving the calculation of numerical summary measures are means, standard deviations and correlation coefficients (see for example [Devore and Berk, 2012, Chapter 1]).

In the following subsections, EDA methods used in the thesis are explained. For this purpose, after explanation an example is given. For this example, the data of patients between the age of 30 and 60 years in year 2016 is analyzed

### 3.2.1 Numerical summary measures

Numerical summary measures can be used to characterize the data set. They can be characterized in measures of location and measures of variability. The following definitions for these measures are taken from [Devore and Berk, 2012, Chapter 1].

## Mean

The sample mean $\bar{x}$ of observations $x_{1}, x_{2}, \ldots, x_{n}$ is given by $\bar{x}=\frac{1}{n} \sum_{i=1}^{n} x_{i}$. To calculate the mean with R , the command mean can be used.

Example 3.1. The calculation of the mean of the variable workload_max of table exampledata can be done in R in the following way:

```
mean(exampledata$workload_max)
## [1] 179.3922
```

Therefore, the mean of the maximum workload of the ergometries is 179 W .

## Median

The sample median $\tilde{x}$ is indeed the middle value of the ordered observations, i.e. it divides the data set into two parts of equal size. If $n$ is odd, then it is the single middle value $x_{\left(\frac{n+1}{2}\right)}$, and if $n$ is even, then it is the average of the two middle values, i.e. $\frac{1}{2}\left(x_{\left(\frac{n}{2}\right)}+x_{\left(\frac{n}{2}+1\right)}\right)$. To calculate the median with R , the command median can be used.

Example 3.2. The calculation of the median of the variable workload_max of table exampledata can be done in R in the following way:

```
median(exampledata$workload_max)
## [1] 180
```

Therefore, the median of the maximum workload of all ergometries is 180 W .

## Quartiles

The quartiles divide the data set into four equal parts. The first quartile $Q_{1}=$ $q_{0.25}$ separates the lower quarter from the upper three-quarters, the second quartile $Q_{2}=q_{0.5}$ is equivalent to the median and the third quartile $Q_{3}=q_{0.75}$ constitutes the upper quarter of the data set. To calculate the quartiles with $R$ the command quantile can be used.

Example 3.3. The calculation of the quartiles of the variable workload_max of table exampledata can be done in R in the following way:

```
quantile(exampledata$workload_max)
\begin{tabular}{lllllr} 
\#\# & \(0 \%\) & \(25 \%\) & \(50 \%\) & \(75 \%\) & \(100 \%\) \\
\#\# & 30 & 142 & 180 & 210 & 400
\end{tabular}
```

Therefore the minimum of the maximum workload is 30 W , the maximum is 400 W and the median is 180 W (as calculated above). Moreover we know that $25 \%$ of the maximum workload is less than 142 W and $25 \%$ of the maximum workload is higher than 210 W .

## Inter quartile range

The inter quartile range (IQR) is defined as $Q_{3}-Q_{1}$. To calculate the IQR with $R$ the command IQR can be used.

Example 3.4. The calculation of the IQR of the variable workload_max of table exampledata can be done in R in the following way:

```
IQR(exampledata$workload_max)
## [1] 68
```

Therefore the range of $50 \%$ of the data around the median is 68 W .

## Quantiles

The quantiles are a generalization of the quartiles with the property that at least a relative share of $p$ data are smaller or equal to $q_{p}$ and maximal a relative share of $(1-p)$ is bigger than $q_{p}$ (see for example [Cleff, 2014, Chapter 3]). In R it can be done with the command quantile, but additional percentages for calculating the quantiles have to be defined.

Example 3.5. The calculation of the $5 \%$-and $95 \%$-quantiles of the above mentioned variable workload_max of table exampledata can be done in R in the following way:

```
quantile(exampledata$workload_max, probs=c(0.05, 0.95))
## 5% 95%
## 100 262
```

Therefore 5\% of the ergometries have a maximum workload of less than 100 W and $5 \%$ of them have a maximum workload of more than 262 W .

## Variance and standard deviation

The sample variance $s^{2}$ is given by $\frac{1}{n-1} \sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2}$. To calculate the variance with R the command var can be used.

The sample standard deviation $s$ is the square root of the variance, i.e. $\sqrt{s^{2}}$. To calculate the standard deviation with R the command sd can be used.

Example 3.6. The calculation of the variance and standard deviation of the variable workload_max of table exampledata can be done in R in the following way:

```
var(exampledata$workload_max)
## [1] 2662.902
sd(exampledata$workload_max)
## [1] 51.60331
```

Therefore the variance of the maximum workload is 2662.9 W and the standard deviation is 51.6 W .

### 3.2.2 Box plot

A box plot is a pictorial summary used to describe most prominent features of data sets. These include the center, the spread, the extend and nature of any deviation from symmetry and the identification of outliers, which are observations that are located unusually far from the main body of the data (see for example [Devore and Berk, 2012, Chapter 1]).

There exist several variations of box plots. The box plots which are created in this thesis provide the following information: The bottom and the top of the boxes are the first and third quartiles $q_{0.25}$ and $q_{0.75}$. The notches display a $95 \%$ confidence interval around the median $\tilde{x}$, i.e. the true median is with a probability of $95 \%$ covered by this interval. The width of the boxes is proportional to the number of observations. These are also written in the middle of the box. The upper whisker is defined as $\min \left(\max (x), Q_{3}+1.5 I Q R\right)$ and the lower whisker is $\max \left(\min (x), Q_{1}-1.5 I Q R\right)$. The points which are less than $Q_{1}-1.5 I Q R$ or
greater than $Q_{3}+1.5 I Q R$ are classified as outliers and represented by points in the box plots.

The creation of a box plot can be done in R in different ways. The easiest way is to use the command boxplot. With the package ggplot2 and the command geom_boxplot more adjustments can be done.

Example 3.7. This example shows two possibilities to create a box plot of the variable workload_max of table exampledata in R.

```
#Variant 1:
boxplot(exampledata$workload_max)
#Variant 2:
#Selection of the data
ggplot(exampledata, aes(x=gender, y=workload_max)) +
    #Box plot with notches and variable width
    geom_boxplot(notch=TRUE, varwidth=TRUE)+
    #Addition of the number of observations above the median
    stat_summary(fun.data = function(workload_max)
        {return(c(y = median(workload_max)+8,
                            label = length(workload_max)))}, geom = "text")+
    #Title and axis label
    ggtitle("Box plot")+
    labs(y="maximum workload [W]")
```


(a) Variant 1: Standard box plot in R

(b) Variant 2: Box plot with the package ggplot2 and additional adjustments

Figure 3.1: Box plots for the variable maximum workload

Figure 3.1(a) shows the standard box plot in R. Without an additional package just limited adjustments can be done. With the help of package ggplot2 many additional characteristics can be adjusted, as in Figure 3.1 (b) shown. Here the box plots for the maximum workload are separated by gender by using
aes ( $\mathrm{x}=\mathrm{gender}, \mathrm{y}=$ workload_max). The width of the boxes are correlated to the number of observations with varwidth=TRUE and additionally the number of observations is given with the command stat_summary. There are additional notches, which represent $95 \%$-confidence intervals around the median, done with notch=TRUE.

### 3.2.3 Bar plot

In a bar plot rectangular bars represent categorical variables. The length of these bars are proportional to the number of observations in the corresponding value of the categorical variable (see e.g. [Akkerboom, 2008, Chapter 7]).

Again like for the box plot, the creation of a bar plot can be done in R in different ways. The easiest way is to use the command barplot. With the package ggplot2 and the command geom_bar more adjustments can be done.

Example 3.8. This example shows two possibilities to create a bar plot of the variable gender of table exampledata in R.

```
#Variant 1:
barplot(table(exampledata$gender))
#Variant 2:
#Selection of the data
ggplot(data=exampledata) +
    #Bar plot
    geom_bar(aes(factor(gender)), stat="count",
            position = position_dodge(width=0.9))+
    #Addition of the number of observations above the bars
    geom_text(aes(x=gender, label=..count..),stat="count",
            position = position_dodge(width = 0.8), vjust = -0.6)+
    #Title and axis label
    ggtitle('Barplot of the gender')+
    labs(x='gender')
```

Figure 3.2(a) shows the standard bar plot in R. The bar plot with the help of package ggplot2 is shown in Figure 3.2 (b). Here the number of observations is given with the command geom_text.

### 3.2.4 Histogram and density plot

In a histogram the $n$ values $x_{1}, \ldots, x_{n}$ of a sample will be summarized in $k$ uniform classes. For each class the frequency is determined and above each class interval a rectangle is drawn whose height is the corresponding frequency.

In order to create the histogram, the ordered data $x_{(1)} \leq \cdots \leq x_{(n)}$ are used to calculate the total area of the sample $\left[x_{(1)}, x_{(n)}\right]$. This area is divided into $k$ uniform classes $\left[a_{0} \leq x_{(1)}, a_{1}\right),\left[a_{1}, a_{2}\right), \ldots,\left[a_{(k-1)}, a_{k} \geq x_{(n)}\right]$, which all have the same width $b$ and the height $h_{j}$ with


Figure 3.2: Number of ergometries seperated by gender

$$
h(x)= \begin{cases}h_{j}, & \text { if } a_{j-1} \leq x<a_{j}, j=1, \ldots, k ; a_{j}-a_{j-1}=b \\ 0, & \text { else. }\end{cases}
$$

The height $h_{j}$ can be scaled through using the absolute frequency $n_{j}$, relative frequency $\frac{n_{j}}{n}$ or density $\frac{n_{j}}{n b}$. With defining the height of the rectangles as the density, classes with different widths can be used ([Cleff, 2014, Chapter 3]), [Devore and Berk, 2012, Chapter 1] and [Toutenburg et al., 2009, Chapter 2]).

Note, that the selection of suitable intervals is important, because different class widths have a big influence on the appearance of the histogram ([Cleff, 2014, Chapter 3]).

Additional information in a histogram can be obtained, if the mean is marked with a line.

Like before, the creation of a histogram can be done in R in different ways. The easiest way is to use the command histo. With the package ggplot2 and the command geom_histogram more adjustments can be done.

Example 3.9. This example shows two possibilities to create a histogram of the variable workload_max of table exampledata in R.

```
#Variant 1:
hist(exampledata$workload_max)
#Variant 2:
#Selection of the data
ggplot(exampledata, aes(x=workload_max, fill=gender)) +
    #Histogram
    geom_histogram(aes(y=..density..), position="identity",
    alpha=0.5,binwidth=20)+
    #Additional line to show the mean
```

```
geom_vline(data=ddply(exampledata, "gender", summarise,
            grp.mean=mean(workload_max)),
    aes(xintercept=grp.mean, color=gender),
    linetype="dashed")+
#Title and axis label
ggtitle("Histogram plot")+
labs(x="maximum workload(W)", y = "density")
```


(a) Variant 1: Standard histogram in R

(b) Variant 2: Histogram with the package ggplot2 and additional adjustments

Figure 3.3: Histogram for the variable maximum workload
Figure 3.3(a) shows the standard histogram in R. The histogram with the help of package ggplot2 is shown in Figure 3.3(b). Here the histograms are separated by the gender and the additional dashed lines mark the means.

Histograms can be approximated with a smooth curve, the so-called density plot (see [Fahrmeir et al., 2016, Chapter 2]). The density plot visualizes the distribution of data over a continuous interval of a variable (see for example [Devore and Berk, 2012, Chapter 4]).

The creation of a density plot can be done in R in different ways. The easiest way is to use the command density and plot it with the command plot. With the package ggplot2 and the command geom_density more adjustments can be done.

Example 3.10. This example shows two possibilities to create a density plot of the variable workload_max of table exampledata in R.

```
#Variant 1:
plot(density(exampledata$workload_max))
#Variant 2:
#Selection of the data
ggplot(exampledata, aes(x=workload_max, fill=gender))+
```

```
#Density plot
geom_density(alpha=0.6)+
#Title and axis label
ggtitle("Density plot")+
labs(x="maximum workload(W)", y = "density")
```



Figure 3.4: Density plot for the variable maximum workload
Figure 3.4 (a) shows the standard density plot in R. The density plot with the help of package ggplot2 is shown in Figure 3.4(b), where the density plots are separated by the gender.

Note, histogram and density plot can be also combined in one plot, as shown in the Figures in Chapter 6

### 3.2.5 Plot of the empirical distribution function

The empirical distribution function (see e.g. [Fahrmeir et al., 2016, Chapter 2]) of a random sample is defined as

$$
F_{n}(x)= \begin{cases}0, & \text { if } x<x_{(i)} \\ \frac{i}{n}, & \text { if } x_{(i)} \leq x_{(i+1)}, i=1, \ldots, n-1 \\ 1, & \text { if } x_{(n)} \leq x\end{cases}
$$

In the corresponding plot the shifted step function $F_{n}^{s}(x)=F_{n}(x)-\frac{1}{2 n}$ for $x_{(i)} \leq$ $x<x_{(x+1)}$ is presented instead of plotting directly $F_{n}(x)$.

The easiest way to create the plot of the empirical distribution function in R is to use the command ecdf and plot it with the command plot. With the package ggplot2 and the command stat_ecdf more adjustments can be done.
Example 3.11. This example shows two possibilities to plot the empirical distribution function of the variable workload_max of table exampledata in R.

```
#Variant 1
plot(ecdf(exampledata$workload_max))
#Variant 2:
#Selection of the data
ggplot(exampledata, aes(x=workload_max))+
    #Empicial distribution function
    stat_ecdf(geom = "point")+
    stat_function(fun = pnorm, n = 101, args =
                        list(mean = mean(exampledata$workload_max),
                        sd = sd(exampledata$workload_max)),
                        colour='red')+
    #Title and axis label
    ggtitle("Plot of the empirical distribution function")+
    labs(x="maximum workload(W)", y="Empirical distibution function")
```


(a) Variant 1: Standard plot of the empirical distribution function in R

(b) Variant 2: Plot of the empirical distribution function with the package ggplot2 and additional adjustments

Figure 3.5: Plot of the empirical distribution function for the variable maximum workload

Figure 3.5 (a) shows the standard plot for the empirical distribution function in R. The plot for the empirical distribution function with the help of package ggplot2 is shown in Figure 3.5(b). It contains also the distribution function of the corresponding normal distribution with mean $\bar{x}$ and standard deviation $s d$.

### 3.2.6 Quantile-quantile plot

In a Quantile-quantile plot ( $\mathrm{Q}-\mathrm{Q}$ plot), the distribution of two variables is compared by plotting their quantiles against each other (see Kohn and Öztürk, 2013, Chapter 15]). Often this plot is used to compare the distribution of a sample with
the theoretical distribution, i.e. the ordered sample values $x_{(i)}$ against the theoretical quantile $F^{-1}\left(\frac{i}{n+1}\right)$, with $i=1, \ldots n$. Therefore the deviation from the reference line, a line with a slope of $45^{\circ}$, can be evaluated.

The easiest way to create a Q-Q plot to compare the empirical quantiles with the quantiles of the standard normal distribution $N(0,1)$ is to use the command qqnorm to create the points and the command qqline to create the line. With the package ggplot2 the command stat_qq can be used to create the dots and the command geom_abline can be used to create the line.

Example 3.12. This example shows two possibilities to make a Q-Q plot of the variable workload_max of table exampledata in R.

```
#Variant 1:
qqnorm(exampledata$workload_max)
qqline(exampledata$workload_max)
#Variant 2:
# Find the 1st and 3rd quartiles
y <- quantile(exampledata$workload_max, c(0.25, 0.75), type=5)
# Find the matching normal values on the x-axis
x <- qnorm( c(0.25, 0.75))
# Compute the line slope
slope <- diff(y) / diff(x)
# Compute the line intercept
int <- y[1] - slope * x[1]
#Selection of the data
ggplot(exampledata, aes(sample=workload_max))+
    #QQ-plot
    stat_qq(geom = "point")+
    geom_abline(intercept=int, slope=slope,colour='red')+
    #Title
    ggtitle("Q-Q plot")
```

Figure 3.6(a) shows the standard Q-Q plot in R. The Q-Q plot with the help of package ggplot2 is shown in Figure 3.6 (b). Here the line has to be calculated separately. The plot indicates a remarkable deviation from the normal distribution.

### 3.2.7 Scatter plot

A scatter plot uses Cartesian coordinates to display values of two variables (see [Devore and Berk, 2012, Chapter 12]). Therefore it belongs to the multivariate analysis. The resulting point cloud gives information about the correlation between these variables (see e.g. [Pruscha, 2015, Chapter 1]).

The easiest way to create the scatter plot in R is to use the command plot. With the package ggplot2 the command geom_point can be used to create the dots. To add an additional regression line the command geom_smooth can be used. For this function different methods like linear regression or generalized


Figure 3.6: Q-Q plot for the variable maximum workload
additive model, which is the standard method for more than 1000 observations, can be applied.

Example 3.13. This example shows two possibilities to make a scatter plot of the variables age and workload_max of table exampledata in R.

```
#Variant 1:
plot(exampledata$age,exampledata$workload_max)
```

```
#Variant 2:
```

\#Variant 2:
\#Selection of the data
\#Selection of the data
ggplot(exampledata, aes(age,workload_max))+
ggplot(exampledata, aes(age,workload_max))+
\#Scatter plot
\#Scatter plot
geom_point()+
geom_point()+
\#Regression line
\#Regression line
geom_smooth()+
geom_smooth()+
\#Title
\#Title
ggtitle("Scatter plot")+
ggtitle("Scatter plot")+
labs(x="age", y="maximum workload(W)")

```
    labs(x="age", y="maximum workload(W)")
```

Figure 3.7(a) shows the standard scatter plot in R. The scatter plot created with the help of package ggplot2 is shown in Figure 3.7(b). Here additionally a regression line including a $95 \%$-confidence interval around it is added.

### 3.2.8 Correlation coefficient

A measurement for the linear correlation between two samples $x$ and $y$ is the (Pearson) correlation coefficient (see e.g. [Devore and Berk, 2012, Chapter 5],

(a) Variant 1: Standard scatter plot in R

(b) Variant 2: Scatter plot with the package ggplot2 and additional adjustments

Figure 3.7: Scatter plot for the variables age and maximum workload
[Cleff, 2014, Chapter 4]). The correlation coefficient is defined by
$r_{x, y}=\frac{s_{x y}}{s_{x} s_{y}}=\frac{\frac{1}{n-1} \sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)\left(y_{i}-\bar{y}\right)}{\frac{1}{n-1} \sqrt{\sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2} \sum_{i=1}^{n}\left(y_{i}-\bar{y}\right)^{2}}}=\frac{\sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)\left(y_{i}-\bar{y}\right)}{\sqrt{\sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2} \sum_{i=1}^{n}\left(y_{i}-\bar{y}\right)^{2}}}$.
$s_{x y}$ is the co-variance between $x$ and $y, s_{x}$ is the standard deviation of $x$ and $s_{y}$ is the standard deviation of $y$.

For the Pearson correlation coefficient the following properties hold:

- r is normalized, i.e. $-1 \leq r \leq+1$.
- If $r>0$ then there is a positive linear correlation, if $r<0$ then there is a negative linear correlation and if $r=0$ then there is no linear correlation.
- If $x$ and $y$ come from independent random variables $X$ and $Y$, then $r \approx 0$, the inversion is not valid in general. Two variables can be uncorrelated, but dependent because of a nonlinear relationship.

In R the Pearson correlation coefficient can be calculated with the function $\operatorname{cor}(\mathrm{x}, \mathrm{y})$. Additionally it is possible to create correlation matrices for several variables. This can be done for example with the package lattice [Sarkar, 2008] and the command corrgram.

Example 3.14. This example shows how to calculate the correlation between two variables and how to create a correlation matrix between several variables in $R$.

```
cor(exampledata$workload_max,exampledata$age)
## [1] -0.2815862
```

The correlation between the maximum workload and age is -0.28 , consequently they are negatively correlated.

```
corrgram(subset(exampledata, select = c("weight","height","age",
    "workload_max")),
    lower.panel = panel.ellipse, upper.panel = panel.pie)
```



Figure 3.8: Correlation matrix between the variables weight, height, age and maximum workload

Figure 3.8 shows the correlation matrix with the help of package lattice. The variables are written on the diagonal line.

The lower triangle matrix shows both ellipses and loess lines ${ }^{11}$. Long, narrow ellipses represent high correlations while circular ellipses represent low correlations.

The value of the correlation can be deducted from the upper triangle matrix. For a positive correlation, blue color is used and the correlation is seen clockwise. A full clock represents a correlation of 1 . On the contrary to this a clock with a negative correlation is colored red and counter clockwise.

### 3.3 Multiple linear regression

In general a regression analysis is a statistical method to model the relationship between two or more variables to gain information about one of them through knowing the values of the other(s). In the simple linear regression the depended or response variable is predicted by a single independent, explanatory or predictor variable. However, in most cases more than one predictor variable is useful. In this case we use multiple linear regression (see e.g. [Devore and Berk, 2012, Chapter 12], [Kleinbaum et al., 1998, Chapter 8], [Fahrmeir et al., 2008, Chapter 2], [Sheather, 2009, Chapter 5], [Gareth et al., 2014, Chapter 3]).

[^1]
### 3.3.1 Multiple linear regression model

The standard model for multiple linear regression (see [Sheather, 2009. Chapter 5] or [Bingham and Fry, 2010, Chapter 3]) is the following:

$$
Y_{i}=\beta_{0}+\beta_{1} x_{i 1}+\ldots+\beta_{p} x_{i p}+\epsilon_{i}, \quad i=1, \ldots, n,
$$

with
$Y_{1}, \ldots, Y_{n} \ldots$ observed metric variables
$x_{1 j}, \ldots, x_{n j} \ldots$ deterministic values of the variables $X_{j}$
$\epsilon_{1}, \ldots, \epsilon_{n} \ldots$ unobserved random variables, which are independent and identically distributed with $E\left(\epsilon_{i}\right)=0, \operatorname{Var}\left(\epsilon_{i}\right)=\sigma^{2}$ and $\operatorname{Cov}\left(\epsilon_{i}, \epsilon_{j}\right)=0$ for $i \neq j$
$\beta_{0}, \ldots, \beta_{p} \ldots$ coefficients of the regression
The matrix notation of this is:

$$
\begin{aligned}
Y & =\beta_{0} 1+\beta_{1} x_{1}+\ldots+\beta_{p} x_{p}+\epsilon \\
& =X \beta+\epsilon
\end{aligned}
$$

with
$Y=\left(Y_{1}, \ldots, Y_{n}\right)^{T} \ldots n \times 1$-vector of dependent observations
$X \ldots n \times k$-design matrix (with a full column rank)
$\epsilon \ldots n \times 1$-vector of unobserved residuals
$\beta \ldots k \times 1$-parameter vector
With given values of the regressors, the $Y_{1}, \ldots, Y_{n}$ are independent with the expected value and variance

$$
\begin{aligned}
E\left(Y_{i}\right) & =\mu_{i}=\beta_{0}+\beta_{1} x_{i 1}+\ldots+\beta_{p} x_{i p}, \quad i=1, \ldots, n \\
\operatorname{Var}\left(Y_{i}\right) & =\sigma^{2}, \quad i=1, \ldots, n .
\end{aligned}
$$

With the assumption of normal distribution for the error values

$$
\epsilon_{i} \sim N\left(0, \sigma^{2}\right), \quad i=1, . ., n
$$

follows the normal distribution for the target variable, therefore

$$
Y_{i} \sim N\left(\mu_{i}, \sigma^{2}\right), \quad i=1, \ldots, n .
$$

Note, that the dependent variable is a linear combination of the parameters, but is not necessarily linear in the independent variables [Kleinbaum et al., 1998, Chapter 8]. For example the model with all possible first- and second order terms

$$
Y=\beta_{0} 1+\beta_{1} x_{1}+\beta_{2} x_{2}+\beta_{3} x_{1}^{2}+\beta_{4} x_{2}^{2}+\beta_{5} x_{1} x_{2}+\epsilon
$$

can be rewritten as

$$
Y=\beta_{0} 1+\beta_{1} x_{1}+\beta_{2} x_{2}+\beta_{3} x_{3}+\beta_{4} x_{4}+\beta_{5} x_{5}+\epsilon .
$$

In R for the linear regression the command lm can be used. Note that in R for high order terms and other nonlinear relations the function $I$ (.) and for interactions between variables the symbol : can be used.

Example 3.15. This example shows how to create a linear regression for the response variable workload_max and the predictor variables age, weight and height in R. Additionally the second order term age ${ }^{2}$ and interaction between weight and height are used in the regression.

```
regression_model=lm(workload_max ~ age+weight+height+I(age^2)+
    weight:height,data=exampledata)
```


### 3.3.2 Estimating the regression coefficients

The fitted regression model is given by

$$
\hat{Y}=\hat{\beta}_{0} 1+\hat{\beta}_{1} x_{1}+\ldots+\hat{\beta}_{p} x_{p} .
$$

The regression coefficients $\hat{\beta}_{0}, \ldots, \hat{\beta}_{p}$ can be determined with the least-squares method ([Kleinbaum et al., 1998, Chapter 8], [Devore and Berk, 2012, Chapter 12]). This method minimizes the sum of squares of the distances between the observed responses and those predicted by the fitted model, i.e.

$$
\operatorname{SSE}(\beta)=\sum_{i=1}^{n}\left(Y_{i}-\hat{Y}_{i}\right)^{2} \rightarrow \min _{\beta_{0}, \ldots, \beta_{p}}
$$

This difference is called as residual sum of squares, error sum of squares or sum of squares about regression.

Another possibility to estimate the regression coefficients is the maximum likelihood estimation (see [Fahrmeir et al., 2008, Chapter 3]). The likelihood function, under the assumption of normal distributed residuals, is given by

$$
L\left(y \mid \beta, \sigma^{2}\right)=\frac{1}{\left(2 \pi \sigma^{2}\right)^{\frac{n}{2}}} \exp \left(-\frac{1}{2 \sigma^{2}} S S E\right) .
$$

Therefore the Log-Likelihood function is

$$
\log L\left(y \mid \beta, \sigma^{2}\right)=-\frac{n}{2} \log \left(2 \pi \sigma^{2}\right)-\frac{1}{2 \sigma^{2}} S S E .
$$

One can see that maximizing the Log-Likelihood function leads to minimizing the SSE. This is because the constant and the factor in front of the SSE can be eliminated for the maximization and maximizing the negative SSE is equivalent to minimizing SSE. Therefore the least-squares method and the maximum likelihood estimation lead to the same result.

The maximum likelihood estimator of the variance $\sigma^{2}$ can be calculated by setting $\frac{\partial \log L\left(y \mid \beta, \sigma^{2}\right)}{\partial \sigma}$ to zero and is

$$
\hat{\sigma}^{2}=\frac{S S E}{n} .
$$

Because this is a biased estimator ${ }^{2}$, the unbiased estimator

$$
\tilde{\sigma}^{2}=\frac{S S E}{n-p}=M S E
$$

[^2]is used.
For receiving the regression coefficients of a linear regression model in R just the name of the model has to be typed. With the command summary before the name of the model, more information about the coefficients can be achieved.

The summary consists of the following parts:

## Call

The first part shows again the predictor variable and the response variables as seen before.

## Residuals

The next part shows the residuals. These are the differences between the actual observed response values and the response values that the model predicted, i.e. $Y_{i}-\hat{Y}_{i}$. For these residuals, five summary measures are given, i.e. the minimum, the first quartile, the median, the third quartile and the maximum. The residuals should be symmetrical distributed around the mean value 0 .

## Coefficients

The next part of the summary gives information about the coefficients of the model. Therefore, first, the coefficient estimates are given. The first one is the intercept and the others refer to the predictor variables. Additionally the standard error of the coefficients are given. This measures the average amount that the coefficient estimate varies from the actual average value of the response variable. Therefore the standard error should be low compared to its coefficients. For the $t$-value the coefficients estimate is divided by its standard error, therefore it should be far away from zero as this would indicate to reject the null hypothesis, and there is a relationship between the coefficient and the dependent variable. With this $t$-value, the $p$-value (in the R output $\operatorname{Pr}(>|t|)$ ) can be calculated. The $p$-value gives the probability that the null hypothesis is true. In our case the null hypothesis says that there is no relationship between the predictor and the response. Finally, the significance codes evaluate the $p$-values. For example, three stars refer to a highly significant $p$-value of less than 0.001 .

## Residual standard error

The residual standard error (RSE) is a measure of the quality of a linear regression fit. It is defined as the square root of the residual sum of squares SSE (see Subsection 3.3.3) and therefore should be small. The degree of freedom is the number of data points minus the number of parameters.

## Multiple R-squared, Adjusted R-squared

The coefficient of determination $R^{2}$ as well as the adjusted coefficient of determination $R_{a d j}^{2}$ are measures of how well the model is fitting the actual data. More information about these coefficients can be found in Subsection 3.3.3,

## F-Statistic

F-statistic is a good indicator of whether there is a relationship between the predictors and the response variables. The further the F-statistic is from 1 the better it is. However, how much larger the F-statistic needs to be, depends on both the number of data points and the number of predictors. Generally, when the number of data points is large, an F-statistic that is only a little bit larger than 1 is already sufficient to reject the null hypothesis, which says that there is no relationship between the predictor and the response variables. The reverse is true as if the number of data points is small, a large F-statistic is required to be able to ascertain that there may be a relationship between predictor and response variables. Additionally, the $p$-value for the test is given.

Example 3.16. In the last example the regression model was stored in the variable regression_model. To get the coefficients this variable has to be called:

```
regression_model
##
## Call:
## lm(formula = workload_max ~ age + weight + height + I(age^2) +
## weight:height, data = exampledata)
##
## Coefficients:
## (Intercept) age weight height
## -812.36511 3.66709 4.97133 5.40829
## I(age^2) weight:height
## -0.05335 -0.02832
```

As a result we can see the previously defined formula of the regression model and the calculated coefficients. Therefore the regression model is

```
workload_max \(=-812.37+3.67\) age +4.97 weight +5.41 height -0.05 age \(^{2}\)
    -0.03 weight : height.
```

The summary of the previously model provides the following information:

```
summary(regression_model)
##
## Call:
## lm(formula = workload_max ~ age + weight + height + I(age~2) +
## weight:height, data = exampledata)
##
## Residuals:
\#\# Min 1Q Median \(\quad\) 3Q \(\quad\) Max
## -144.019 -25.229 -0.348 23.652 185.211
##
## Coefficients:
```

```
## Estimate Std. Error t value Pr (>|t|)
## (Intercept) -812.36511 121.33092 -6.695 3.32e-11 ***
## age 3.66709 1.84674 1.986 0.047298 *
## weight 4.97133 1.39243 3.570 0.000371 ***
## height 5.40829 0.66814 8.095 1.42e-15 ***
## I(age^2) -0.05335 0.01949 -2.736 0.006303 **
## weight:height -0.02832 0.00792 -3.576 0.000363 ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 41.29 on 1177 degrees of freedom
## Multiple R-squared: 0.3624,Adjusted R-squared: 0.3597
## F-statistic: 133.8 on 5 and 1177 DF, p-value: < 2.2e-16
```

We see a considerable symmetrical distribution of the residuals. As mentioned above, the standard error should be small compared to the coefficients' estimate, which is the case in our example. The $t$-statistic values are relatively far away from zero and are considerably large relative to the standard error. The $p$-values are very close to zero and the significance codes show a high significance for all predictor variables. The residual standard error is 41.29 calculated with 1,177 degrees of freedom. We had 1,183 data points and 6 parameters. The coefficient of determination is 0.3624 and the adjusted coefficient of determination is 0.3597 . The F-statistic is 133.8 which is relatively larger than 1 , given the size of our data.

### 3.3.3 Analysis of variance and the coefficient of determination

The analysis of variance (ANOVA) provides an overall summary of a multiple regression analysis (see [Kleinbaum et al., 1998, Chapter 8]). The total sum of squares (SST) consists of the regression sum of squares (SSR) and the error sum of squares (SSE), i.e.

$$
\begin{array}{rlll}
S S T & = & \text { SSR } & + \text { SSE } \\
\sum_{i=1}^{n}\left(Y_{i}-\bar{Y}\right)^{2} & = & \sum_{i=1}^{n}\left(\hat{Y}_{i}-\bar{Y}\right)^{2} & +\sum_{i=1}^{n}\left(Y_{i}-\hat{Y}_{i}\right)^{2} .
\end{array}
$$

The mean of squares are defined as the sum of squares divided by the degree of freedom:

$$
\begin{aligned}
& M S T=\frac{S S T}{n-1} \\
& M S R=\frac{M S R}{p-1} \\
& M S E=\frac{M S E}{n-p}
\end{aligned}
$$

The sum of squares as well as the mean of squares can be calculated in R with the command anova. It presents the degree of freedom (df), the sum of squares (Sum Sq), the mean of squares (Mean Sq), the $F$-value, the $p$-value $(\operatorname{Pr}(>\mathrm{F})$ ) and the significance codes. It tests whether the model terms are significant.

Example 3.17. The ANOVA for the previous example in R is the following:

```
anova(regression_model)
## Analysis of Variance Table
##
## Response: workload_max
## Df Sum Sq Mean Sq F value Pr(>F)
## age 1 249572 249572 146.3661<2.2e-16 ***
## weight 1 301878 301878 177.0419< 2.2e-16 ***
## height 1 552022 552022 323.7438 < 2.2e-16 ***
## I(age~2) 1 15350 15350 9.0023 0.0027532 **
## weight:height 1 21803 21803 12.7870 0.0003632 ***
## Residuals 1177 2006926 1705
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

In this table the SSE is 46987470 . The SSR is the sum of the first five sum of squares, i.e. age to weight:height. Finally, the SST is the sum of all of them.

The coefficient of determination, which is a quantitative measure of how well the fitted model predicts the dependent variable, is defined as

$$
R^{2}=1-\frac{S S E}{S S T}=\frac{S S R}{S S T}
$$

The coefficient of determination $R^{2}$ lies between 0 and 1 . If it is equal to 1 , then the model fits perfect $(\mathrm{SSE}=0)$ and if it is equal to 0 , then there is no linear correlation (SSR=0).

Different models can just be compared under the following three assumptions (see [Fahrmeir et al., 2008, Chapter 3]):

1. In all models the same dependent variable $y$ is used, i.e. a comparison of models with objective criterion $y$ and $\log (y)$ is not possible.
2. In all models the number of regression coefficients is the same.
3. All models have a constant $\beta_{0}$.

Therefore, in general, different models cannot be compared with the coefficient of determination, because the coefficient of determination $R^{2}$ is dependent on the number of predictor variables. If the number of predictor variables gets height, then $R^{2}$ rises. It is therefore desirable to adjust the coefficient of determination. The adjusted coefficient of determination (see [Devore and Berk, 2012, Chapter 12]) is defined by

$$
R_{a d j}^{2}=1-\frac{M S E}{M S T}=1-\frac{n-1}{n-p} \frac{S S E}{S S T} .
$$

To display the coefficient of determination and the adjusted coefficient of determination from the summary of a linear model, the commands r.squared and adj.r.squared can be used.

Example 3.18. The summary of the previous model provides the following information:

```
summary(regression_model)$r.squared
## [1] 0.3623848
summary(regression_model)$adj.r.squared
## [1] 0.3596762
```


### 3.3.4 Diagnostics of the model

As mentioned before, several assumptions had to be made to use the multiple linear regression. The diagnostics of the model can be separated into the following parts (see [Faraway, 2009, Chapter 4]):

1. The error values are independent and identically normally distributed $\epsilon_{i} \stackrel{i i d}{\sim}$ $N\left(0, \sigma^{2}\right), \quad i=1, . ., n$
2. The structural part of the model $\hat{Y}=X \beta$ is correct.
3. Unusual observations, which do not fit the model and therefore might change the selection and fit of the model, should be identified.

## Constant variance

To identify a constant variance, the residual vs. fitted plots can be used. This plot is expected to appear random.

## Normality

For the normality check a Q-Q plot can be used. It will give a straight line if the errors are distributed normally.

## Correlated errors

To identify correlated errors a Scale-Location plot can be used. This plot is expected to appear random with no discernable patterns.

## Identification of unusual observations

To identify unusual observations the residual vs. leverage plot can be used. In this plot, the Cook's distance is marked to show which points have the greatest influence on the regression, i.e. are leverage points.

This diagnostics of the model can be done in R with the command plot.
Example 3.19. The diagnostics for the above example can be done in the following way:

```
plot(regression_model)
```



Figure 3.9: Diagnostic plot of the example linear regression model
In the first plot of Figure 3.9 the residuals are plotted against the predicted values. One can see that the variance is not constant. The second plot of Figure 3.9 shows a Q-Q plot of the standardized residuals. For small and big values there is a deviation from the line, i.e. there is a skinny positive and skinny negative tail. The third plot of Figure 3.9 should appear random with no patterns, as with the first plot. But this is again not the case, therefore the errors are correlated. Finally, the last plot of Figure 3.9 shows which points have the greatest influence on the regression (leverage points) which are observations 23032, 28008 and 26236.

### 3.3.5 Analysis of collinearity

In multiple linear regression it can happen that the predictor variables are correlated (see [Fahrmeir et al., 2008, Chapter 3]). The higher the linear correlation between the predictor variables, the higher the variance. In this case the estimations can be extremely inexact.

To remove strong collinearity, the relevant covariables can be omitted, from them a jointly (easy interpreted) variable can be built, a ridge-regression can be done or a main component regression can be used. More information about these methods can be found in [Fahrmeir et al., 2008, Chapter 3].

### 3.3.6 Box-Cox transformation

In Section 3.3.1 it has already been mentioned that predictor variables can be transformed for example by adding a polynomial term. Also the response variable can be transformed. A popular method to determine a transformation on the response variable is the Box-Cox transformation (see [Faraway, 2009, Chapter 7]). The goal of this method is to find a parameter $\lambda$ for a variance stabilizing transformation, i.e. to make sure that the variance of the transformed response variable $y^{*}(\lambda)$ is independent of its mean. The transformation is given by

$$
y^{*}(\lambda)= \begin{cases}\frac{y^{\lambda}}{\lambda} & \lambda \neq 0 \\ \log (y) & \lambda=0\end{cases}
$$

An estimator of the parameter $\lambda$ can be obtained by the profile log-likelihood function.

In R the command boxcox of the package MASS([Venables and Ripley, 2002] $)$ calculates the estimator for $\lambda$ and draws the profile of the likelihood function including a $95 \%$-confidence interval for $\lambda$.

Example 3.20. For the above example the Box-Cox plot can be shown in the following way:

```
boxcox(regression_model)
```



Figure 3.10: Box-Cox plot of the example linear regression model

One can see in Figure 3.10 that a transformation with $\lambda \approx 0.4$ is necessary.

### 3.3.7 Confidence intervals and prediction intervals

In the regression for a new given observation, the value of the response variables can be predicted. For this value, also confidence intervals and prediction intervals can be calculated (see [Faraway, 2009, Chapter 3]).

The confidence interval covers the expected value of the dependent variable $E\left(y_{+}\right)$of a new observation $x_{+}$with a probability of $(1-\alpha)$ and is defined as

$$
\hat{y}_{+} \pm t_{n-p, 1-\frac{\alpha}{2}} \sqrt{\hat{\sigma}^{2} x_{+}^{T}\left(X^{T} X\right)^{-1} x_{+}}
$$

The prediction interval covers the actual new observation $y_{+}$of a new observation $x_{+}$with a probability of $(1-\alpha)$ and is defined as

$$
\hat{y}_{+} \pm t_{n-p, 1-\frac{\alpha}{2}} \sqrt{\hat{\sigma}^{2}\left(1+x_{+}^{T}\left(X^{T} X\right)^{-1} x_{+}\right)}
$$

Note, that by definition the prediction interval is always bigger than the confidence interval.

In R both intervals can be calculated with the command predict. For a confidence interval the additional option interval="confidence" has to be chosen and for a prediction interval the option interval="prediction" has to be added. In both cases the level can also be specified.
Example 3.21. For our example the intervals can be calculated for an observation with a height of 170 cm , a weight of 60 kg and an age of 50 years in the following way:

```
test <- data.frame(height=170,weight=60, age=50)
predict(regression_model, test, se.fit=TRUE, interval="confidence",
        level=0.90)$fit
## fit lwr upr
## 1 166.4537 162.4279 170.4795
predict(regression_model, test, se.fit=TRUE, interval="prediction",
        level=0.90)$fit
## fit lwr upr
```

The new observation has $y_{+}$166.45 W . The confidence interval for this observation is $[162.43 ; 170.48]$, which means that the expected value of the new observation $E\left(y_{+}\right)$is to $90 \%$ in this interval. The prediction interval is [98.36;234.55], which means that the actual new observation $y_{+}$is to $90 \%$ in this interval.

### 3.4 Variable selection

### 3.4.1 Steps in selecting the best regression equation

For selecting the best regression model, the following steps have to be followed (see e.g. [Kleinbaum et al., 1998, Chapter 16]):

1. Specification of the maximum model
2. Specification of a criterion for selecting a model
3. Specification of a strategy for selecting variables
4. Conduction of the specified analysis
5. Evaluating the reliability of the chosen model

### 3.4.2 Specification of the maximum model

The maximum model should contain the following elements (see for more information [Kleinbaum et al., 1998, Chapter 16]):

1. All conceivable basic predictor variables
2. High-order powers of basic predictor variables
3. Other transformations of predictor variables
4. Interactions among predictor variables, including two-way and higherorder interactions
5. All possible 'control' variables, as well as their powers and interactions

Note that overfitting a model, i.e. including variables in the model with truly zero regression coefficients in the population, will not introduce bias on the result if usual regression assumptions are met, but it must be ensured that overfitting does not introduce harmful collinearity (see Subsection 3.3.5). Also underfitting the model, i.e. by leaving important predictor variables out, will introduce bias in the estimated regression coefficients.

### 3.4.3 Selection criteria

In general, larger models will fit better and have smaller error sum of squares SSE, but use more parameters. Thus for the choice of the model these two factors have to be balanced. Therefore, for evaluating potential subsets of predictor variables, selection criteria can be used. A selection criteria is an index, which can be calculated for each candidate model to compare the models. Thus, for a given selection criteria, the different models can be ordered from the best to the worst (see [Kleinbaum et al., 1998, Chapter 16]).

However, more than one selection criteria should be considered, because no single criterion works best. In practice, using a different selection criteria may lead to a different model choice (see [Kleinbaum et al., 1998, Chapter 16]).

The discussion of the following four criteria for evaluating subsets of predictor variables are taken from [Sheather, 2009, Chapter 7].

## $R^{2}$ and adjusted $R^{2}$

The coefficient of determination, as already mentioned in Subsection 3.3.3, is defined as

$$
R^{2}=1-\frac{S S E}{S S T}=\frac{S S R}{S S T}
$$

Because adding a new variable to a model can only decrease the coefficient of determination $R^{2}$, always the biggest model would be chosen and the adjusted coefficient of determination is a better choice. The adjusted coefficient of determination, as already mentioned in Subsection 3.3.3, is defined by

$$
R_{a d j}^{2}=1-\frac{M S E}{M S T}=1-\frac{n-1}{n-p} \frac{S S E}{S S T}
$$

where $p$ is the number of predictor variables in the current model.
Using the adjusted $R^{2}$ as the selection criterion, the model with the highest $R_{a d j}^{2}$ should be selected.

## Akaike's Information Criterion AIC

The AIC evaluates the

$$
A I C=n \log \left(\frac{S S E}{n}+2 p\right)
$$

The smaller the value of the AIC, the better the model.

## Corrected Akaike's Information Criterion AIC $_{C}$

$$
A I C_{C}=A I C+\frac{2(p+2)(p+3)}{n-p-1}
$$

The $A I C_{C}$ is especially suitable for a small sample size compared to the number of predictor variables, i.e. $\frac{n}{p+1} \leq 40$.

## Bayesian Information Criterion BIC

$$
B I C=-2 \log L\left(\hat{\beta}, \hat{\sigma}^{2}, y\right)+(p+1) \log (n)
$$

The smaller the value of the BIC, the better the model.

Mallow's $C_{p}$
Mallow's $C_{p}$ (see Kleinbaum et al., 1998, Chapter 16]) is defined as

$$
C_{p}=\frac{S S E}{M S E}-(n-2(p+1)) .
$$

A small value of $C_{p}$ means that the model is relatively precise.
Mallows's $C_{p}$ has been shown to be equivalent to the AIC in the special case of Gaussian linear regression (see [Boisbunon et al., 2014]).

Using the BIC results in simpler models, which are more robust. Therefore in Chapter 6 the BIC will be the chosen criterion.

### 3.4.4 Specification of a strategy for selecting variables

The third step in choosing the best model is to specify the strategy for selecting variables. [Sheather, 2009, Chapter 7] classifies these methods into two different approaches to choose the potential subsets of predictor variables, namely

1. all possible subsets, and
2. stepwise methods.

The stepwise methods include the forward and backward selection.

## All subset selection

The all subset selection is to be preferred over all other variable selection strategies, if it is possible (see [Kleinbaum et al., 1998, Chapter 16]). This is the only method, where it is guaranteed that the model with the best value of the selected selection criterion is found.

In $R$ all subsets can be calculated with the function regsubsets, which is in the package leaps. Useful options are nbest and nvmax. With nbest=n it can be specified, that $n$ models of each size are kept in the result object. Without this option $n=1$ is assumed. With nvmax=n the maximal size model, i.e. the number of variables to include are defined. Without this option $n=8$ is assumed.

Example 3.22. The following example shows the summary of the two best regression subsets for one to five variables of the above model:

```
model_regsubsets<-regsubsets(workload_max ~ age+weight+height+
    I(age^2)+weight:height,
    data=exampledata,nbest=1,nvmax=5)
summary(model_regsubsets)$outmat
\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \#\# & & age & weig & hei & I (ag & & \\
\hline \#\# 1 & ( 1 ) & " " & " " & "*" & " & " & " \\
\hline \#\# 2 & ( 1 ) & " " & & "*" & "*" & " & " \\
\hline \#\# 3 & ( 1 ) & "*" & " " & "*" & "*" & " & " \\
\hline \#\# 4 & ( 1 ) & " " & "*" & "*" & "*" & & \\
\hline \#\# 5 & ( 1 ) & "*" & "*" & "*" & "*" & "* & " \\
\hline
\end{tabular}
```

To evaluate which model is the best, the selection criteria BIC (standard criterion), $R^{2}, R_{a d j}^{2}$ and $C_{p}$ from Subsection 3.4 .3 can be used. The first line, which has no option scale automatically uses BIC:

```
plot(model_regsubsets)
plot(model_regsubsets, scale="r2")
plot(model_regsubsets, scale="adjr2")
plot(model_regsubsets, scale="Cp")
```

Figure 3.11 shows the results for the different selection criteria.


Figure 3.11: Results for different selection criteria for the example linear regression

```
plot(model_regsubsets$rss, xlab="Number of Variables", ylab="SSE",
    type="l")
plot(summary(model_regsubsets)$adjr2, xlab="Number of Variables",
    ylab=expression(R[adj]~2), type="l")
points(which.max(summary(model_regsubsets)$adjr2),
        summary(model_regsubsets)$adjr2[which.max(
            summary(model_regsubsets)$adjr2)]
        , col="red", cex =2, pch =20)
plot(summary(model_regsubsets)$cp, xlab="Number of Variables",
    ylab="CP", type="l")
points(which.min(summary(model_regsubsets)$cp),
        summary(model_regsubsets)$cp[which.min(
            summary(model_regsubsets)$cp)]
        , col="red", cex =2, pch =20)
plot(summary(model_regsubsets)$bic, xlab="Number of Variables",
    ylab="BIC", type="l")
points(which.min(summary(model_regsubsets)$bic),
```

```
summary(model_regsubsets)$bic[which.min(
    summary(model_regsubsets)$bic)],
col="red", cex =2, pch =20)
```



Figure 3.12: Information criteria for the example linear regression
The first plot in Figure 3.12 shows the SSE for the best models with one to five variables. The other plots show the values of the different selection criteria. As a result the model with five parameters is the best for all selection criteria.

Note, that also the function leaps exists in $R$, which is similar to the function regsubsets.

However, if the number of variables in the maximum model exceeds a certain size, it becomes impractical and instead it is preferable to use a stepwise method. The most popular stepwise methods are the forward selection and the backward selection.

## Forward selection

The forward selection starts with a model, which just includes the intercept. In each iteration one predictor variable, taken from the set of the variables of
the maximum model, is included. The predictor variable is chosen such that the resulting model improves the selection criterion as much as possible. The algorithm ends, if all predictor variables are in the model or if no further improvement is possible.

## Backward selection

The backward selection is the opposite of the forward selection, i.e. it starts with the maximum model with all predictor variables. In each step the predictor variable, which improves the selection criterion as much as possible, gets excluded. The algorithm ends, if all predictor variables got excluded or no further improvement is possible.

## Stepwise selection

The stepwise selection combines the forward and the backward selection. In each iteration it will be decided, if a further variable comes into a model or if a variable gets excluded.

In $R$ the variable selection can be done with the function step. The used selection criterion in this function is the AIC.

Example 3.23. The following is an example for the forward selection. For each step first the actual AIC and regression coefficients are given. For the coefficients, which can be included, the resulting sum of squares, the residual sum of squares RSS and the AIC are given:

```
null<-lm(workload_max ~ 1,data=exampledata)
full<-lm(workload_max ~ age+weight+height+I(age^2)+weight:height,
    data=exampledata)
modell_regression_step_fs<-step(null, scope=list(lower=null,
                                upper=full),
    direction="forward")
## Start: AIC=9331.52
## workload_max ~ 1
##
## Df Sum of Sq RSS AIC
## + height 1 982714 2164836 8890.8
## + weight 1 314399 2833151 9209.0
## + I(age~2) 1 257059 2890491 9232.7
## + age 1 249572 2897978 9235.8
## <none> }31475509331.
##
## Step: AIC=8890.75
## workload_max ~ height
##
## Df Sum of Sq RSS AIC
## + I(age^2) 1 127448 2037388 8821.0
## + age 1 120669 2044167 8824.9
```

```
## <none> 2164836 8890.8
## + weight 1 424 2164413 8892.5
##
## Step: AIC=8820.97
## workload_max ~ height + I(age^2)
##
## Df Sum of Sq RSS AIC
## + age 1 8657.5 2028730 8817.9
## <none> 2037388 8821.0
## + weight 1 64.1 2037324 8822.9
##
## Step: AIC=8817.93
## workload_max ~ height + I(age^2) + age
##
## Df Sum of Sq RSS AIC
## <none> 2028730 8817.9
## + weight 1 1.4482 2028729 8819.9
```

Afterwards a summary of the best model can be given by:

```
summary(modell_regression_step_fs)
##
## Call:
## lm(formula = workload_max ~ height + I(age^2) + age,
## data = exampledata)
##
## Residuals:
## Min 1Q Median 3Q Max
## -139.584 -25.128 -0.323 23.625 188.828
##
## Coefficients:
## Estimate Std. Error t value Pr (>|t|)
## (Intercept) -420.55335 50.28850 -8.363 <2e-16 ***
## height 3.10155 0.13891 22.327 <2e-16 ***
## I (age~2) -0.05838 0.01949 -2.995 0.0028 **
## age 4.13965 1.84554 2.243 0.0251 *
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 41.48 on 1179 degrees of freedom
## Multiple R-squared: 0.3555,Adjusted R-squared: 0.3538
## F-statistic: 216.7 on 3 and 1179 DF, p-value: < 2.2e-16
```

```
modell_regression_step_bs<-step(full, direction="backward")
```

And finally the combination of both forward and backward selection can be done in the following way:

```
modell_regression_step_fbs<-step(null, scope = list(upper=full),
    data=exampledata, direction="both")
```

All directions give the same result.

### 3.5 Dummy regression

In Section 3.3 only continuous predictor variables were considered. To extend the predictor variables to categorical variables, dummy variables can be used. The dummy variable in a regression equation takes on a finite number of values, so that different categories of a nominal variable can be defined (see [Gareth et al., 2014, Chapter 3] and [Kleinbaum et al., 1998, Chapter 14]).

The term dummy is due to the fact that the values taken on by such variables do not indicate meaningful measurements but rather the categories of interest (see [Kleinbaum et al., 1998, Chapter 14]).
[Kleinbaum et al., 1998, Chapter 14] defines a rule for defining dummy variables for regression analysis to avoid collinearity: "If the nominal independent variable of interest has $k$ categories, then exactly $k-1$ dummy variables must be defined to index these categories, provided that the regression model contains a constant term (i.e. an intercept $\beta_{0}$ ). If the regression model does not contain an intercept, then $k$ dummy variables are needed to index the $k$ categories of interest."
[Fahrmeir et al., 2008, Chapter 3] gives an explicit definition to model the categorical variable with c levels $x \in\{1, \ldots, c\}$ as $c-1$ dummy variables:

$$
x=\left\{\begin{array}{l}
1 \\
2 \\
\vdots \\
c
\end{array} \quad \Rightarrow x_{1}=\left\{\begin{array}{ll}
1 & x=1 \\
0 & \text { else }
\end{array} \ldots x_{c-1}= \begin{cases}1 & x=c-1 \\
0 & \text { else }\end{cases}\right.\right.
$$

The resulting dummy variables can be used in R in the same way as continuous variables.

### 3.6 Regression surfaces

Regression surfaces are used to examine the relationship between a response variable and the exploratory variables. The visualization of a regression surface can be done with the package visreg [Breheny and Burchett, 2017].

In this thesis, two functions from this package are used. The first is visreg with which the regression model can be visualized. The default plots contain
a confidence band, prediction line, and partial residuals. Also, options for factors, transformations, conditioning and interactions are supported. The second function is visreg2d and with this function it can be shown how two variables interact to affect the response in a regression model.

Example 3.24. This example shows regression surfaces for the above regression with the formula

$$
W L=\text { age }+ \text { weight }+ \text { height }+I\left(\text { age }^{2}\right)+\text { weight }: \text { height } .
$$

The function visreg can be used in the following way:

```
visreg(lm(workload_max ~ age+weight+height+I(age^2)+weight:height,
            data=exampledata),
    ' age', band=TRUE,gg=TRUE, overlay=TRUE, partial=FALSE, alpha=0.05,
    breaks=c(25,50,75),ylab='WL',print.cond=FALSE)+ylim(50, 220)
visreg(lm(workload_max ~ age+weight+height+I(age^2)+weight:height,
            data=exampledata),
            'weight', by='height',plot.type="persp", band=TRUE,gg=TRUE,
            overlay=TRUE,
            partial=FALSE,alpha=0.05,breaks=c(150,170,190),ylab='WL')+
    ylim(50,250)
```


(a) Regression line for the maximum workload denpendent on age

(b) Regression lines for the maximum workload depending on weight for three different breaks of height

Figure 3.13: Plots of the regression line and confidence bands of the regression surface

Figure 3.14 shows these plots. Figure 3.14(a) shows the maximum workload depending on the age. To plot this, the other parameters have to be fixed. $I\left(a_{g e}{ }^{2}\right)$ is calculated by the age. The other parameters are set to the median values., i.e. weight is set to 78 and height is set to 173 . The function visreg can also be used to see how the effect of weight differs depending on the height with the
option by. Figure 3.14 (b) shows this. Here the height is fixed at three different stages. The slope of the regression lines of the surface is different for each of these heights. In both plots additionally the $95 \%$-confidence bands are plotted.

The function visreg2d can be used in the following way:

```
visreg2d(lm(workload_max ~ age+weight+height+I(age^2)+weight:height,
    data=exampledata),
    'weight','height',plot.type='gg',zlab='WL')
visreg2d(lm(workload_max ~ age+weight+height+I(age~2)+weight:height,
            data=exampledata),
        'weight','height',plot.type='persp',zlab='WL')
```


(a) Contour plot

(b) Perspective plot

Figure 3.14: Plots of the regression surface of the maximum workload depending on weight and height

The resulting plots are in Figure 3.14 . The first plot, Figure 3.14(a), shows a contour plot (option plot.type=' gg') and Figure 3.14 (b) shows a perspective plot (option plot.type='persp'). In both plots the interaction between height and weight can be observed.

### 3.7 Decision trees

Decision trees are a way to visualize regression models (e.g. [Falk et al., 2014, Chapter 9] or [Bankhofer and Vogel, 2008, Chapter 18]). There exist two variants of decision trees: classification trees and regression trees. The classification trees are used for nominal dependent variables and decision trees for quantitative dependent variables.

Decision trees are used for an automatic classification of data objects in order to solve decision problems. A decision tree consists of a root vertex, inner vertexes and leaves. Every vertex except the leaves represent one logical decision. The leaves represent an answer of the decision tree. This answer could be in the
form of the mean or box plots. Therefore, in the tree, the target variable for each observation can be predicted by following the path from the root node to the corresponding leaf.

To create a decision tree in $R$, the command tree from the package tree can be used.

Example 3.25. This example shows a regression tree for the maximum workload. As stated before, the maximum workload depends on age, height and weight. The right branch refers in this tree to yes and the left one to no.

```
plot(tree(workload_max ~ age+height+weight,data=exampledata))
```

text(tree(workload_max ~ age+height+weight,data=exampledata))


Figure 3.15: Regression tree for the example linear regression

We can see that the regression tree only contains the variables height and age. This corresponds to the result that the correlation between the maximum workload and the height and age is higher than with the weight.

If a new observation is 40 years old and has a height of 170 cm , then expected maximum workload is 165.1 W .

For the following variant of a regression tree the packages rpart and party are needed.

Example 3.26. This example shows another variant to get a regression tree. First the tree can be created with the command rpart.

```
tree<-rpart(workload_max ~ age+height+weight,data=exampledata)
tree
## n= 1183
##
## node), split, n, deviance, yval
## * denotes terminal node
##
## 1) root 1183 3147550.00 179.3922
## 2) height< 168.5 281 325207.10 131.8826 *
## 3) height>=168.5 902 1990486.00 194.1929
## 6) height< 179.5 497 886373.40 181.0966
## 12) age>=52.5 221 380658.10 168.7783 *
## 13) age< 52.5 276 445328.60 190.9601
## 26) weight< 69.5 46 66799.91 163.0435 *
## 27) weight>=69.5 230 335509.10 196.5435 *
## 7) height>=179.5 405 914264.70 210.2642
## 14) age>=50.5 235 437771.70 201.4340 *
## 15) age< 50.5 170 432840.40 222.4706 *
```

The cptable gives information about the complexity parameter (CP), which is used to control the size of the regression tree.

```
tree$cptable
## CP nsplit rel error xerror xstd
## 1 0.26428697 0 1.0000000 1.0012694 0.04480537
## 2 0.06031623 1 0.7357130 0.7469441 0.03803352
## 3 0.01918529 2 0.6753968 0.6917521 0.03440656
## 4 0.01386877 3 0.6562115 0.6846830 0.03403352
## 5 0.01366764 4 0.6423427 0.6799076 0.03439675
## 6 0.01000000 5 0.6286751 0.6708352 0.03421516
```

To adjust the size of the tree the command prune can be used.

```
tree_size<-prune(tree, cp = tree$cptable[3,"CP"])
tree_size
## n= 1183
##
## node), split, n, deviance, yval
## * denotes terminal node
##
## 1) root 1183 3147550.0 179.3922
## 2) height< 168.5 281 325207.1 131.8826 *
## 3) height>=168.5 902 1990486.0 194.1929
## 6) height< 179.5 497 886373.4 181.0966 *
## 7) height>=179.5 405 914264.7 210.2642 *
```

Finally the regression tree can be plotted with the command plot.

```
plot(as.party(tree_size))
```



Figure 3.16: Regression tree for the example linear regression with the package party

## Chapter 4

## Data preparation

In this chapter, steps involving the preparation of raw data (received from ZARG) for statistical evaluation are explained in detail. The chapter starts with a description of the received raw data. Afterwards each step involved in the data preparation is described.

The data preparation required 5 steps:
Step 1: Transformation of the XML files in a CSV file
Step 2: Integration of the CSV files in a MySQL database
Step 3: Integration of the files with information on blood parameters, medication and diagnosis in the main table with a Java program

Step 4: Reading the MySQL database into $R$
Step 5: Adaptation of the table in R
Figure 4.1 shows these steps.

### 4.1 Received data

The received data consists of separate files with information on ergometries, blood parameters, diagnoses and medication prescribed.

### 4.1.1 XML files for data of the ergometries

The data from the ergometries have been provided in XML files. For each ergometry, there was one XML file. These XML files consist of variables such as age, gender, height, weight, maximum workload. In addition, files had information about the time series of the ergometry, start time of the step, the workload, systolic blood pressure, diastolic blood pressure, heart rate and cadence.

### 4.1.2 CSV files for the blood parameters, diagnosis and medication

The information on blood parameters, medication and diagnoses of the participants has been provided in CSV files.


Figure 4.1: Workflow for the data preparation

## CSV file: Blood parameters

This CSV file contains information about total cholesterol (TC), low-density lipoprotein (LDL), high-density lipoprotein (HDL), triglyceride (TG), creatinine (Cr), fasting blood sugar level (FBS) and uric acid (UA) levels in blood. The information on the variables present in this file are shown in Table 4.1. The first column contains the value of that parameter if it was measured within the range of two weeks before or after the relevant ergometry, and the second column states whether this measured value is pathological (T) or not (F).

| Variables | Units | Description |
| :--- | :--- | :--- |
| patient_id | - | Patient ID |
| entry_id | - | identification number for the entry <br> date when the laboratory was taken |
| lab_date | date | parameter of the lab |
| parameter <br> lab_value <br> evaluation | - | $m g / d l$ |
| corresponding value of the parameter |  |  |
| T for pathological and F for not pathological |  |  |

Table 4.1: Description of the variables in CSV file blood parameters

## CSV file: Diagnosis

The information about the diagnosis of participants who performed at least one ergometry is present in this CSV file. The information on the variables present
in this file are shown in Table 4.2,

| Variables | Units | Description |
| :--- | :--- | :--- |
| patient_id | - | Patient ID |
| entry_id | - | identification number for the entry |
| date | date | date of the diagnosis <br> type of the diagnosis |
| diagnosis | - | type |

Table 4.2: Description of the variables in Table diagnosis

## CSV file: Medication

This file contains information about the types and doses of medication prescribed to participants. The information on the variables present in this file are shown in Table 4.3.

| Variables | Units | Description |
| :--- | :--- | :--- |
| patient_id | - | Patient ID |
| entry_id | - | identification number for the entry |
| date | date | date on which the medication was prescribed |
| medication | - | type of the drug <br> doses of the medication |
| doses | - | identification number of the medicine |
| medication_id | - |  |

Table 4.3: Description of the variables in Table medication

### 4.2 Step 1: Transformation of the XML files in a CSV file

As first step, the data from the XML files have been transformed into a CSV file using XSL stylesheet. The stylesheet is attached in Appendix A. The variables of the resulting CSV file are described in Table 4.4. This table contains the general information about the participants and some parameters of the corresponding ergometry. The general information includes patient ID, age, gender, height, weight and abdominal measurement. The ergometry information includes start time, end time, device, pace maker, resting heart rate, maximal heart rate, maximal power, resting systolic blood pressure, resting diastolic blood pressure, maximal systolic blood pressure, maximal diastolic blood pressure and the reason for termination.

In total, there were 29,805 records each containing information about one ergometry. After quality control, some of the records were deleted due to lack of correct information. Finally, 28, 625 records were used for downstream analysis which passed the quality control step. These records were collected between 2004-01-27 and 2017-06-13 (14 years).

| Variables | Units | Description |
| :---: | :---: | :---: |
| patient_id | - | Patient ID |
| start_time | date and time | date and time of the ergometry's start |
| end_time | date and time | date and time of the ergometry's end |
| age | years | patient's age |
| gender | - | patient's gender |
| height | cm | patient's height |
| weight | kg | patient's weight |
| waist | cm | patient's waist circumference |
| pacemaker | - | binary variable for existence of pacemaker |
| device | - | type of device, ergometer / treadmill |
| WL | W | maximum workload the patient could achieve |
| $\mathrm{SBP}_{r}$ | mmHg | resting systolic blood pressure |
| $\mathrm{DBP}_{r}$ | mmHg | resting diastolic blood pressure |
| $\mathrm{SBP}_{\text {max }}$ | mmHg | systolic blood pressure at maximum workload |
| $\mathrm{DBP}_{\text {max }}$ | mmHg | diastolic blood pressure at maximum workload |
| $\mathrm{HR}_{r}$ | bpm | resting heart rate |
| $\mathrm{HR}_{\text {max }}$ | bpm | maximal heart rate during the ergometry |
| termination | - | reason for termination of the ergometry |
| purpose |  | purpose for the ergometry |

Table 4.4: Description of the variables in Table maindata

### 4.3 Step 2: Integration of the CSV files in MySQL database

Four CSV files maindata, blood parameters, diagnosis and medication are integrated in a MySQL database. The MySQL program for this is attached in Appendix B.

### 4.4 Step 3: Integration of the blood parameters, diagnosis and medication in the table maindata with Java programs

For the sake of convenience in table maindata additional columns for blood parameters, diagnosis and medication were generated with the help of Java programs. These programs are attached in Appendix Cto Appendix E.

### 4.4.1 Columns for the blood parameters

For each ergometry, the information on each blood parameter is inserted in two new columns. These columns refer to the value of the corresponding blood parameter and its evaluation as mentioned in Table 4.1.

### 4.4.2 Column for diagnosis

The column for diagnosis contains information in the form of binary numbers. The participant with a diagnosis of cardiovascular diseases is assigned 1, otherwise 0 .

### 4.4.3 Columns for medication

The information on beta blockers and statins is inserted in two separate columns. Here, also the binary numbers are used to indicate if the participant is taking medication or not. The participant taking beta blockers, from the list mentioned in Section 2.5, is assigned 1, otherwise 0 . The convention is the same for statins too.

### 4.5 Step 4: Reading the table maindata into $R$

The finished table maindata is exported into $R$. The corresponding $R$ script is attached in Appendix F.

### 4.6 Step 5: Adaptation of the table maindata in $R$

In the last step, additional variables calculated from existing variables are added. For this calculation, the following formulas are used:

Formula for the body mass index:

$$
B M I\left[\mathrm{~kg} / \mathrm{m}^{2}\right]=\frac{\text { weight }[\mathrm{kg}]}{\left(\frac{\text { height }[\mathrm{cm}]}{100}\right)^{2}}
$$

Formula for the waist-to-height-ratio:

$$
W H R=\frac{\text { waist }[\mathrm{cm}]}{\text { height }[\mathrm{cm}]}
$$

Formula for the workload-to-weight-ratio:

$$
\begin{aligned}
W W R[W / k g] & =\frac{W L[W]}{\text { weight }[k g]} \\
T C: H D L & =\frac{T C}{H D L} \\
L D L: H D L & =\frac{L D L}{H D L} \\
T G: H D L & =\frac{T G}{H D L}
\end{aligned}
$$

The body surface area is calculated from weight and height using the Du Bois formula (see Chapter 2) and the maximum workload using the model from
[Wonisch et al., 2008]. Furthermore, the column showing the year in which erogometry was performed has been added.

Finally, two tables with information which correspond to stage II and stage III of cardiac out-patient rehabilitation are created. In these tables, above mentioned information available from these two stages for a single participant is presented in one row.

The R script for this is added in Appendix $F$.

### 4.7 Variables used in the statistical analysis

Table 4.5 shows a summary of all variables which will be used in the next chapters.

|  | Variables | Units | Description |  |  |  |  |
| :--- | :--- | :---: | :--- | :---: | :---: | :---: | :---: |
|  |  |  |  |  | gender | - | patient's gender $^{1}$ |
| medication | - | medication history $^{2}$ |  |  |  |  |  |
| diagnosis $^{3}$ |  |  |  |  |  |  |  |

Table 4.5: Description of the variables used in the statistical analysis
${ }^{1}$ M... male, F... female
${ }^{2} 1 \ldots$ statin, $2 \ldots$ beta blocker, $3 \ldots$ both, $0 \ldots$ none
${ }^{3} 1 \ldots$ cardiac diagnosis, $0 \ldots$ non-cardiac or no diagnosis

## Chapter 5

## Exploratory data analysis

In this chapter, an exploratory data analysis (EDA) is used to analyze the data for patterns and relationships. A mathematical description of EDA and its methods are given in Section 3.2. In Section 5.1, a univariate analysis is done, where each variable is analyzed separately by a calculation of statistical indicators and presented as an illustration. In Section 5.2, a multivariate analysis, correlation matrices are used to provide an insight into the linear relationship between paired variables, also scatter plots are used to identify patterns between multiple variables. In Section 5.3, a gender specific comparison between the maximum workload obtained in ergometries from the first ( $2004 \& 2005$ ) and last two years (2016 \& 2017) of study is done for the quality control of the data. Finally a short conclusion of this chapter is given in Section 5.4 .

### 5.1 Univariate analysis

The EDA for each variable is performed to summarize their main characteristics and to find structures. The aim of this analysis is to verify the data and to find and eliminate errors in it.

### 5.1.1 Composition of the data regarding gender, medication and diagnosis

Figure 5.1 shows the categorization of the ergometries by three nominal variables namely gender, medication and diagnosis. Figure 5.1(a) shows that 18,919 ergometries are done by males and 9,706 by females. Males performed twice as many ergometries as females. For the categorization using medications only two medication groups are taken into account as mentioned in Chapter 4. Figure 5.1(b) shows the number of ergometries in patients with no medication, with either one of statin or beta blocker and with both. In total, 4,031 ergometries are done by patients taking statin and 4,904 taking beta blocker. In most of the cases, the participants were not taking statins or beta blocker. Figure 5.1(c) shows the categorization of ergometries in two groups. The first group of 17,544 ergometries is a group with the diagnosis of non-cardiac diseases or no diagnosis and the second group with 11,081 ergometries is with the diagnosis of cardiac diseases. So the majority of data for the ergometries is from the participants without
any cardiac disease diagnosis.

(a) Number of ergometries performed by females and males

(b) Number of ergometries divided by medication status

(c) Number of ergometries divided by diagnosis status

Figure 5.1: Number of ergometries separated by gender, medication and diagnosis

### 5.1.2 Statistical indicators of the variables

Detailed assessment of statistical indicators is given in Table 5.1 along with the missing values in the data. It shows that just 8 variables have no missing values. Unfortunately the waist circumference is measured during just 3,800 ergometries. Each variable is discussed thoroughly in the upcoming subsections.

| variable | min | $q_{0.25}$ | $q_{0.5}$ | $\bar{x}$ | $q_{0.75}$ | $\max$ | $s$ | NA's $^{\prime}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| age | 10 | 49 | 60 | 57.92 | 69 | 94 | 14.84 | 0 |
| height | 139 | 167 | 173 | 172.60 | 179 | 208 | 8.98 | 0 |
| weight | 32 | 69 | 78 | 78.99 | 88 | 160 | 14.82 | 0 |
| waist | 62 | 92 | 99 | 99.55 | 107 | 158 | 12.04 | 24825 |
| BMI | 15.22 | 23.74 | 26.03 | 26.44 | 28.73 | 55.28 | 4.06 | 0 |
| WHR | 0.37 | 0.53 | 0.57 | 0.57 | 0.61 | 0.89 | 0.07 | 24825 |
| BSA | 1.15 | 1.77 | 1.91 | 1.91 | 2.05 | 2.76 | 0.020 | 0 |
| DBP_r | 36 | 71 | 79 | 79.06 | 87 | 223 | 19.30 | 1339 |
| DBP_max | 36 | 76 | 86 | 86.67 | 96 | 257 | 30.88 | 315 |
| SBP_r | 6 | 106 | 118 | 119.40 | 130 | 291 | 13.23 | 1390 |
| SBP_max | 73 | 164 | 184 | 185.10 | 204 | 347 | 18.54 | 31 |
| HR_r | 35 | 67 | 76 | 77.61 | 86 | 179 | 14.88 | 98 |
| HR_max | 55 | 127 | 148 | 146.20 | 166 | 324 | 26.44 | 0 |
| TC | 78 | 158 | 188 | 193.19 | 223 | 434 | 47.82 | 9767 |
| LDL | 8.6 | 82.2 | 105.8 | 112.21 | 137.4 | 345.0 | 40.63 | 9839 |
| HDL | 16 | 43 | 51 | 52.83 | 61 | 157 | 14.09 | 9872 |
| TG | 27 | 86 | 118 | 140.75 | 167 | 1204 | 88.31 | 9767 |
| Cr | 0.58 | 0.97 | 1.09 | 1.12 | 1.23 | 3.29 | 0.024 | 14219 |
| FBS | 42 | 96 | 104 | 110.36 | 115 | 378 | 25.50 | 13443 |
| UA | 1.50 | 5.09 | 5.92 | 5.98 | 6.81 | 12.86 | 1.38 | 14152 |
| TC:HDL | 1.51 | 3.04 | 3.61 | 3.80 | 4.38 | 10.62 | 1.02 | 9872 |
| LDL:HDL | 0.29 | 1.62 | 2.04 | 2.19 | 2.63 | 6.18 | 0.80 | 9912 |
| TG:HDL | 0.30 | 1.53 | 2.35 | 3.02 | 3.63 | 45.19 | 0.56 | 9872 |
| WL | 21 | 113 | 150 | 158 | 200 | 440 | 58.53 | 0 |
| WWR | 0.24 | 1.50 | 1.96 | 2.02 | 2.46 | 6.10 | 0.73 | 0 |

Table 5.1: Descriptive statistics of all variables with the following indicators: minimum, 1-quartile, median, average, 3-quartile, maximum, standard deviation and the number of missing values

### 5.1.3 Analysis of the variables age, height, weight and waist circumference

The following analysis shows box plots, histograms and density plots for the variables age, height, weight and waist circumference categorized by gender. These variables age, height and weight are measured for each ergometry. In contrast to that, the waist circumference is just available for 3,800 ergometries as it is measured only during out-patient rehabilitation.

Figure 5.2 shows a box plot, a histogram and a density plot for age. All of them are categorized by gender. The mean age of females is 59.13 with a standard deviation of 14.00, whereas for males mean age is 57.30 and the standard deviation of 15.22 . Both plots show that the distribution of age is similar for both genders, although the median as well as the mean in females is slightly higher and the standard deviation is slightly smaller. The range for females and males is similar, the minimum is 10 and 11 and the maximum is 93 and 94 , respectively.


Figure 5.2: Exploratory data analysis for the variable age

The mean height in females ( 164 cm ) is 13 cm less than in males $(177 \mathrm{~cm})$. The standard deviation is similar in females and males. It is 6.16 and 6.74. The height of females spans from 139 cm to 190 cm while for male it is from 143 cm to 208 cm as seen in Figure 5.3 .

(a) Box plot of the height divided by gender

(b) Histogram (binwidth=5) and density plot of the height with marked mean divided by gender

Figure 5.3: Exploratory data analysis for the variable height
As that of variable height, similar trends, i.e. similar standard deviation and different mean, are present in weight as seen in Figure reffig:weight. The mean weight for females is 68.94 kg , whereas for men it is 84.14 kg . The maximum weight for male in the cohort is 160 kg and female 140 kg .


Figure 5.4: Exploratory data analysis for the variable weight

Figure 5.5 shows the plots for the waist circumference. Although the mean for female is 7.58 cm lower compared to male, the standard deviation is higher. Equivalent to the mean, the median is higher for male, and the length of the $95 \%$-confidence interval around the median is much higher for both genders as compared to other variables due to availability of only 3,800 measurements.

(a) Box plot of the waist divided by gender

(b) Histogram (binwidth=5) and density plot of the waist with marked mean divided by gender

Figure 5.5: Exploratory data analysis for the variable waist

### 5.1.4 Analysis of the additionally calculated variables body mass index and waist-to-height-ratio

Both variables BMI and WHR are calculated from variables in the section above. The relevance of these variables for the heart attack risk is given in Chapter 2. Although the weight and the height of males and females are different, the BMI is similar for both genders as shown in Figure 5.6.


Figure 5.6: Exploratory data analysis for the variable BMI

(a) Box plot of the of the WHR divided by gender

(b) Histogram (binwidth=0.05) and density plot of the of the WHR with marked mean divided by gender

Figure 5.7: Exploratory data analysis for the variable WHR

Similar to the BMI, the analysis of variable WHR yields similar results for males and females. Although the mean of WHR is similar, the standard deviation is higher for females as seen in Figure 5.7 .

### 5.1.5 Analysis of the blood pressure

Figure 5.8 and Figure 5.9 show box plots of the resting blood pressure and blood pressure at maximum workload, respectively, separated by the gender. There is only a big difference in the systolic blood pressure at maximum workload among males and females but other values are similarly distributed in both genders.


Figure 5.8: Exploratory data analysis for the variable diastolic blood pressure


Figure 5.9: Exploratory data analysis for the variable systolic blood pressure

To analyze the correlation between the resting blood pressure and the increase in the blood pressure during an ergometry, the difference between blood pressure at the maximum workload and the resting blood pressure is calculated. Figure 5.10 shows the scatter plot of the resting blood pressure compared with the increase in blood pressure. It is interesting to note that the increase in the diastolic blood pressure is also negative. The reason for this could be the difficulty in measuring the diastolic blood pressure during the exercise, which results in lower diastolic blood pressure values than actual. For both systolic and diastolic blood pressure the increase can get higher if the resting blood pressure is low.


Figure 5.10: Increase of the blood pressure during ergometry

### 5.1.6 Analysis of the heart rate

Figure 5.11 shows gender specific box plots for the resting and the maximum heart rate. It shows that the heart rate is very similar between the genders, but the median of the resting heart rate is slightly higher for females while the median of the maximum heart rate is higher for males.

Figure 5.12 shows the relationship between resting heart rate and increase of the heart rate during an ergometry. The increase of the heart rate is a difference between the resting heart rate and the heart rate at the end of that ergometry. No negative values indicate that during all ergometries, heart rate was increased.


Figure 5.11: Exploratory data analysis for the variable heart rate


Figure 5.12: Scatter plot for the resting heart rate and the increase of the heart rate during an ergometry

### 5.1.7 Analysis of the blood parameters

For the ergometries 7 different blood parameters were measured. Figure 5.13 shows the box plots of the variables TC, LDL, HDL, TG. The median of the variables TC, LDL and HDL are higher for females. In contrary, the median for the variable TG is similar, but some outliers are far away from the median.

(a) Box plot of the total cholesterol separated by gender

(c) Box plot of the high-density lipoprotein separated by gender

(b) Box plot of the low-density lipoprotein separated by gender

(d) Box plot of the triglycerides separated by gender

Figure 5.13: Box plots for the variables TC, LDL, HDL, TG

The analysis of the variables $\mathrm{Cr}, \mathrm{FBS}$ and UA, Figure 5.14, shows higher medians for male than for female.

(a) Box plot of the creatinin separated by gender

(b) Box plot of the fasting blood sugar level separated by gender

(c) Box plot of the uric acid separated by gender

Figure 5.14: Box plots for $\mathrm{Cr}, \mathrm{FBS}$ and UA

### 5.1.8 Additionally calculated variables TC to HDL ratio, LDL to HDL ratio and TG to HDL ratio

For analyzing the effect of blood cholesterol level on cardiac health, the TC:HDL ratio, the LDL:HDL ratio and the TG:HDL ratio are calculated. These parameters are better indicators of cardiac health. Figure 5.15 shows that there is no remarkable difference between the genders.

(a) Box plot of TC-to-HDL-ratio separated by gender

(b) Box plot of LDL-to-HDL-ratio separated by gender

(c) Box plot of TG-to-HDL-ratio separated by gender

Figure 5.15: Box plots for the calculated variables TC:HDL, LDL:HDL and TG:HDL

### 5.1.9 Analysis of the maximum workload and maximum workload-to-weight-ratio

Finally the variables WL and WWR are analyzed. Figure 5.16 shows box plots categorized by gender, medication and diagnosis, respectively, and a histogram and density plot of the maximum workload. The mean of the variable maximum workload is much higher for men. If participants of the ergometry have an cardiac diagnosis or take statin or beta blocker, then the maximum workload is decreasing.

(a) Box plot of the maximum workload divided by gender

(c) Box plot of the maximum workload divided by diagnosis

(b) Box plot of the maximum workload divided by medication history

(d) Histogram and density plot for the maximum workload separated by gender

Figure 5.16: Exploratory data analysis for the variable maximum workload

Figure 5.17 shows box plots categorized by gender, medication and diagnosis, respectively, and a histogram of the maximum workload-to-weight-ratio. The difference between the maximum workload-to-weight-ratio between males and females is less than in the maximum workload.

(a) Box plot of the maximum workload-to-weight-ratio divided by gender

(c) Box plot of the maximum workload-to-weight-ratio divided by diagnosis

(b) Box plot of the maximum workload-to-weight-ratio divided by medication

(d) Histogram and density plot of the maximum workload-to-weight-ratio divided by gender

Figure 5.17: Exploratory data analysis for the variable maximum-workload-to-weight-ratio

### 5.2 Multivariate analysis

The multivariate analysis is used to investigate the correlation between more than one parameters.

### 5.2.1 Correlation

The correlation between the variables is explored in a correlation matrix, which explores the linear relationship. Figure 5.18 and Figure 5.19 show the correlation between the variables. One can see that the correlation to the WL is in average less than to the WWR. The WWR has a correlation of more than 0.5 with the age and the waist-to-height-ratio. Further, four variables, height, waist, BMI and FBS have a correlation of more than 0.25 to the WWR.

Due to the low correlation between the cardiac parameters and the blood parameters with the WWR, in the regression analyses of the next chapter these variables will not be taken into account.


Figure 5.18: Correlation between the variables of the basic information and the measured parameters during an ergometry, the WL and the WWR for all ergometries together


Figure 5.19: Correlation of the blood parameters, the WL and the WWR of all ergometries together

### 5.2.2 Scatter plots

For the variables of the basic information scatter plots with the WWR are shown. Figure 5.20 shows scatter plots for the variables height, age, weight and waist and the WWR and Figure 5.21 shows the plots for the calculated variables BMI, WHR and BSA and the WWR. In both Figures also regression lines are drawn in.

(a) Scatter plot between height and maximum workload-to-weight-ratio

(c) Scatter plot between weight and maximum workload-to-weight-ratio

(b) Scatter plot between age and maximum workload-to-weight-ratio

(d) Scatter plot between waist and maximum workload-to-weight-ratio

Figure 5.20: Scatter plots between the variables of the basic information and the maximum workload-to-weight-ratio

(a) Scatter plot between body mass index and maximum workload-to-weight-ratio

(b) Scatter plot between waist-to-heightratio and maximum workload-to-weightratio

(c) Scatter plot between body surface area and maximum workload-to-weight-ratio

Figure 5.21: Scatter plots between the calculated varaibles of the basic information and the maximum workload-to-weight-ratio

### 5.3 Quality control of the data

Figure 5.22 asserts that the maximum workload is distributed similarly at the beginning (2004 \& 2005) and the end of the study (2016 \& 2017). A deviation of the maximum workload in the beginning and the end of the study would point to an error in the measurement.


Figure 5.22: Quality control for the maximum workload during time

### 5.4 Discussion

In summary, in this chapter, the data is analyzed using both univariate and multivariate EDA. The first aim of this analysis was to analyze the data to find incorrect entries and eliminate them. Without checking the data for quality, incorrect entries would have an influence on the results of the regression ultimately yielding wrong results. The second objective was to get a general overview of the data and find its structures. These results can be further used in the next chapters, in which normal values for the maximum workload and the maximum workload-to-weight-ratio are derived.

The first observation of this analysis is that the variables weight, height and waist differ a lot in gender, whereas the BMI and WHR are similar for both genders. This observation can be used for choosing the variables for the regression analysis. Another observation is that the variable WWR has a higher correlation to the other variables than the maximum workload. Consequently, it is preferable to use the WWR as a prediction variable in the regression analysis instead of the maximum workload.

The cardiac parameters and the blood parameters have a low correlation to the maximum workload and the maximum workload-to-weight-ratio. Whereas, the variables of basic information have quite a good correlation to them. For this reason, the variables for cardiac parameters and blood parameters are omitted from further analysis. The EDA showed that there is approximately a linear relationship between the variables of basic information and the maximum workload and maximum workload-to-weight-ratio. Therefore a linear regression can be used for the calculation of normal values.

## Chapter 6

## Normal values for the maximum workload of exercise testing

The aim of this chapter is to model normal values for the maximum workload of ergometries. The chosen method for this is a linear regression. The currently used normal values for ergometries in Austria are suggested in the Austrian practice guidelines for ergometries (Wonisch et al., 2008]). However, the information about the applied data to develop this model is not available. For this reason, in this Chapter, the currently used normal values are analyzed and compared with new approaches which use similar independent variables. As a starting point, a correlation analysis is done in Section 1 followed by regression trees in Section 2. In Section 3 to Section 7 different models are introduced. Section 3 explains the model used. First, a linear regression model with the same effects is derived in Section 4. Afterwards, the best model with the same independent variables but with all main effects and all intersections is built in Section 5. Next, the model is extended by the variables weight and height in Section 6. As the last step in Section 7, instead of the maximum workload, the maximum workload-to-weight-ratio is used as the dependent variable. In Section 8, all models are compared along with a conclusion. Finally, in Section 9 a dummy regression model is introduced.

### 6.1 Correlation

Figure 6.1 shows the correlation between weight, height, age, body surface area (calculated with the formula of Du Bois), the outputs of an ergometry maximum workload and maximum workload-to-weight-ratio. In this chapter, there are regression models for the maximum workload as well as for the maximum workload-to-weight-ratio. One result of Chapter 5 is that the maximum workload-to-weight-ratio is preferable over the maximum workload.

Since the body surface area is calculated with the formula of Du Bois, the correlation in Figure 6.1 between it and the weight and height is very high. The correlation between the other independent variables is quite low.


Figure 6.1: Analysis of correlation with the variables weight, height, age, BMI, BSA, maximum workload and maximum workload-to-weight-ratio

### 6.2 Regression trees

This section shows regression trees for the maximum workload and the maximum workload-to-weight-ratio, respectively, in Figure 6.2 and Figure 6.3 .

(a) Regression tree for the maximum workload (b) Regression tree for the maximum workload-to-weight-ratio

Figure 6.2: Regression trees for males with the independent variables weight, height, age, body surface area and the dependent variables maximum workload and maximum workload-to-weight-ratio

The structure of the trees is the same for males and females, i.e. in the regression trees for the maximum workload in both decision vertices the age
plays a role and in the regression trees for the maximum workload-to-weightratio, the first vertex splits the age and the second one the weight.

(a) Regression tree for the maximum workload (b) Regression tree for the maximum workload-to-weight-ratio

Figure 6.3: Regression trees for females with the independent variables weight, height, age, BSA and the dependent variables maximum workload and maximum workload-to-weight-ratio

### 6.3 Model P: Linear regression model from the Austrian practice guidelines for ergometries

The Austrian practice guidelines for ergometries ([Wonisch et al., 2008]) contains a formula for the physical performance. This formula traced back to the publication from [Arstila, 1972]. With this formula, the normal values of the maximum workload can be calculated by knowing the body surface area and the age. Because males and females reach different values, there exist two different formulas separated by gender:

$$
\begin{aligned}
\text { male: } W L_{\max }[W] & =6.773+136.141 B S A\left[m^{2}\right]-0.916 B S A\left[m^{2}\right] \text { age }[y] \\
\text { female: } W L_{\max }[W] & =3.933+86.641 B S A\left[m^{2}\right]-0.346 B S A\left[m^{2}\right] \text { age }[y] .
\end{aligned}
$$

For determining the body surface area the formula of Du Bois is used in the formulas above (see [Du Bois and Du Bois, 1916]):

$$
\text { BSA }\left[\mathrm{m}^{2}\right]=0.007148 \text { weight }[\mathrm{kg}]^{0.425} \text { height }[\mathrm{cm}]^{0.725}
$$

Applying this formula on the data from ZARG provides the results in Table 6.1 .

| response variable | Model P |  |
| :--- | :---: | :---: |
|  | male | female |
| SSR | 20430888 | 1745237 |
| SSE | 39733086 | 9513851 |
| SST | 60964358 | 12347738 |
| $R_{a d j}^{2}$ | 0.3483 | 0.2295 |

Table 6.1: Results of Model P

### 6.4 Model 1: Linear regression model for the maximum workload depending on the surface and the interaction of the BSA and the age

Model 1 has the same main effect and interactions as the currently used model, i.e. the surface and the interaction between the BSA and the age:

$$
W \hat{W} L[W]=\hat{\beta}_{0}+\hat{\beta}_{1} B S A\left[m^{2}\right]+\hat{\beta}_{2} B S A\left[m^{2}\right] \text { age }[y] .
$$

### 6.4.1 Analysis of the model

Table 6.2 and Table 6.3 summarize the results of Model 1 for males and females. In the models for both genders, all coefficients are highly significant. The adjusted coefficient of determination $R_{a d j}^{2}$ is for male 0.3744 and for female it is 0.4055 .

| WL ~BSA + BSA : age |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |  |
|  | Estimate | Std. Error | t value | $\operatorname{Pr}(>\|t\|)$ |  |  |
| (Intercept) | 93.19284 | 4.05615 | 22.98 | $<2 \mathrm{e}-16$ | ** |  |
| BSA | 105.67996 | 2.02190 | 52.27 | $<2 \mathrm{e}-16$ | *** |  |
| BSA:age | -1.09894 | 0.01102 | -99.74 | $<2 \mathrm{e}-16$ | *** |  |
| RSE | 44.9 on 18916 degrees of freedom |  |  |  |  |  |
| $R^{2}$ | 0.3745 |  |  |  |  |  |
| $R_{\text {adj }}^{2}$ | 0.3744 |  |  |  |  |  |
| F-statistic | 5663 on 2 and 18916 DF |  |  |  |  |  |
|  | Df | Sum Sq | Mean Sq | F value | $\operatorname{Pr}(>\mathrm{F})$ |  |
| BSA | 1 | 2777209 | 2777209 | 1377.6 | <2.2e-16 | *** |
| BSA:age | 1 | 20054085 | 20054085 | 9947.9 | <2.2e-16 | *** |
| Residuals | 18916 | 38133065 | 2016 |  |  |  |
| Signif. codes | $0^{\text {'***' }} 0.00$ | ${ }^{\prime * * \prime} 0.01{ }^{\text {'*' }}$ | 0.05 '.' 0.1 |  |  |  |

Table 6.2: Summary and ANOVA of Model 1 for males

| WL $\sim$ BSA $+B S A$ : age |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |  |
|  | Estimate | Std. Error | t value | $\operatorname{Pr}(>\|t\|)$ |  |  |
| (Intercept) | 67.2302 | 3.1903 | 21.07 | $<2 \mathrm{e}-16$ | *** |  |
| BSA | 83.0788 | 1.9365 | 42.90 | $<2 \mathrm{e}-16$ | *** |  |
| BSA:age | -0.9214 | 0.0116 | -79.41 | $<2 \mathrm{e}-16$ | *** |  |
| RSE | 27.5 on 9703 degrees of freedom |  |  |  |  |  |
| $R^{2}$ | 0.4057 |  |  |  |  |  |
| $R_{\text {adj }}^{2}$ | 0.4055 |  |  |  |  |  |
| F-statistic | 3311 on 2 and 9703 DF |  |  |  |  |  |
| p-value: | <2.2e-16 |  |  |  |  |  |
|  | Df | Sum Sq | Mean Sq | F value | $\operatorname{Pr}(>\mathrm{F})$ |  |
| BSA | 1 | 240237 | 240237 | 317.64 | $<2.2 \mathrm{e}-16$ | *** |
| BSA:age | 1 | 4768876 | 4768876 | 6305.32 | < 2.2e-16 | *** |
| Residuals | 9703 | 7338625 | 756 |  |  |  |
| Signif. codes | $0^{\text {'***' }} 0.00$ | $1^{\prime * * \prime} 0.01^{\text {** }}$ | 0.05 '.' 0.1 | ' 1 |  |  |

Table 6.3: Summary and ANOVA of Model 1 for females

### 6.4.2 Diagnostics of the model

The Box-Cox plots in Figure 6.4 show that a transformation of the maximum workload is necessary for both genders. Due to better comparability with the formula of [Wonisch et al., 2008] this is not done in Model 1.


Figure 6.4: Box-Cox plots of Model 1

Following the regression, the requirements of the regression model have to be checked. Figure 6.5 and Figure 6.6 show the results of the diagnostics for male and female, respectively.

The first plot of Figure 6.5 and Figure 6.6, respectively, shows a scatter plot between residuals and predicted values. For both genders, a small pattern is


Figure 6.5: Diagnostic plots of Model 1 for males
recognizable, although it should look random. The second plot of Figure 6.5 and Figure 6.6 shows a Q-Q plot of the residuals. It will give a straight line if the errors are normally distributed. Both plots for males and females show that for very small and big values there is a deviation from this line, i.e. there is a skinny positive and skinny negative tail. The third plot of Figure 6.5 and Figure 6.6 should look random with no patterns, which is the case in both plots. The last plot of Figure 6.5 and Figure 6.6 identifies the points which have the greatest influence on the regression (leverage points).

### 6.4.3 Confidence intervals and prediction intervals for Model 1

In this subsection, the confidence intervals and prediction intervals are created in Table 6.4 for males and in Table 6.5 for females. In this table, for the age and BSA, three different values are chosen. One can see that the confidence intervals are much tighter than the prediction intervals. Note, that the intervals are not reasonable for Model 1, because in Model 1 there was no transformation done although it was necessary.


Figure 6.6: Diagnostic plots of Model 1 for females

| Men |  |  |  |
| :---: | :---: | :---: | :---: |
| age/BSA | 1.5 | 2 | 2.5 |
| 25 | $[208.04,212.96]$ | $[248.08,251.13]$ | $[286.2,291.21]$ |
|  | $[122.46,298.54]$ | $[161.59,337.63]$ | $[200.67,376.75]$ |
| 50 | 169.29 | 194.66 | 220.03 |
|  | $[167.16,171.42]$ | $[193.95,195.37]$ | $[217.97,222.09]$ |
|  | $[81.26,257.32]$ | $[106.65,282.67]$ | $[132,308.06]$ |
| 75 | 128.08 | 139.71 | 151.34 |
|  | $[126,130.16]$ | $[138.71,140.71]$ | $[148.92,153.76]$ |
|  | $[40.05,216.11]$ | $[51.7,227.72]$ | $[63.3,239.38]$ |

Table 6.4: Prediction values for the maximum workload [W] (first row), confidence intervals (second row) and prediction intervals (third row) of Model 1 for males

### 6.4.4 Regression surface of Model 1

| Women |  |  |  |
| :---: | :---: | :---: | :---: |
| age/BSA | 1.5 | 2 | 2.5 |
| 25 | 157.3 | 187.32 | 217.34 |
|  | $[155.74,158.85]$ | $[185.44,189.19]$ | $[213.98,220.7]$ |
|  | $[103.36,211.23]$ | $[133.38,241.26]$ | $[163.33,271.35]$ |
| 50 | 122.74 | 141.25 | 159.75 |
|  | $[121.68,123.81]$ | $[140.09,142.41]$ | $[156.93,162.58]$ |
|  | $[68.82,176.66]$ | $[87.33,195.17]$ | $[105.77,213.73]$ |
| 75 | 88.19 | 95.18 | 102.16 |
|  | $[87.06,89.33]$ | $[93.85,96.5]$ | $[99.21,105.12]$ |
|  | $[34.27,142.11]$ | $[41.25,149.1]$ | $[48.18,156.15]$ |

Table 6.5: Prediction values for the maximum workload [W] (first row), confidence intervals (second row) and prediction intervals (third row) of Model 1 for females


Figure 6.7: Plots of the regression surface of Model 1

Figure 6.7 shows the regression surface of Model 1. One can see that there is a main effect and also interaction. This interaction can be seen more precisely in Figure 6.8. Here the age is fixed at the three different stages from the tables above. The slope of the regression lines of the surface is different for each of these ages. Additionally, the $95 \%$-confidence bands are plotted.


Figure 6.8: Plots of the regression line and confidence bands of the BSA for different ages of Model 1

### 6.5 Model 2: Linear regression model for the maximum workload depending on the body surface area and the age and its interaction

Based on the same independent variables, body surface area and age, the best model is chosen. Both main effects and the interaction can be considered, but to reduce the number of variables, a variable selection is done. Therefore, all possible subsets of the pool of the explanatory variables are calculated, and the model that fits the data best according to the chosen criterion is found.

### 6.5.1 Variable selection

Table 6.6 shows the best model for different numbers of parameters. In the best model with one parameter, just the age is chosen and in the best model with two parameters the BSA, and the age are chosen. This is in contrast to the model which is currently used, where the BSA and the interaction are used. This will hold for both males and females.

| no. of parameters | BSA | age | BSA:age |
| :---: | :---: | :---: | :---: |
| 1 | $*$ | $*$ |  |
| 2 | $*$ | $*$ | $*$ |
| 3 | $*$ | $*$ | $*$ |

Table 6.6: Summary of the best models with 1 to 3 parameters for deriving Model 2 for males and females

In a next step, the best model among these models in Table 6.6 is chosen. For this selection, Figure 6.9 shows plots for the different selection criteria. Fig-
ure 6.9 (a) shows the error sum of squares SSE, which should be small. The adjusted coefficient of determination $R_{a d j}^{2}$ is shown in Figure 6.9(b). The resulting value of the $R_{a d j}^{2}$ should be as high as possible. The chosen selection criterion for our models is the Bayesian Information Criterion because this criterion chooses quite small models.

(a) Graphical description of the error sum of squares for the best models with 1 to 4 parameters (blue lines refer to male, red lines refer to female)

(b) Graphical description of the $R_{a d j}^{2}$ for the best models with 1 to 3 parameters (blue lines refer to male, red lines refer to female)

(c) Graphical description of the BIC for the best models with 1 to 3 parameters
Figure 6.9: Information criteria for deriving Model 2
As a result in the final version of Model 2 for both males and females, the two variables BSA and age are chosen. Therefore, the following regression model is used:

$$
\hat{W} L^{0.7}[W]=\hat{\beta}_{0}+\hat{\beta}_{1} B S A\left[m^{2}\right]+\hat{\beta}_{2} \text { age }[y] .
$$

### 6.5.2 Analysis of the model

Table 6.7 and Table 6.8 show a summary of the chosen regressions for males and females. All coefficients are highly significant.

| WL ${ }^{0.7} \sim$ BSA + age |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |  |
|  | Estimate | Std. Error | $t$ value | $\operatorname{Pr}(>\|t\|)$ |  |  |
| (Intercept) | 42.240422 | 0.655197 | 64.47 | $<2 \mathrm{e}-16$ | *** |  |
| BSA | 6.747887 | 0.300029 | 22.49 | $<2 \mathrm{e}-16$ | *** |  |
| age | -0.320909 | 0.003223 | -99.58 | <2e-16 | ** |  |
| RSE | 6.672 on 18916 degrees of freedom |  |  |  |  |  |
| $R^{2}$ | 0.3746 |  |  |  |  |  |
| $R_{\text {adj }}^{2}$ | 0.3745 |  |  |  |  |  |
| F-statistic | 5665 on 2 and 18916 DF |  |  |  |  |  |
| p-value: | <2.2e-16 |  |  |  |  |  |
|  | Df | Sum Sq | Mean Sq | F value | $\operatorname{Pr}(>\mathrm{F})$ |  |
| BSAe | 1 | 62933 | 62933 | 1413.8 | <2.2e-16 | *** |
| age | 1 | 441375 | 441375 | 9915.7 | < 2.2e-16 | *** |
| Residuals | 18916 | 842000 | 45 |  |  |  |
| Signif. codes | $0^{\text {'***' }} 0.00$ | '**' $0.01{ }^{\prime * \prime}$ | 0.05 '.' 0.1 |  |  |  |

Table 6.7: Summary and ANOVA of Model 2 for males

| WL ${ }^{0.7} \sim$ BSA + age |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |  |
|  | Estimate | Std. Error | t value | $\operatorname{Pr}(>\|t\|)$ |  |  |
| (Intercept) | 34.562048 | 0.576806 | 59.92 | $<2 \mathrm{e}-16$ | *** |  |
| BSA | 5.102416 | 0.308410 | 16.54 | $<2 \mathrm{e}-16$ | *** |  |
| age | -0.265126 | 0.003363 | -78.83 | $<2 \mathrm{e}-16$ | *** |  |
| RSE | 4.636 on 9703 degrees of freedom |  |  |  |  |  |
| $R^{2}$ | 0.4026 |  |  |  |  |  |
| $R_{\text {adj }}^{2}$ | 0.4025 |  |  |  |  |  |
| F-statistic | 3270 on 2 and 9703 DF |  |  |  |  |  |
| p-value: | $<2.2 \mathrm{e}-16$ |  |  |  |  |  |
|  | Df | Sum Sq | Mean Sq | F value | $\operatorname{Pr}(>\mathrm{F})$ |  |
| BSA | 1 | 6998 | 6998 | 325.6 | <2.2e-16 | *** |
| age | 1 | 133566 | 133566 | 6214.7 | < 2.2e-16 | *** |
| Residuals | 9703 | 208535 | 21 |  |  |  |
| Signif. codes | $0^{\text {'***' }} 0.00$ | '*** $0.01{ }^{\text {'*' }}$ | 0.05 '.' 0.1 |  |  |  |

Table 6.8: Summary and ANOVA of Model 2 for females

### 6.5.3 Diagnostics of the model

The Box-Cox plots in Figure 6.10 show that the already performed transformation of the maximum workload was necessary.


Figure 6.10: Box-Cox plots of Model 2


Figure 6.11: Diagnostic plots of Model 2 for males

Figure 6.11 and Figure 6.12 analyze Model 2 to check the requirements of the regression model for both male and female.


Figure 6.12: Diagnostic plots of Model 2 for females

### 6.5.4 Confidence intervals and prediction intervals for Model 2

In this subsection the confidence intervals and prediction intervals are created in Table 6.9 and in Table 6.10. In this table, for the age and BSA, the same values as for Model 1 are chosen. Note that the values of this tables are transformed back to the maximum workload itself.

| Men |  |  |  |
| :---: | :---: | :---: | :---: |
| age/BSA | 1.5 | 2 | 2.5 |
| 25 | $[222.35,228.06]$ | $[248.38,251.76]$ | $[273.05,278.37]$ |
|  | $[136.66,325.82]$ | $[158.23,353.48]$ | $[180.69,381.85]$ |
|  | 169.33 | 192.24 | 216 |
|  | $[167.21,171.45]$ | $[191.51,192.97]$ | $[213.81,218.2]$ |
|  | $[89.46,262.78]$ | $[108.6,288.76]$ | $[128.78,315.52]$ |
| 75 | 118.54 | 139.23 | 160.9 |
|  | $[116.66,120.42]$ | $[138.31,140.16]$ | $[158.65,163.15]$ |
|  | $[48.85,204]$ | $[65.05,228.15]$ | $[82.53,253.15]$ |

Table 6.9: Prediction values for the maximum workload [W] (first row), confidence intervals (second row) and prediction intervals (third row) of Model 2 for males

| Women |  |  |  |
| :---: | :---: | :---: | :---: |
| age/BSA | 1.5 | 2 | 2.5 |
| 25 | 164.49 | 181.59 | 199.19 |
|  | $[162.62,166.37]$ | $[179.63,183.56]$ | $[195.58,202.82]$ |
|  | $[107.92,227.66]$ | $[123.07,246.46]$ | $[138.73,265.78]$ |
| 50 | 122.54 | 138.25 | 154.51 |
|  | $[121.44,123.64]$ | $[137.04,139.45]$ | $[151.45,157.58]$ |
|  | $[71.54,180.98]$ | $[85.02,198.56]$ | $[99.11,216.7]$ |
| 75 | 84.53 | 98.66 | 113.42 |
|  | $[83.46,85.61]$ | $[97.45,99.87]$ | $[110.57,116.29]$ |
|  | $[40.07,137.68]$ | $[51.53,153.93]$ | $[63.77,170.77]$ |

Table 6.10: Prediction values for the maximum workload [W] (first row), confidence intervals (second row) and prediction intervals (third row) of Model 2 for females

### 6.5.5 Regression surface of Model 2

Figure 6.13 shows the regression surface of the regression for males and females.
In Figure 6.14 as well as in Figure 6.15 the age is fixed in three different stages from the tables above. In both figures, the slope of the regression lines is always the same, because there is no interaction. Additionally, the $95 \%$-confidence bands are plotted.


Figure 6.13: Plots of the regression surface for Model 2


Figure 6.14: Plots of the regression lines and confidence bands of the surface for different ages of Model 2

### 6.6 Model 3: Linear regression model for the maximum workload to weight ratio depending on BSA and age and its interaction

In the next modification, the maximum-workload-to-weight-ratio is the depended variable instead of the maximum workload.

### 6.6.1 Variable selection

The best models with one to three variables for males and females are shown in Table 6.11 .


Figure 6.15: Plots of the regression lines and confidence bands of the age for different surfaces of Model 2

| no. | BSA | age | BSA:age |
| :---: | :---: | :---: | :---: |
| 1 | $*$ | $*$ | $*$ |
| 2 | $*$ | $*$ | $*$ |
| 3 | $*$ | $*$ | $*$ |

Table 6.11: Summary of the best models with 1 to 3 parameters for deriving Model 3

For choosing the best model out of these, Figure 6.16 shows plots for the information criteria.

As a result, 3 parameters can be chosen. Therefore, the following regression model will be used:

$$
W \hat{W} R^{0.6}[W]=\hat{\beta}_{0}+\hat{\beta}_{1} B S A\left[m^{2}\right]+\hat{\beta}_{2} \text { age }[y]+\hat{\beta}_{3} B S A\left[m^{2}\right] \text { age }[y] .
$$


(a) Graphical description of the error sum of squares for the best models with 1 to 3 variables
(b) Graphical description of the $R_{a d j}^{2}$ for the best models with 1 to 3 variables

(c) Graphical description of the BIC for the best models with 1 to 3 variables

Figure 6.16: Information criteria for deriving Model 3

### 6.6.2 Analysis of the model

In Table 6.12 and Table 6.13 summary and ANOVA are presented for males and females.

| WWR ${ }^{0.6} \sim B S A * a g e$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |  |
|  | Estimate | Std. Error | t value | $\operatorname{Pr}(>\|t\|)$ |  |  |
| (Intercept) | 3.9290491 | 0.0837277 | 46.927 | $<2 \mathrm{e}-16$ | *** |  |
| BSA | -0.8184991 | 0.0422183 | -19.387 | $<2 \mathrm{e}-16$ | *** |  |
| age | -0.0213401 | 0.0014378 | -14.842 | $<2 \mathrm{e}-16$ | *** |  |
| BSA:age | 0.0043623 | 0.0007305 | 5.972 | $2.39 \mathrm{e}-09$ | *** |  |
| RSE | 0.2523 on 18915 degrees of freedom |  |  |  |  |  |
| $R^{2}$ | 0.3942 |  |  |  |  |  |
| $R_{\text {adj }}^{2}$ | 0.3941 |  |  |  |  |  |
| F-statistic | 4103 on 3 and 18915 DF |  |  |  |  |  |
| p-value: | $<2.2 \mathrm{e}-16$ |  |  |  |  |  |
|  | Df | Sum Sq | Mean Sq | F value | $\operatorname{Pr}(>\mathrm{F})$ |  |
| BSA | 1 | 80.87 | 80.87 | 1270.325 | <2.2e-16 | *** |
| age | 1 | 700.48 | 700.48 | 11003.647 | <2.2e-16 | *** |
| BSA:age | 1 | 2.27 | 2.27 | 35.664 | $2.387 \mathrm{e}-09$ | *** |
| Residuals | 18915 | 1204.12 | 0.06 |  |  |  |
| Signif. codes | $0^{\text {'***' }} 0.001$ | ***' $0.01{ }^{\text {* }}$ | .05 '.' 0.1 |  |  |  |

Table 6.12: Summary and ANOVA of Model 3 for males

| WWR ${ }^{0.6} \sim B S A *$ age |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |  |
|  | Estimate | Std. Error | t value | $\operatorname{Pr}(>\|t\|)$ |  |  |
| (Intercept) | 3.786664 | 0.099688 | 37.98 | $<2 \mathrm{e}-16$ | *** |  |
| BSA | -0.958777 | 0.057894 | -16.56 | <2e-16 | *** |  |
| age | -0.021056 | 0.001673 | -12.59 | < 2e-16 | *** |  |
| BSA:age | 0.004878 | 0.000973 | 5.01 | $5.4 \mathrm{e}-07$ | *** |  |
| RSE | 0.21 on 9702 degrees of freedom |  |  |  |  |  |
| $R^{2}$ | 0.487 |  |  |  |  |  |
| $R_{\text {adj }}^{2}$ | 0.487 |  |  |  |  |  |
| F-statistic p-value: | $3.08 \mathrm{e}+03$ on 3 and 9702 DF$<2.2 \mathrm{e}-16$ |  |  |  |  |  |
|  | Df | Sum Sq | Mean Sq | F value | $\operatorname{Pr}(>\mathrm{F})$ |  |
| BSA | 1 | 97 | 96.9 | 2209.8 | < 2e-16 | *** |
| age | 1 | 307 | 306.6 | 6990.3 | < 2e-16 | *** |
| BSA:age | 1 | 1 | 1.1 | 25.1 | $5.4 \mathrm{e}-07$ | *** |
| Residuals | 9702 | 426 | 0.0 |  |  |  |
| Signif. codes | $0^{\text {'***' }} 0.00$ | $1^{\text {*** }} 0.01^{\text {** }}$ | 0.05 '. 0.1 | '1 |  |  |

Table 6.13: Summary and ANOVA of Model 3 for females

### 6.6.3 Diagnostics of the model

The Box-Cox plots in Figure 6.17 show that the already performed transformation of the maximum workload was necessary.


Figure 6.17: Box-Cox plot of Model 3


Figure 6.18: Diagnostic plots of Model 3 for males

Figure 6.18 and Figure 6.19 analyze Model 3 to check the requirements.


Figure 6.19: Diagnostic plots of Model 3 for females

### 6.6.4 Confidence intervals and prediction intervals for Model 3

In this subsection, the confidence intervals and prediction intervals are created in Table 6.14 and in Table 6.15. In these tables for the age and BSA, again the same values are chosen. Note that the values of this tables refer to the maximum workload to weight ratio instead of the maximum workload.

| Men |  |  |  |
| :---: | :---: | :---: | :---: |
| age/BSA | 1.5 | 2 | 2.5 |
| 25 | 4.1 | 3.11 | 2.24 |
|  | $[4.02,4.17]$ | $[3.09,3.14]$ | $[2.18,2.3]$ |
|  | $[2.75,5.65]$ | $[1.93,4.52]$ | $[1.22,3.49]$ |
| 50 | 3.07 | 2.33 | 1.67 |
|  | $[3.04,3.11]$ | $[2.32,2.34]$ | $[1.65,1.7]$ |
|  | $[1.89,4.47]$ | $[1.29,3.6]$ | $[0.79,2.8]$ |
| 75 | 2.17 | 1.64 | 1.17 |
|  | $[2.13,2.21]$ | $[1.63,1.65]$ | $[1.14,1.21]$ |
|  | $[1.17,3.41]$ | $[0.76,2.76]$ | $[0.43,2.18]$ |

Table 6.14: Prediction values for the maximum workload-to-weight-ratio [W/kg] (first row), confidence intervals (second row) and prediction intervals (third row) of Model 3 for males

| Women |  |  |  |
| :---: | :---: | :---: | :---: |
| age/BSA | 1.5 | 2 | 2.5 |
| 25 | 3.19 | 2.16 | 1.3 |
|  | $[3.14,3.24]$ | $[2.11,2.21]$ | $[1.2,1.4]$ |
|  | $[2.18,4.35]$ | $[1.31,3.17]$ | $[0.62,2.15]$ |
| 50 | 2.33 | 1.56 | 0.91 |
|  | $[2.31,2.35]$ | $[1.54,1.58]$ | $[0.87,0.95]$ |
|  | $[1.45,3.37]$ | $[0.83,2.46]$ | $[0.35,1.67]$ |
| 75 | 1.58 | 1.04 | 0.59 |
|  | $[1.56,1.61]$ | $[1.01,1.06]$ | $[0.54,0.63]$ |
|  | $[0.85,2.49]$ | $[0.44,1.82]$ | $[0.14,1.24]$ |

Table 6.15: Prediction values for the maximum workload-to-weight-ratio [W/kg] (first row), confidence intervals (second row) and prediction intervals (third row) of Model 3 for females

### 6.6.5 Regression surface of Model 3

Figure 6.20 shows the regression surface of the regression for males and females.
In Figure 6.21 as well as in Figure 6.22, the age is fixed in three different stages from the tables above. In both figures, the slope is changing because of the interaction. Additionally, the $95 \%$-confidence bands are plotted.


Figure 6.20: Plots of the regression surface for Model 3


Figure 6.21: Plots of the regression lines and confidence bands of the surface for different ages for Model 3

### 6.7 Model 4: Linear regression model for the maximum workload to weight ratio depending on height, weight and age

To reduce the number of variables a variable selection is made. Therefore, all possible subsets of the pool of explanatory variables are calculated, and the model that best fits the data according to the BIC is developed.


Figure 6.22: Plots of the regression lines and confidence bands of the age for different surfaces for Model 3

### 6.7.1 Variable selection

Table 6.16 and Table 6.17 show the best model for different numbers of parameters for males and females, respectively. For example, in the best model for males with four parameters the height, age and the interaction between height and weight and between height and age are chosen. Whereas, in the best model for females with four parameters the weight, age and the interaction between weight and age and between height, weight and age are chosen.

| no. height | weight | age | height:weight | age:height | weight:age | height:weight:age |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  | $*$ | $*$ |
| 2 |  | $*$ | $*$ |  | $*$ |  | $*$ |
| 3 | $*$ |  | $*$ | $*$ | $*$ |  |  |
| 4 | $*$ |  | $*$ | $*$ | $*$ |  | $*$ |
| 5 | $*$ | $*$ | $*$ | $*$ |  | $*$ | $*$ |
| 6 | $*$ | $*$ | $*$ | $*$ | $*$ | $*$ | $*$ |
| 7 | $*$ |  |  |  |  |  |  |

Table 6.16: Summary of the best models with 1 to 7 parameters for deriving Model 4 for males

In the next step, the best model among these models in Table 6.16 is chosen. As in the model above, the BIC is the chosen criterion. Figure 6.23 shows plots for the information criteria.

For convenience, for both males and females, three parameters are chosen. This has the advantage that both regressions have the same parameters

$$
W \hat{W} R^{0.6}[W]=\hat{\beta}_{0}+\hat{\beta}_{1} \text { weight }[\mathrm{kg}]+\hat{\beta}_{2} \text { age }[y]+\hat{\beta}_{3} h e i g h t[\text { cm }] \text { age }[y] .
$$



Table 6.17: Summary of the best models with 1 to 7 parameters for deriving Model 4 for females

(a) Graphical description of the error sum of squares for the best models with 1 to 7 variables

(b) Graphical description of the $R_{a d j}^{2}$ for the best models with 1 to 7 variables

(c) Graphical description of the BIC for the best models with 1 to 7 variables

Figure 6.23: Information criteria for deriving Model 4

### 6.7.2 Analysis of the model

In Table 6.18 and in Table 6.19 a summary and ANOVA are presented.

| WWR ${ }^{0.6} \sim$ weight + age + age $:$ height |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |  |
|  | Estimate | Std. Error | t value | $\operatorname{Pr}(>\|t\|)$ |  |  |
| (Intercept) | $3.160 \mathrm{e}+00$ | $1.362 \mathrm{e}-02$ | 232.07 | $<2 \mathrm{e}-16$ | *** |  |
| weight | -1.140e-02 | $1.463 \mathrm{e}-04$ | -77.91 | $<2 \mathrm{e}-16$ | *** |  |
| age | -4.413e-02 | 8.675e-04 | -50.87 | $<2 \mathrm{e}-16$ | *** |  |
| age:height | $1.875 \mathrm{e}-04$ | $5.067 \mathrm{e}-06$ | 37.01 | $<2 \mathrm{e}-16$ | *** |  |
| RSE | 0.2342 on 18915 degrees of freedom |  |  |  |  |  |
| $R^{2}$ | 0.4782 |  |  |  |  |  |
| $R_{\text {adj }}^{2}$ | 0.4781 |  |  |  |  |  |
| F-statistic | 5777 on 3 and 18915 DF |  |  |  |  |  |
| p-value: | <2.2e-16 |  |  |  |  |  |
|  | Df | Sum Sq | Mean Sq | $F$ value | $\operatorname{Pr}(>\mathrm{F})$ |  |
| weight | 1 | 214.85 | 214.85 | 3918.0 | $<2.2 \mathrm{e}-16$ | *** |
| age | 1 | 660.53 | 660.53 | 12045.1 | <2.2e-16 | ** |
| age:height | 1 | 75.09 | 75.09 | 1369.4 | < 2.2e-16 | *** |
| Residuals | 18915 | 1037.26 | 0.05 |  |  |  |
| Signif. codes | $0^{\text {'***' }} 0.00$ | '**' $0.01{ }^{\prime * \prime}$ | 0.05 '. 0.1 |  |  |  |

Table 6.18: Summary and ANOVA of Model 4 for males

| WWR ${ }^{0.6} \sim$ weight + age + age $:$ height |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |  |
|  | Estimate | Std. Error | t value | $\operatorname{Pr}(>\|t\|)$ |  |  |
| (Intercept) | $2.775 \mathrm{e}+00$ | $1.330 \mathrm{e}-02$ | 208.68 | <2e-16 | *** |  |
| weight | -1.089e-02 | $1.639 \mathrm{e}-04$ | -66.45 | $<2 \mathrm{e}-16$ | *** |  |
| age | -3.374e-02 | $9.083 \mathrm{e}-04$ | -37.15 | <2e-16 | *** |  |
| age:height | $1.394 \mathrm{e}-04$ | $5.732 \mathrm{e}-06$ | 24.32 | $<2 \mathrm{e}-16$ | *** |  |
| RSE | 0.1937 on 9702 degrees of freedom |  |  |  |  |  |
| $R^{2}$ | 0.5616 |  |  |  |  |  |
| $R_{\text {adj }}^{2}$ | 0.5615 |  |  |  |  |  |
| F-statistic | 4143 on 3 and 9702 DF |  |  |  |  |  |
| p-value: | <2.2e-16 |  |  |  |  |  |
|  | Df | Sum Sq | Mean Sq | F value | $\operatorname{Pr}(>F)$ |  |
| weight | 1 | 175.68 | 175.680 | 4683.15 | <2.2e-16 | * |
| age | 1 | 268.44 | 268.435 | 7155.75 | < 2.2e-16 | *** |
| age:height | 1 | 22.19 | 22.187 | 591.46 | < 2.2e-16 | *** |
| Residuals | 9702 | 363.95 | 0.038 |  |  |  |
| Signif. codes | $0^{\text {'***' }} 0.00$ | '**' $0.01{ }^{\text {'*' }}$ | 0.05 '.' 0.1 |  |  |  |

Table 6.19: Summary and ANOVA of Model 4 for females

### 6.7.3 Diagnostics of the model

The Box-Cox plots in Figure 6.24 show that the already performed transformation of the maximum workload was necessary.


Figure 6.24: Box-Cox plots of Model 4


Figure 6.25: Diagnostic plots of Model 4 for males

Figure 6.25 and Figure 6.26 analyze Model 4 to check the requirements of the regression model for males and females, respectively.


Figure 6.26: Diagnostic plots of Model 4 for females

### 6.7.4 Confidence intervals and prediction intervals for Model 4

In this subsection, the confidence intervals and prediction intervals are created in Table 6.20 for men and in Table 6.21 for women. In this tables, the variables age, weight and height are necessary.

| Men, weight=70 |  |  |  |
| :---: | :---: | :---: | :---: |
| age/height | 170 | 180 | 190 |
| 25 | 3.32 | 3.45 | 3.58 |
|  | [3.3,3.35] | [3.43,3.48] | [3.55,3.61] |
|  | [2.18,4.65] | [2.29,4.8] | [2.4,4.94] |
| 50 | 2.54 | 2.77 | 3.01 |
|  | [2.53,2.55] | [2.76,2.79] | [2.99,3.04] |
|  | [1.53,3.75] | [1.72,4.01] | [1.92,4.29] |
| 75 | 1.84 | 2.15 | 2.48 |
|  | [1.83,1.86] | [2.13,2.17] | [2.45,2.51] |
|  | [0.97, 2.92] | [1.22,3.29] | [1.48,3.68] |
| Men, weight=90 |  |  |  |
| age/height | 170 | 180 | 190 |
| 25 | 2.73 | 2.85 | 2.97 |
|  | [2.71,2.76] | [2.83,2.87] | [2.95,2.99] |
|  | [1.69,3.97] | [1.79,4.11] | [1.88,4.25] |
| 50 | 2.01 | 2.22 | 2.44 |
|  | [2,2.03] | [2.21,2.23] | [2.43,2.46] |
|  | [1.11,3.12] | [1.27,3.37] | [1.45,3.63] |
| 75 | 1.38 | 1.66 | 1.96 |
|  | [1.37,1.4] | [1.65,1.67] | [1.93,1.98] |
|  | [0.63,2.36] | [0.83,2.7] | [1.06,3.06] |
| Men, weight=110 |  |  |  |
| age/height | 170 | 180 | 190 |
| 25 | 2.19 | 2.3 | 2.41 |
|  | [2.16,2.22] | [2.27,2.32] | [2.38,2.43] |
|  | [1.25,3.33] | [1.33,3.46] | [1.42,3.59] |
| 50 | 1.54 | 1.73 | 1.92 |
|  | [1.52,1.56] | [1.71,1.74] | [1.91,1.94] |
|  | [0.74,2.55] | [0.88,2.78] | [1.04,3.02] |
| 75 | 0.98 | 1.22 | 1.49 |
|  | [0.96,1] | [1.21,1.24] | [1.46,1.51] |
|  | [0.35, 1.85] | [0.51,2.16] | [0.7,2.49] |

Table 6.20: Prediction values for the maximum workload-to-weight-ratio $[\mathrm{W} / \mathrm{kg}]$ (first row), confidence intervals (second row) and prediction intervals (third row) of Model 4 for males

### 6.7.5 Regression surface of Model 4

Figure 6.27 shows the regression surface of the regression for males and females.
Figure 6.28 and Figure 6.29 visualize the regression function. In both plots, the age is fixed in three different stages from the tables above. Figure 6.28 shows that there is no interaction between weight and height. In contrary to that, the interaction between age and height can be observed in Figure 6.29. In both plots, the parameter which is not used is set to the median value and additionally, the

| Women, weight=50 |  |  |  |
| :---: | :---: | :---: | :---: |
| age/height | 150 | 165 | 180 |
| 25 | 2.94 | 3.07 | 3.21 |
|  | [2.91,2.97] | [3.05,3.1] | [3.18,3.24] |
|  | [2.03,3.98] | [2.15,4.13] | [2.27,4.28] |
| 50 | 2.16 | 2.41 | 2.66 |
|  | [2.14,2.19] | [2.39,2.42] | [2.63,2.69] |
|  | [1.37,3.09] | [1.58,3.37] | [1.79,3.66] |
| 75 | 1.49 | 1.8 | 2.15 |
|  | [1.46,1.51] | [1.78,1.83] | [2.11,2.19] |
|  | [0.82,2.3] | [1.08,2.68] | [1.36,3.08] |
| Women, weight=70 |  |  |  |
| age/height | 150 | 165 | 180 |
| 25 | 2.4 | 2.53 | 2.65 |
|  | [2.37,2.43] | [2.5,2.55] | [2.63,2.68] |
|  | [1.57,3.37] | [1.68,3.51] | [1.79,3.65] |
| 50 | 1.69 | 1.91 | 2.14 |
|  | [1.67,1.71] | [1.9,1.92] | [2.12,2.17] |
|  | [0.99,2.54] | [1.17,2.8] | [1.36,3.07] |
| 75 | 1.09 | 1.37 | 1.68 |
|  | [1.07,1.11] | [1.36,1.38] | [1.65,1.71] |
|  | [0.51,1.82] | [0.73,2.16] | [0.97,2.53] |
| Women, weight=90 |  |  |  |
| age/height | 150 | 165 | 180 |
| 25 | 1.91 | 2.02 | 2.14 |
|  | [1.88,1.94] | [1.99,2.05] | [2.11,2.17] |
|  | [1.16,2.8] | [1.26,2.93] | [1.35,3.07] |
| 50 | 1.27 | 1.47 | 1.67 |
|  | [1.24,1.29] | [1.45,1.48] | [1.65,1.7] |
|  | [0.65,2.04] | [0.81,2.28] | [0.97,2.52] |
| 75 | 0.74 | 0.98 | 1.26 |
|  | [0.72,0.76] | [0.97,1] | [1.23,1.28] |
|  | [0.27,1.38] | [0.44,1.69] | [0.64,2.02] |

Table 6.21: Prediction values for the maximum workload-to-weight-ratio $[\mathrm{W} / \mathrm{kg}]$ (first row), confidence intervals (second row) and prediction intervals (third row) of Model 4 for females
$95 \%$-confidence bands are plotted.


Figure 6.27: Plots of the regression surface for Model 4


Figure 6.28: Plots of the regression lines and confidence bands of the weight for different ages of Model 4

### 6.8 Comparison of the models

In this section the models are compared.

### 6.8.1 Summary of the models

Model 1: $\hat{W} L[W]=\hat{\beta}_{0}+\hat{\beta}_{1} B S A\left[m^{2}\right]+\hat{\beta}_{2} B S A\left[m^{2}\right]$ age $[y]$
Model 2: $W L^{0.7}[W]=\hat{\beta}_{0}+\hat{\beta}_{1} B S A\left[m^{2}\right]+\hat{\beta}_{2}$ age $[y]$
Model 3: $W \hat{W} R^{0.6}[\mathrm{~W} / \mathrm{kg}]=\hat{\beta}_{0}+\hat{\beta}_{1} B S A\left[\mathrm{~m}^{2}\right]+\hat{\beta}_{2}$ age $[y]+\hat{\beta}_{3} B S A\left[m^{2}\right]$ age $[y]$
Model 4: $W \hat{W} R^{0.6}[W / \mathrm{kg}]=\hat{\beta}_{0}+\hat{\beta}_{1}$ weight $[\mathrm{kg}]+\hat{\beta}_{2}$ age $[y]+\hat{\beta}_{3} h$ eight $[\mathrm{cm}]$ age $[\mathrm{kg}]$


Figure 6.29: Plots of the regression lines and confidence bands of the age for different surfaces of Model 4

### 6.8.2 Comparison of the sum of squares and the adjusted coefficient of determination

To compare these models the coefficient of determination $R^{2}$ and the correlation are compared for males in Table 6.22 and for females in Table 6.23 .

| response variable | $W$ |  | $W^{0.7}$ | $W W R^{0.6}$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | Model P | Model 1 | Model 2 | Model 3 | Model 4 |
| SSR | 20430888 | 22831293 | 504308 | 783.6 | 950.5 |
| SSE | 39733086 | 38133065 | 842000 | 1204.12 | 1037.26 |
| SST | 60964358 | 60964358 | 1346308 | 1988 | 1988 |
| $R_{a d j}^{2}$ | 0.3483 | 0.3744 | 0.3745 | 0.3941 | 0.4781 |
| corr | 0.9740719 |  |  |  |  |

Table 6.22: Comparison of the Models for males

| response variable | $W$ |  | $W^{0.7}$ | $W W R^{0.6}$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | Model P | Model 1 | Model 2 | Model 3 | Model 4 |
| SSR | 1745237 | 5009113 | 140564 | 405 | 466.3 |
| SSE | 9513851 | 7338625 | 208535 | 426 | 363.95 |
| SST | 12347738 | 12347738 | 349099 | 831 | 830.2 |
| $R_{\text {adj }}^{2}$ | 0.2295 | 0.4055 | 0.4025 | 0.4870 | 0.5615 |
| corr | 0.7827556 |  |  |  |  |

Table 6.23: Comparison of the Models for females

### 6.8.3 Comparison of the surfaces

The three-dimensional regression surfaces are compared to show the difference between Model 1 and Model P. In both models, the same parameters are taken. Unfortunately, for the model from [Wonisch et al., 2008] no additional information, e.g. the distribution of age, is available. Figure 6.30 shows the difference between the surfaces of Model P and Model 1 for both males and females.


Figure 6.30: Surface of Model P and Model 1: orange surface belongs to Model $P$ and the blue surface belongs to Model 1

Figure 6.31 shows scatter plots between Model P and Model 1. In Figure $6.31(\mathrm{a})$, which shows the situation for males, one can see that the points are close to the red line. In Figure $6.31(\mathrm{~b})$, which shows the situation for females, one can see that the point cloud differs from the red line. This effect can be also seen in the discrepancy of the correlation.


Figure 6.31: Scatter plot of the maximum workloads for Model P and Model 1

### 6.9 Model D: Dummy linear regression model for the maximum workload to weight ratio depending on the height, weight and age and the dummy variables gender, diagnosis and medication

In addition to the maximum workload to weight ratio, the diagnosis and medication are included. To reduce the number of variables a variable selection is done. Therefore, all possible subsets of the pool of explanatory variables are calculated and the model that best fits the data according to the BIC is developed.

### 6.9.1 Regression tree

Figure 6.32 shows a regression tree for the variable WWR. The independent variables are BSA, age, height, weight, gender, diagnosis and medication.


Figure 6.32: Regression tree for the variables of Model D

### 6.9.2 Variable selection

Table 6.24 shows the best model for different numbers of parameters. For example in the best model with four parameters height, weight, age and the interaction between height and gender is chosen.

In a next step, the best model among models in Table 6.24 is chosen. As in the above model the BIC is the chosen criterion. Figure 6.33 shows plots for the information criteria.

Table 6.24: Summary of the best models with one to six parameters for deriving Model D

(a) Graphical description of the error sum of squares for the best models with 1 to 64 variables

(b) Graphical description of the $R_{a d j}^{2}$ for the best models with 1 to 6 variables

(c) Graphical description of the BIC for the best models with 1 to 6 variables

Figure 6.33: Information criteria for deriving Model D

For Model D the best model with six parameters is chosen:

$$
\begin{aligned}
& W \hat{W} R^{0.5}[W]=\quad \hat{\beta}_{0}+\hat{\beta}_{1} \text { weight }[k g]+\hat{\beta}_{2} \text { age }[y]+\hat{\beta}_{3} h e i g h t[\text { cm]age }[y] \\
& +\hat{\beta}_{5} h e i g h t[\mathrm{~cm}] M A L E+\hat{\beta}_{6} \text { age }[y] M A L E+\hat{\beta}_{4} h e i g h t[c m] M E D .
\end{aligned}
$$

### 6.9.3 Analysis of the model

In Table 6.25 a summary and ANOVA is presented.

| WWR ${ }^{0.6} \sim$ weight + age + height $:$ age |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |  |
|  | Estimate | Std. Error | t value | $\operatorname{Pr}(>\|t\|)$ |  |  |
| (Intercept) | $2.777 \mathrm{e}+00$ | 1.158e-02 | 239.82 | $<2 \mathrm{e}-16$ | *** |  |
| weight | -1.100e-02 | $1.114 \mathrm{e}-04$ | -98.79 | $<2 \mathrm{e}-16$ | *** |  |
| age | -3.463e-02 | $6.441 \mathrm{e}-04$ | -53.76 | $<2 \mathrm{e}-16$ | *** |  |
| age:height | $1.465 \mathrm{e}-04$ | 3.846e-06 | 38.08 | $<2 \mathrm{e}-16$ | *** |  |
| height:MALE | $1.989 \mathrm{e}-03$ | $6.320 \mathrm{e}-05$ | 31.46 | $<2 \mathrm{e}-16$ | *** |  |
| age:MALE | -2.053e-03 | $1.804 \mathrm{e}-04$ | -11.38 | $<2 \mathrm{e}-16$ | *** |  |
| height:MED | -3.225e-04 | $1.843 \mathrm{e}-05$ | -17.50 | <2e-16 | *** |  |
| RSE | 0.2201 on 28618 degrees of freedom |  |  |  |  |  |
| $R^{2}$ | 0.5455 |  |  |  |  |  |
| $R_{a d j}^{2}$ | 0.5454 |  |  |  |  |  |
| F-statistic | 5726 on 6 and 28618 |  |  |  |  |  |
| p-value: | <2.2e-16 |  |  |  |  |  |
|  | Df | Sum Sq | Mean Sq | F value | $\operatorname{Pr}(>\mathrm{F})$ |  |
| weight | 1 | 94.58 | 94.58 | 1952.41 | $<2.2 \mathrm{e}-16$ | *** |
| age | 1 | 995.48 | 995.48 | 20550.35 | < 2.2e-16 | *** |
| age:height | 1 | 388.27 | 388.27 | 8015.30 | < 2.2e-16 | *** |
| height:MALE | 1 | 164.06 | 164.06 | 3386.81 | < 2.2e-16 | *** |
| age:MALE | 1 | 6.89 | 6.89 | 142.15 | < 2.2e-16 | *** |
| height:MED | 1 | 14.83 | 14.83 | 306.21 | < 2.2e-16 | *** |
| Residuals | 28618 | 1386.29 | 0.05 |  |  |  |
| Signif. codes | $0^{\text {'***' }} 0.001$ | ${ }^{\prime * * \prime} 0.01^{\prime * \prime}$ | 0.05 '.' 0.1 |  |  |  |

Table 6.25: Summary and ANOVA of Model D

### 6.9.4 Diagnostics of the model

The Box-Cox plots in Figure 6.34 show that the already performed transformation of the maximum workload was necessary.

Figure 6.35 analyzes Model D to check the requirements of the regression model.


Figure 6.34: Box-Cox plots of Model D


Figure 6.35: Diagnostic plots of Model D

### 6.10 Discussion

In summary, in this chapter, different models for obtaining normal values for the maximum workload and the maximum workload-to-weight-ratio are ana-
lyzed. In Austria, Model P is currently used to calculate the normal values of ergometries. Based on this model, new models are derived. New models show that an improvement of the currently used model is possible. In Model P, the maximum workload is calculated based on BSA and the interaction between age and BSA. When compared to the newly developed Model 1, it can be observed that Model P has a poor goodness of fit for females. This could be due to the different structure of underlying data while deriving Model P. Secondly, Model 1 shows that a transformation of the prediction variable is necessary. The next model, Model 2, already includes the transformation of the prediction variable and uses a maximum model which includes both main effects and the interaction. Comparison of Model 2 shows that this model has no particular effect on the adjusted coefficient of determination, though it produces correct prediction and confidence intervals. Use of the maximum workload-to-weigth-ratio as a prediction variable instead of the maximum workload results in Model 3. Comparison with prior models shows that an increase of the adjusted coefficient of determination is possible. Model 4 is using weight and height instead of BSA and yields the best results among all these models.

Finally, a dummy regression model is introduced at the end of this chapter. This model D uses the information about the diagnosis and medication (statin and beta blocker) along with age, gender, weight, and height. In contrary to the other models, Model D used just one regression for males and females.

## Chapter 7

## Normal values for the maximum workload of exercise testing during cardiac out-patient rehabilitation

This chapter deals with the results of ergometries during cardiac out-patient rehabilitation. The data of the cardiac out-patient rehabilitation consists of the ergometries during stage II and stage III (see Chapter 2). For stage II there exists one ergometry at the entry examination and one at the final examination. During stage III there exists an ergometry additionally at the intermediate examination.

One of the reasons to execute these ergometries is to discover the physical constitution of the patients. This can be measured inter alia by the maximum workload which is achieved at the ergometries. To evaluate these results normal values can be used. Generally speaking the goal of this chapter is to find normal values of the maximum workload for these ergometries. Therefore, the following research questions are answered in this chapter:

1. What are the normal values of the maximum workload at the entry examination of stage II in cardiac out-patient rehabilitation?
2. How much should be contributed in stage II of cardiac out-patient rehabilitation?
3. What are the normal values of the maximum workload at the entry examination of stage III in cardiac out-patient rehabilitation?
4. How much should be contributed in stage III of cardiac out-patient rehabilitation?

The remainder of this chapter is the following: Section 7.1 shows the composition of the data and an analysis of the maximum workload. The next four sections are answering the research questions. Section 7.2 deals with the normal values for the entry examination of stage II. Afterwards the contribution during stage II is covered in Section 7.3 . Section 7.4 deals in the same manner with the normal values of stage III and Section 7.5 deals with the contribution during stage III. Finally Section 7.6 gives a short conclusion of the results.

### 7.1 Composition of the data

There is data of 5,029 ergometries during cardiac out-patient rehabilitation available in total. As a first step the composition of the data is analyzed in this section. For this purpose the data is split into four categories: reason for examination, gender, medication and diagnosis.

Starting with the purpose of examination, Figure 7.1(a) shows the number of ergometries during the different stages. The available data for stage II consist of 779 ergometries at the entry examination and 792 ergometries at the final examination. For stage III the data of 674 ergometries at the entry examination, 1,320 ergometries at the intermediate examination and 1,464 ergometries at the final examination are available. Note that there is no entry examination of stage III if stage III starts directly after stage II. In this case the final examination of stage II is the entry examination of stage III.

Figure 7.1(b) shows the split of ergometries by gender. In total the data consist of 3,870 ergometries done by men and 1,159 ergometries done by women. Concluding that the number of men in the cardiac out-patient rehabilitation is more than three times higher than the number of women.

(a) Number of ergometries during the different stages of cardiac out-patient rehabilitation (*Number without the occurences in which the final examination of stage II is also the entry examination of stage III)

(b) Number of ergometries split by gender

Figure 7.1: Number of ergometries during cardiac out-patient rehabilitation split by the reason for examination and gender

Another way of splitting the data is the medication and diagnosis. For the medication the drug groups statin and beta blocker are used and are noted in the following by heart medication. For more information about these medications see Section 2.5. Figure 7.2(a) shows split of ergometries in these medications. In the data 2,517 ergometries were done without statin and beta blocker and 2,512 ergometries were done under a heart medication. This means that around the half of the people did not take any heart medication.

Figure 7.2(b) shows the split of ergometries by diagnosis. The diagnosis is split into people which have a heart disease, e.g. infarct or coronal heart disease. For more information about the actual used diagnoses see Chapter $2.4,062$ ergometries were done with a heart disease and just 947 patients of cardiac outpatient rehabilitation does not have any heart disease. This was unexpected because typically just people with a heart disease make a cardiac rehabilitation.

(a) Number of ergometries separated by medication (nothing means neather statin nor betablocker)

(b) Number of ergometries separated by diagnosis (nothing means neather infarkt nor khk nor another kardio disease)

Figure 7.2: Number of ergometries during cardiac out-patient rehabilitation separated by medication or diagnosis

Finally the analysis of the maximum workload which is achieved in the ergometries during cardiac out-patient rehabilitation is shown in Figure 7.3. Figure 7.3(a) shows the maximum workload for males and Figure 7.3(b) shows the maximum workload for females. The first fact which can be observed is that the maximum workload is much less for females. In each sub-figure the data are further split into the different stages during cardiac outpatient-rehabilitation. For both males and females an increase of the maximum workload during stage II as well as during stage III can be observed. Another interesting result is that the maximum workload decreases between the two stages. One reason for this could be that the patients do not do any exercises during the break between stage II and stage III. A more precise analysis of the maximum workload during stage II and stage III is done in the following sections.

### 7.2 Normal values for the maximum workload of the entry examination of stage II during cardiac outpatient rehabilitation

In this section a linear regression is done for deriving normal values for the maximum workload of the entry examination of stage II during cardiac out-


Figure 7.3: Box plots of the maximum workload during the different stages of cardiac out-patient rehabilitation split by gender
patient rehabilitation. First the relevant variables are identified by a correlation analysis. Afterwards a regression tree is built to identify the main variables. Finally this section includes a regression model for deriving the normal values. Therefore also a variable selection is done. The resulting model is notated by Model RII (rehabilitation stage II).

For deriving normal values the waist circumference is a crucial variable. Unfortunately, not for all data the waist circumference is available. For this reason just the data which include values for the waist circumference are included. This constraint reduces the data from 779 to 430 ergometries.

### 7.2.1 Correlation

Figure 7.4 shows the correlation between all variables for male and female. In both correlation matrices the maximum workload-to-weight-ratio has a higher correlation to the other variables than the maximum workload. For this reason the normal values refer to the maximum workload-to-weight-ratio. Note that also further independent variables were considered at the beginning. The first group of variables are the variables which are measured in the beginning of the ergometry, i.e. resting heart rate, resting systolic blood pressure and resting diastolic blood pressure. The second group were the results of the laboratory, i.e. cholesterol, low-density lipoprotein, high-density lipoprotein, triglyceride, creatinine, fasting blood sugar level and uric acid. Due to the complexity in practice and the low correlation to the maximum workload-to-weight-ratio these variables are not used for the regression. The remaining independent variables weight, height, age, waist and waist-to-height-ratio form the pool of variables for the regression.


Figure 7.4: Analysis of correlation with the variables weight, height, body mass index, age, waist, waist-to-height-ratio, maximum workload and maximum workload-to-weight-ratio for the entry examination of stage II

### 7.2.2 Regression trees

In a next step regression trees are built for the maximum workload-to-weightratio. For the regression tree the independent variables waist and BMI are removed because of the high correlation to other independent variables. The resulting variables are weight, height, age, and waist-to-height-ratio. Figure 7.5 shows the regression trees. For both males and females the variables waist-to-height-ratio and age are relevant. For females also the variable weight is crucial. To sum it up, the structure of the regression trees varies and the resulting box plots of the leaf vertices are crucially different for both genders.

### 7.2.3 Variable selection

For deriving the regression model a variable selection is done first to find out the best variables. Table 7.1 and Table 7.2 show the best models for different numbers of parameters.


```
\begin{tabular}{lllllllll}
\hline 1 & & & \(*\) & & \(*\) & & & \(*\) \\
2 & & & \(*\) & \(*\) & \(*\) & \(*\) & \(*\) & \\
3 & \(*\) & \(*\) & \(*\) & & \(*\) & & & \\
\hline
\end{tabular}
```

Table 7.1: Summary of the best models with one to four parameters for deriving Model RII for males

In a next step the best model in Table 7.1 and in Table 7.2 has to be chosen. The variables in the best models are different for males and females, hence there

(a) Male

(b) Female

Figure 7.5: Regression trees with the independent variables weight, height, age, body mass index, waist, waist-to-height-ratio and the dependent variable maximum workload-to-weight-ratio for the entry examination of stage II

|  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | no. height:weight weight:age height:WHR age:WHR height:weight: height:weight: weight:age: |  |  |  |  |  |  |
| 1 |  |  |  |  |  |  | * |
| 2 |  |  | * | * |  |  |  |
| 3 | * | * |  | * |  |  |  |
| 4 | * |  |  | * | * | * |  |

Table 7.2: Summary of the best models with one to four parameters for deriving Model RII for females

(a) Graphical description of the error sum of squares for the best models with 1 to 16 variables

(b) Graphical description of the $R_{a d j}^{2}$ for the best models with 1 to 5 variables

(c) Graphical description of the BIC for the best models with 1 to 5 variables

Figure 7.6: Information criteria for deriving Model RII
exist different parameters for both models. This is consistent to the observation that the regression trees have a different structure. Figure 7.6 shows the plots for the error sum of squares, the adjusted coefficient of determination and the BIC.

For the resulting regression models for males 3 parameters are chosen and
for females 4 parameters are chosen:
Model RII for males:
$W \hat{W} R^{0.6}[\mathrm{~W}]=\hat{\beta}_{0}+\hat{\beta}_{1} h e i g h t[\mathrm{~cm}]$ weight $[\mathrm{kg}]+\hat{\beta}_{2}$ weight $[\mathrm{kg}]$ age $[y]+\hat{\beta}_{3}$ age $[y] W H R$ Model RII for females:

$$
\begin{array}{r}
W \hat{W} R^{0.6}[\mathrm{~W}] \begin{array}{c}
=\hat{\beta}_{0}+\hat{\beta}_{1} \text { height }[\mathrm{cm}] \text { weight }[\mathrm{kg}]+\hat{\beta}_{2} \text { age }[y] W H R+ \\
\hat{\beta}_{3} h e i g h t[\mathrm{~cm}] \text { weight }[\mathrm{kg}] \text { age }[y]+\hat{\beta}_{4} h \text { eight }[\mathrm{cm}]: \text { weight }[\mathrm{kg}]: \text { WHR }
\end{array} .
\end{array}
$$

### 7.2.4 Analysis of the model

| WWR ${ }^{0.6} \sim$ height $:$ weight + weight $:$ age + age $:$ WHR |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |
|  | Estimate | Std. Error | $t$ value | $\operatorname{Pr}(>\|t\|)$ |  |
| (Intercept) | $2.428 \mathrm{e}+00$ | 8.497e-02 | 28.578 | $<2 \mathrm{e}-16$ | *** |
| height:weight | -5.521e-05 | 6.803e-06 | -8.116 | 1.02e-14 | *** |
| weight:age | $1.782 \mathrm{e}-04$ | $3.159 \mathrm{e}-05$ | 5.642 | 3.67e-08 | *** |
| age:WHR | -3.594e-02 | $3.979 \mathrm{e}-03$ | -9.032 | $<2 \mathrm{e}-16$ | *** |
| RSE | 0.1697 on 323 degrees of freedom |  |  |  |  |
| $R^{2}$ | 0.4539 |  |  |  |  |
| $R_{\text {adj }}^{2}$ | 0.4489 |  |  |  |  |
| F-statistic | 89.5 on 3 and 323 DF |  |  |  |  |
| p-value: | < 2.2e-16 |  |  |  |  |
| Signif. codes | $0{ }^{\text {****' }} 0.001^{\text {'**' }} 0.01^{\text {'*' }} 0.05^{\prime} . .^{\prime} 0.1^{\prime \prime} 1$ |  |  |  |  |


| WWR ${ }^{0.6} \sim$ height : weight + age $:$ WHR + height : weight : age |
| :---: | :---: | :---: | :---: | :---: | :---: |
| +height : weight $:$ WHR |

Table 7.4: Summary of Model RII for females
Table 7.3 and Table 7.4 show the summaries for the models. The adjusted coefficient of determination is 0.45 for males and 0.58 for females.

### 7.2.5 Diagnostics of the model

The Box-Cox plots in Figure 7.7 show that the already performed transformation of the maximum workload was necessary.


Figure 7.7: Box-Cox plots of Model RII


Figure 7.8: Diagnostic plots of Model RII for males

Figure 7.8 and Figure 7.9 analyze Model RII to check the requirements of the regression model for males and females, respectively.


Figure 7.9: Diagnostic plots of Model RII for females

### 7.3 Normal values for the contribution of the maximum workload in stage II during cardiac outpatient rehabilitation

In this section the contribution of the maximum workload in stage II is analyzed. Therefore just the data of patients which attend both the entry examination and the final examination of stage II are considered. In total there exist 848 patients who did at least one of the ergometries during stage II. 644 patients completed both ergometries. For the following analysis just the patients, who completed both ergometries are relevant.

As a starting point the maximum workload in stage II is presented graphically. Figure 7.10 (a) compares the maximum workload of stage II in the entry examination with the final examination. The red line highlights where both
workloads are equal. All the points above the red line have an improvement, all the points under the red line have a deterioration.

Figure 7.10 (b) shows box plots of the improvement of the maximum workload itself. In this figure the data are additionally separated by gender. For both males and females the boxes are in the positive area. The median of the improvement for males is higher than the median of the improvement for females.

(a) Comparision of the maximum workload from the entry examination with the final examination of stage II

(b) Box plot of the improvement of the maximum workload during stage II split by gender

Figure 7.10: Graphical illustration of the improvement of the maximum workload in stage II of cardiac out-patient rehabilitation

Table 7.5 contains statistical indicators for the improvement. During stage II the mean of the improvement for males is about 17.9 W and for females it is about 11.8 W .

|  | $\min$ | $q_{0.25}$ | $q_{0.5}$ | $\bar{x}$ | $q_{0.75}$ | $\max$ | $s^{2}$ | NA's $^{\prime}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| male | -41 | 10 | 20 | 17.86 | 25 | 72 | 234.24 | 165 |
| female | -19 | 5 | 11 | 11.76 | 19 | 40 | 106.86 | 39 |

Table 7.5: Descriptive statistics of the improvement during stage II: minimum, 1-quartile, median, average, 3-quartile, maximum, standard deviation and the number of missing values

### 7.3.1 Correlation

Figure 7.11 shows the correlation between the independent variables height, age, weight, waist, body mass index, waist-to-height-ratio and the dependent variable improvement. It shows that the correlation between all independent variables and the improvement is quite low for males as well as for females.

In addition to the variables specified above the normal values for the improvement can also be derived from the maximum workload, the maximum


Figure 7.11: Correlation matrix for stage II of cardiac out-patient rehabilitation between the variables height, age, weight, waist, body mass index, waist-to-height-ratio and the improvement
workload-to-weight-ratio and the duration of stage II. The maximum workload and the maximum workload-to-weight-ratio only refer to the entry examination of stage II. Figure 7.12 shows the correlation matrix for these variables and the improvement. It shows that the correlation is very low.


Figure 7.12: Correlation matrix for stage II of cardiac out-patient rehabilitation between the variables maximum workload at entry examination of stage II, maximum workload-to-weight-ratio at entry examination of stage II, duration of stage II and the improvement

### 7.3.2 Regression trees

This section shows regression trees for the improvement in Figure 7.13. The structure of the trees is different for males and females. The box plots in the leaf vertices are quite similar.

### 7.3.3 Regression model

Executing a linear regression with variable selection leads to a regression model with 5 parameters for males and 4 parameters for females. Both models have very low adjusted coefficients of determination: under 0.15 and about 0.1. For this reason the regression model is not shown in this chapter.

### 7.4 Normal values for the maximum workload of the entry examination of stage III during cardiac outpatient rehabilitation

In this section a linear regression is done for deriving normal values for the maximum workload of the entry examination of stage II during cardiac outpatient rehabilitation. First the relevant variables are identified by a correlation analysis. Afterwards to illustrate the main variables a regression tree is built. Finally this section includes a regression model for deriving the normal values. Therefore also a variable selection is done. The resulting model is notated by Model RIII (rehabilitation stage III).

For deriving normal values the waist circumference is a crucial variable. Unfortunately, not for all data during rehabilitation the waist circumference is available. For this reason just the data which include values for the waist circumference are included. This constraint reduces the data from 674 to 340 ergometries.

### 7.4.1 Correlation

Figure 7.14 shows the correlation between all variables for males and females. In both correlation matrices the maximum workload-to-weight-ratio has a higher correlation to the other variables than the maximum workload. For this reason the normal values refer to the maximum workload-to-weight-ratio. Note that also further independent variables were considered in the beginning. The first group of variables are the variables which are measured at the beginning of the ergometry, i.e. resting heart rate, resting systolic blood pressure and resting diastolic blood pressure. The second group were the results of the laboratory, i.e. cholesterol, low-density lipoprotein, high-density lipoprotein, triglyceride, creatinine, fasting blood sugar level and uric acid. Due to the complexity in practice and the low correlation to the maximum workload-to-weight-ratio this variables are not used for the regression. The remaining independent variables weight, height, age, waist and waist-to-height-ratio form the pool of variables for the regression.

(a) Males

(b) Females

Figure 7.13: Regression trees for the improvement of stage II with the independent variables weight, height, age, waist-to-height-ratio and the dependent variable maximum workload-to-weight-ratio


Figure 7.14: Analysis of correlation with the variables weight, height, body mass index, age, waist, waist-to-height-ratio, maximum workload and maximum workload-to-weight-ratio for the entry examination of stage III

### 7.4.2 Regression trees

In a next step regression trees are built for the maximum workload-to-weightratio. For the regression tree the independent variables waist and BMI are removed because of the high correlation to other independent variables. The resulting variables are weight, height, age, and waist-to-height-ratio. Figure 7.15 shows the received the regression trees. For both males and females the variables waist-to-height-ratio and age are relevant. For females also the variable weight is crucial. To sum it up, the structure of the regression trees varies and the resulting box plots of the leaf vertices are crucially different for both genders.

### 7.4.3 Variable selection

For deriving the regression model a variable selection is done first to find out the best variables. Table 7.6 and Table 7.7 show the best models for different numbers of parameters.


Table 7.6: Summary of the best models with 1 to 5 parameters for deriving Model RIII for males

(a) Male

(b) Female

Figure 7.15: Regression trees with the independent variables weight, height, age, body mass index, waist, waist-to-height-ratio and the dependent variable maximum workload-to-weight-ratio for the entry examination of stage III


Table 7.7: Summary of the best models with 1 to 5 parameters for deriving Model RIII for females

(a) Graphical description of the error sum of squares for the best models with one to 16 variables

(b) Graphical description of the $R_{a d j}^{2}$ for the best models with one to 5 variables

(c) Graphical description of the BIC for the best models with one to 5 variables

Figure 7.16: Information criteria for deriving Model RIII

In a next step the best of the models in Table 7.6 and in Table 7.7 has to be chosen. Unfortunately the variables in the best models are different for males and females. This is consistent to the observation that the regression trees have
a different structure. Figure 7.16 shows the plots for the error sum of squares, the adjusted coefficient of determination and the Bayesian information criterion.

Using the BIC for men 3 parameters and for women 2 parameters are chosen. male:

$$
\begin{aligned}
W \hat{W} R^{0.5}[W]=\hat{\beta}_{0}+ & \hat{\beta}_{1} \text { weight }: \text { age }+\hat{\beta}_{2} \text { height }: \text { age }: \text { WHR } \\
& +\hat{\beta}_{3} \text { height }: \text { weight }: \text { age }: \text { WHR }
\end{aligned}
$$

female:

$$
W \hat{W} R^{0.5}[W]=\hat{\beta}_{0}+\hat{\beta}_{1} \text { age }+\hat{\beta}_{2} W H R
$$

### 7.4.4 Analysis of the model

Table 7.8 and Table 7.9 summarize both models.

| WWR ${ }^{0.6} \sim$ weight : age + age : height : WHR + weight : age : height WHR |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |
|  | Estimate | Std. Error | t value | $\operatorname{Pr}(>\|t\|)$ |  |
| (Intercept) | $1.597 \mathrm{e}+00$ | 6.005e-02 | 26.601 | $<2 \mathrm{e}-16$ | *** |
| weight:age | $2.131 \mathrm{e}-04$ | $4.598 \mathrm{e}-05$ | 4.636 | 5.73e-06 | *** |
| age:height:WHR | -1.197e-04 | $1.964 \mathrm{e}-05$ | -6.094 | 4.15e-09 | *** |
| weight:age:height:WHR | -1.283e-06 | $2.292 \mathrm{e}-07$ | -5.599 | $5.66 \mathrm{e}-08$ | *** |
| Residual standard error | 0.1653 on 250degrees of freedom |  |  |  |  |
| $R^{2}$ | 0.3817 |  |  |  |  |
| $R_{\text {adj }}^{2}$ | 0.3743 |  |  |  |  |
| F-statistic | 51.45 on 3 and 250 DF |  |  |  |  |
| p-value: | <2.2e-16 |  |  |  |  |
| Signif. codes | $0^{\text {****' } 0.001 ~}{ }^{\text {*** }} 0.01^{\text {'*' }} 0.05^{\prime \prime} .^{\prime} 0.1^{\prime \prime} 1$ |  |  |  |  |

Table 7.8: Summary of Model RIII for males

| WWR ${ }^{0.6} \sim$ age + WHR |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Coefficients: |  |  |  |  |  |
|  | Estimate | Std. Error | t value | $\operatorname{Pr}(>\|t\|)$ |  |
| (Intercept) | 2.227838 | 0.169508 | 13.143 | $<2 \mathrm{e}-16$ | *** |
| age | -0.005608 | 0.001355 | -4.138 | 8.36e-05 | *** |
| WHR | -1.273880 | 0.274596 | -4.639 | $1.29 \mathrm{e}-05$ | *** |
| Residual standard error | 0.1708 on 83 degrees of freedom |  |  |  |  |
| $R^{2}$ | 0.3375 |  |  |  |  |
| $R_{\text {adj }}^{2}$ | 0.3215 |  |  |  |  |
| F-statistic | 21.14 on 2 and 83 DF |  |  |  |  |
| p-value: | $3.805 \mathrm{e}-08$ |  |  |  |  |
| Signif. codes | $0^{\text {****' } 0.001 ~}{ }^{\text {***' }} 0.01^{\text {** }} 0.05^{\prime \prime} .^{\prime} 0.1^{\prime \prime} 1$ |  |  |  |  |

Table 7.9: Summary of Model RIII for females

### 7.4.5 Diagnostics of the model

The Box-Cox plots in Figure 7.17 show that the already performed transformation of the maximum workload was necessary.


Figure 7.17: Box-Cox plots of Model RIII


Figure 7.18: Diagnostic plots of Model RIII for males

Figure 7.18 and Figure 7.19 analyze Model RIII to check the requirements of the regression model for men and women, respectively.


Figure 7.19: Diagnostic plots of Model RIII for females

### 7.5 Normal values for the contribution of the maximum workload in stage III during cardiac outpatient rehabilitation

In this section the contribution of the maximum workload in stage III is analyzed. Therefore just the data of patients which attend both the entry examination and the final examination of stage III are considered. In total there exist 1476 patients who did at least one of the ergometries during stage III. 787 patients completed entry examination and the final examination. Note that for the missing entry examinations of stage III, the final examinations of stage II are used, which are missing in Figure 7.1.

As a starting point the maximum workload in stage III is presented graphically. Figure 7.20(a) compares the maximum workload of stage III in the entry
examination with the final examination. The red line highlights where both workloads are equal. All the points above the red line have an improvement, all the points under the red line have a deterioration.

Figure 7.20 (b) shows box plots of the improvement of the maximum workload itself. In this figure the data are additionally separated by gender. For both males and females the boxes are in the positive area. The median of the improvement for males is higher than the median of the improvement for females.


Figure 7.20: Graphical illustration of the improvement of the maximum workload in stage III of cardiac out-patient rehabilitation

Table 7.10 contains statistical indicators for the improvement. During stage III the mean of the improvement for males is about 14.2 W and for females it is about 9.7 W .

|  | $\min$ | $q_{0.25}$ | $q_{0.5}$ | $\bar{x}$ | $q_{0.75}$ | $\max$ | $s^{2}$ | NA's $^{\prime}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| male | -80 | 0 | 12 | 14.22 | 30 | 80 | 388.75 | 508 |
| female | -60 | 0 | 10 | 9.65 | 20 | 60 | 234.27 | 143 |

Table 7.10: Descriptive statistics of the improvement during stage III: minimum, 1-quartile, median, average, 3-quartile, maximum, standard deviation and the number of missing values

### 7.5.1 Correlation

Figure 7.21 shows the correlation between the independent variables height, age, weight, waist, body mass index, waist-to-height-ratio and the dependent variable improvement. It shows that the correlation between all independent variables and the improvement is quite low for males as well as for females.

(a) Male

(b) Female

Figure 7.21: Correlation matrix for stage III of cardiac out-patient rehabilitation between the variables height, age, weight, waist, body mass index, waist-to-height-ratio and the improvement

For deriving normal values for the improvement the maximum workload and the maximum workload-to-weight-ratio, respectively, during the entry examination and the duration of stage III can be used. Figure 7.22 shows the correlation matrix for these variables and the improvement. It shows that the correlation is very low.


Figure 7.22: Correlation matrix for stage III of cardiac out-patient rehabilitation between the variables maximum workload at entry examination of stage III, maximum workload-to-weight-ratio at entry examination of stage II, duration of stage III and the improvement

### 7.5.2 Regression trees

This section shows regression trees for the improvement in Figure 7.23. The structure of the trees is different for males and females. The box plots in the leaf vertices are quite similar.


Figure 7.23: Regression trees for the improvement of stage III with the independent variables weight, height, age, waist-to-height-ratio and the dependent variable maximum workload-to-weight-ratio

### 7.5.3 Regression model

As for the normal values of the improvement of stage II the result of a linear regression has a very low adjusted coefficient of determination. For this reason the regression model is not shown in this chapter.

### 7.6 Discussion

At the moment, to my knowledge, there exist no normal values of the maximum workload in ergometries specific to the stages of rehabilitation. The same normal values are used for interpretation of ergometries from healthy people as well as people in rehabilitation. Nevertheless, these normal values should be adjusted to get rehabilitation specific normal values. In this chapter, normal values for the maximum workload for the entry examination stage II as well as for stage III are derived. The newly derived normal values have an adjusted coefficient of determination of 0.45 for males and 0.58 for females in stage II and 0.37 for males and 0.42 for females in stage III. Note, that the output of the regression models is the maximum workload-to-weight-ratio, which has to be multiplied with the weight to gain the maximum workload.

Furthermore, the improvement in the maximum workload during stage II and stage III is analyzed. For the improvement, the mean is calculated and also regression trees are created. Due to the low correlation between the independent variables and the maximum workload-to-weight-ratio, a regression analysis is not done.

A planned further research question is to find the optimal duration of stage III during cardiac out-patient rehabilitation. Due to only small changes in the duration of stage III and slight differences in the results, it was not possible to answer this by the underlying data.

## Chapter 8

## Conclusion and outlook for further research

### 8.1 Summary

In Austria, currently used reference values for the maximum workload reached during an ergometry are based on a model from 1972. ZARG uses the same values for the evaluation of ergometries performed at their center, but they doubt that the presently used reference values fit well.

For that reason, the evaluation of the currently used Model P with data from 28,625 ergometries against newly developed models was done to calculate the normal values of maximum workload. The analysis showed that the adjusted coefficient of determination for females in Model P is 0.23 as compared to 0.41 in Model 1, but there was not as much improvement seen in the adjusted coefficient of determination for males ( 0.35 vs 0.37 ). Therefore, it could be concluded that Model P does not fit well to calculate the normal values of maximum workload in females. This could be due to a different population used to calculate Model P. Furthermore, the use of the predicted variable maximum workload-to-weight-ratio and its box cox transformation leads to the development of another model (Model 3) which has an adjusted coefficient of determination of 0.39 for males and 0.49 for females, respectively. Hence, use of the variable maximum workload-to-weight-ratio instead of maximum workload leads to a better model. The use of the predicted variable maximum workload-to-weight-ratio and independent variables height and weight instead of the conventional variable body surface area resulted into Model 4. This model has an improved adjusted coefficient of determination of 0.48 for males and of 0.57 for females. Therefore, higher values of the adjusted coefficient of determination from Model 4 suggest this model is more precise in calculating the normal values of the maximum workload. Finally, development of a gender independent model using the history of medication as an independent dummy variable along with the previously used variable in Model 4 resulted in an adjusted coefficient of determination of 0.55 . Therefore, we may conclude that the use of Model D eliminates the need for using gender specific models without compromising the value of the adjusted coefficient of determination.

In the current scenario, there is only one set of normal values used to interpret the maximum workload in ergometries irrespective of the cardiac fitness of
that individual. Even if the person is recovering from a heart attack or is entirely fit, the normal values of the maximum workload are the same. Therefore, the new normal values for the entry examination of stage II as well as for stage III of cardiac rehabilitation were calculated using the ergometry data of the people in cardiac rehabilitation. The newly derived normal values have an adjusted coefficient of determination of 0.45 for males and 0.58 for females in stage II, and of 0.37 for males and 0.42 for females in stage III. Henceforth, these cardiac rehabilitation stage-specific normal values could be used for the evaluation of ergometries during cardiac rehabilitation. Finally, the average improvement in the maximum workload during stage II of cardiac rehabilitation was 17.86 W in males and 11.76 W in females, whereas for stage III, the average improvement was 14.22 W for males and 9.65 W for females. Hence, these values could be used as the normal values to evaluate the improvement of a person in cardiac rehabilitation in the respective stages.

### 8.2 Limitation and Recommendations

The results of this thesis show that the waist circumference is a crucial parameter for deriving normal values of the maximum workload. However, in the cohort of 28,625 ergometries it was measured only during 3,800 ergometries. Therefore, it is suggested that for each ergometry the waist circumference should be measured. With more data of the waist circumference, the model would also contain information about the waist, to include the WHR in the model which should lead to an even better fit.

Because of non uniformity in the written diagnosis of the heart diseases in this cohort, the variable ,diagnosis' was not precisely measured to be useful for the regression. Therefore, adaptation of the international statistical classification of diseases (ICD) codes for disease diagnosis will help to have more precise information for regression to calculate the normal values.

### 8.3 Further research questions

- Does statin therapy influence the maximum workload in cardiac exercise stress testing?
- What are the benefits of an out-patient cardiac rehabilitation over an inpatient cardiac rehabilitation?
- What can be concluded from a curve of the heart rate during a maximal cardiac exercise stress testing?

The analysis to answer the questions above could not be conducted due to the time constraint and unavailable data of in-patient cardiac rehabilitation.

To sum up the added value of this thesis, new improved normal values of the maximal workload for ergometries as well as specific normal values for outpatient rehabilitation can be directly applied in practice.

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## Appendices

## Appendix A

## XSL stylesheet for converting the XML files in a CSV file

```
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    <xsl:output method="text" />
    <xsl:template match="/">
    <xsl:choose>
        <xsl:when test="/CardiologyXML/PatientInfo/PID_!=_''">
            <xsl:value-of select="/CardiologyXML/PatientInfo/PID"/>
        </xsl:when>
        <xsl:otherwise>
            <xsl:text>0</ xsl:text>
        </xsl:otherwise>
    </xsl:choose>
    <xsl:text> </xsl:text>
    <xsl:value-of select="/CardiologyXML/ObservationDateTime/Year" />
    <xsl:text>-</xsl:text>
    <xsl:value-of select="/CardiologyXML/ObservationDateTime/Month"/>
    <xsl:text>-</xsl:text>
    <xsl:value-of select="/CardiologyXML/ObservationDateTime/Day"/>
    <xsl:text> </xsl:text>
    <xsl:value-of select="/CardiologyXML/ObservationDateTime/Hour" />
    <xsl:text>:</xsl:text>
    <xsl:value-of select="/CardiologyXML/ObservationDateTime/Minute" />
    <xsl:text>:</xsl:text>
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    <xsl:value-of select="/CardiologyXML/ObservationEndDateTime/Month"/
        >
    <xsl:text>-</xsl:text>
    <xsl:value-of select="/CardiologyXML/ObservationEndDateTime/Day" />
    <xsl:text> </xsl:text>
    <xsl:value-of select="/CardiologyXML/ObservationEndDateTime/Hour" />
    <xsl:text>:</xsl:text>
    <xsl:value-of select="/CardiologyXML/ObservationEndDateTime/Minute"
        />
    <xsl:text>:</xsl:text>
    <xsl:value-of select="/CardiologyXML/ObservationEndDateTime/Second"
        />
```

```
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    <xsl:choose>
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            <xsl:value-of select=" /CardiologyXML/PatientInfo/Age" />
        </xsl:when>
        <xsl:otherwise>
        <xsl:text>-1</xsl:text>
        </xsl:otherwise>
    </xsl:choose>
    <xsl:text> </xsl:text>
    <xsl:value-of select="/CardiologyXML/PatientInfo/Gender"/>
    <xsl:text> </xsl:text>
    <xsl:choose>
    <xsl:when test="/CardiologyXML/PatientInfo/Height_!=_ ''">
            <xsl:value-of select="/CardiologyXML/PatientInfo/Height"/>
        </xsl:when>
        <xsl:otherwise>
        <xsl:text>-1</xsl:text>
    </xsl:otherwise>
    </xsl:choose>
    <xsl:text> </xsl:text>
    <xsl:choose>
        <xsl:when test="/CardiologyXML/PatientInfo/Weight_!= ''">
        <xsl:value-of select="/CardiologyXML/PatientInfo/Weight"/>
    </xsl:when>
    <xsl:otherwise>
        <xsl:text>-1</xsl:text>
        </xsl:otherwise>
    </xsl:choose>
    <xsl:text> </xsl:text>
    <xsl:value-of select="/CardiologyXML/Interpretation/
    CustomSummaryStatement" />
    <xsl:text> </xsl:text>
    <xsl:value-of select="/CardiologyXML/PatientInfo/PaceMaker"/>
    <xsl:text> </xsl:text>
    <xsl:value-of select="/CardiologyXML/Protocol/Device"/>
    <xsl:text> </xsl:text>
    <xsl:value-of select=" / CardiologyXML/ExerciseMeasurements/
    MaxWorkload" />
    <xsl:text> </xsl:text>
    <xsl:choose>
        <xsl:when test="/CardiologyXML/TrendData/TrendEntry[PhaseName='
            VORBEL. '_and_Systolic BP ][1]/ SystolicBP_!!= '' ">
            <xsl:value-of select=" / CardiologyXML/TrendData/TrendEntry[
            PhaseName= 'VORBEL. '_and_SystolicBP ][1]/ SystolicBP " />
        </xsl:when>
        <xsl:otherwise>
            <xsl:text>-1</ xsl:text>
        </xsl:otherwise>
    </xsl:choose>
<xsl:text> </xsl:text>
    <xsl:choose>
        <xsl:when test="/CardiologyXML/TrendData/TrendEntry[PhaseName='
            VORBEL. '_and_DiastolicBP][1]/ Diastolic BP每!= ''">
            <xsl:value-of select=" / CardiologyXML/TrendData/TrendEntry[
            PhaseName= 'VORBEL. '_and_DiastolicBP ][1]/ Diastolic BP "/>
        </xsl:when>
        <xsl:otherwise>
```

```
                <xsl:text>-1</xsl:text>
        </xsl:otherwise>
    </xsl:choose>
    <xsl:text> </xsl:text>
    <xsl:choose>
        <xsl:when test="/CardiologyXML/ExerciseMeasurements/
```



```
            <xsl:value-of select="/CardiologyXML/ExerciseMeasurements/
                MaxSystolicBP" />
        </xsl:when>
        <xsl:otherwise>
            <xsl:text>-1</xsl:text>
        </xsl:otherwise>
    </xsl:choose>
    <xsl:text> </xsl:text>
    <xsl:choose>
        <xsl:when test="/CardiologyXML/ExerciseMeasurements/
            MaxDiastolicBP_!=_''">
            <xsl:value-of select="/CardiologyXML/ExerciseMeasurements/
                MaxDiastolicBP " />
            </xsl:when>
            <xsl:otherwise>
            <xsl:text>-1</xsl:text>
            </xsl:otherwise>
    </xsl:choose>
    <xsl:text> </xsl:text>
    <xsl:choose>
        <xsl:when test="/CardiologyXML/ExerciseMeasurements/
            RestingStats/RestHR_!= ' ' ">
            <xsl:value-of select="/CardiologyXML/ExerciseMeasurements/
                RestingStats/RestHR" />
            </xsl:when>
            <xsl:otherwise>
            <xsl:text>-1</xsl:text>
            </xsl:otherwise>
    </xsl:choose>
    <xsl:text> </xsl:text>
    <xsl:choose>
        <xsl:when test="/CardiologyXML/ExerciseMeasurements/
            MaxHeartRate!= ' ' '">
            <xsl:value-of select="/CardiologyXML/ExerciseMeasurements/
                MaxHeartRate"/>
            </xsl:when>
            <xsl:otherwise>
            <xsl:text>-1</xsl:text>
            </xsl:otherwise>
    </xsl:choose>
    <xsl:text> </xsl:text>
    <xsl:value-of select="/CardiologyXML/Interpretation/
            ReasonForTermination "/>
    <xsl:text> </xsl:text>
    <xsl:value-of select="/CardiologyXML/ClinicalInfo/ReasonForStudy" />
    <xsl:text>
    </xsl:text>
</xsl:template>
</xsl:stylesheet>
```


## Appendix B

## MySQL script for integrating the CSV files in a MySQL data base

```
use ergometry;
drop table if exists timeseries;
drop table if exists maindata;
drop table if exists diagnosis;
drop table if exists medication;
drop table if exists lab;
SET SQL_SAFE_UPDATES = 0;
SET default_storage_engine=InnoDB;
CREATE TABLE maindata (
    patient_id int not null auto_increment,
    start_time datetime not null default current_timestamp,
    end_time datetime,
    age int(11) null,
    gender text,
    height int(11) null,
    weight int(11) null,
    waist int(11) null,
    pacemaker text null,
    device text null,
    workload_max decimal null,
    systolicbp_rest int(11) null,
    diastolicbp_rest int(11) null,
    systolicbp_max int(11) null,
    diastolicbp_max int(11) null,
    hr_rest int(11) null,
    hr_max int(11) null,
    termination_reason text,
    reason_for_study text,
    special_workload text,
    primary key (patient_id, start_time))
    ENGINE=InnoDB;
CREATE TABLE timeseries (
    patient_id int not null,
    start_time datetime not null default current_timestamp,
    entry_id int not null,
    start_entry time null,
```

```
    workload decimal null,
    diastolicbp int(11) null,
    systolicbp int(11) null,
    hr int(11) null,
    cadence int(11) null,
    primary key (patient_id, start_time, entry_id))
    ENGINE=InnoDB;
-- add the foreign key constraint:
ALTER TABLE timeseries
    ADD CONSTRAINT fk_timeseries_maindata
            foreign key (patient_id, start_time)
            references maindata (patient_id, start_time)
            ON DELETE CASCADE;
-- deleting foreign key constraint
-- alter table timeseries drop foreign key fk_timeseries_maindata;
CREATE TABLE diagnosis (
    patient_id int not null,
    entry_id int not null,
    diagnosis_date date not null,
    diagnosis text,
    primary key (patient_id, entry_id))
    ENGINE=InnoDB;
CREATE TABLE medication (
    patient_id int not null,
    entry_id int not null,
    medication_date date null,
    medication text,
    dosis text,
    medication_id int(11) null,
    primary key (patient_id, entry_id))
    ENGINE=InnoDB;
CREATE TABLE lab (
    patient_id int not null,
    entry_id int not null,
    lab_date date not null,
    parameter text,
    lab_value numeric (6,2) null,
    evaluation text null,
    primary key (patient_id, entry_id))
    ENGINE=InnoDB;
-- add data to maindata:
load data infile '/var/lib/mysql/maindata.csv' into table maindata
    CHARACTER SET UTF8 fields terminated by '\t';
-- add data to timeseries:
load data infile '/var/lib/mysql/timeseries.csv' into table timeseries
    fields terminated by '\t';
-- add data to diagnosis:
load data infile '/var/lib/mysql/diagnosis.csv' into table diagnosis
    fields terminated by '\t';
```

- add data to medication:
load data infile '/var/lib/mysql/medication.csv' into table medication fields terminated by '\t';
- add data to lab:
load data infile '/var/lib/mysql/lab.csv' into table lab fields terminated by '\t';
- test which data sets are in the timeseries but not in the maindata - select * from timeseries left join maindata on maindata.patient_id= timeseries.patient_id and maindata.start_time=timeseries.start_time where maindata.patient_id is NULL;
- setting empty cells (-1) to NULL

UPDATE maindata SET patient_id = patient_id, start_time = start_time, age $=$ NULL WHERE maindata.age $=-1$;
UPDATE maindata SET patient_id = patient_id, start_time = start_time, height $=$ NULL WHERE maindata. height $=-1$;
UPDATE maindata SET patient_id = patient_id, start_time = start_time, weight $=$ NULL WHERE maindata. weight $=-1$;
UPDATE maindata SET patient_id = patient_id, start_time = start_time, workload_max= NULL WHERE maindata. workload_max =-1;
UPDATE maindata SET patient_id = patient_id, start_time = start_time, workload_max= NULL WHERE maindata. workload_max $=0$;
UPDATE maindata SET patient_id = patient_id, start_time = start_time, systolicbp_rest= NULL WHERE maindata.systolicbp_rest=-1;
UPDATE maindata SET patient_id = patient_id, start_time = start_time, diastolicbp_rest $=$ NULL WHERE maindata. diastolicbp_rest $=-1$;
UPDATE maindata SET patient_id = patient_id, start_time = start_time, systolicbp_max $=$ NULL WHERE maindata.systolicbp_max $=-1$;
UPDATE maindata SET patient_id = patient_id, start_time = start_time , diastolicbp_max $=$ NULL WHERE maindata.diastolicbp_max $=-1$;
UPDATE maindata SET patient_id = patient_id, start_time = start_time, hr_rest $=$ NULL WHERE maindata. hr_rest $=-1$;
UPDATE maindata SET patient_id = patient_id, start_time = start_time, hr_max $=$ NULL WHERE maindata. $\mathrm{hr} \_\max =-1$;
UPDATE maindata SET patient_id = patient_id, start_time = start_time, waist $=$ NULL WHERE maindata. waist $=-1$;

UPDATE timeseries SET patient_id = patient_id, start_time = start_time, workload= NULL WHERE timeseries. workload $=-1$;
UPDATE timeseries SET patient_id = patient_id, start_time = start_time, systolicbp $=$ NULL WHERE timeseries. systolicbp $=-1$;
UPDATE timeseries SET patient_id = patient_id, start_time = start_time, diastolicbp $=$ NULL WHERE timeseries.diastolicbp $=-1$;
UPDATE timeseries SET patient_id = patient_id, start_time = start_time, $\mathrm{hr}=$ NULL WHERE timeseries.hr $=-1$;
UPDATE timeseries SET patient_id = patient_id, start_time = start_time, cadence $=$ NULL WHERE timeseries.cadence $=-1$;

- deleting data sets
delete from maindata where device = 'Treadmill';
delete from maindata where workload_max is NULL;
delete from maindata where patient_id=3276; -- test ID
delete from maindata where workload_max $<=20$;
delete from maindata where termination_reason LIKE '';

```
delete from maindata where termination_reason='Kreislaufkollaps';
-- changing decimal to int (ergometer does not have decimal values)
ALTER TABLE maindata CHANGE workload_max workload_max INT(11) null;
ALTER TABLE timeseries CHANGE workload workload INT(11) null;
-- deleting the entries of the other tables whichs dates after after
    the last ergometry
delete from lab where lab_date > '2017-07-01';
delete from medication where medication_date > '2017-07-01';
delete from diagnosis where diagnosis_date > '2017-07-01';
    adding lab
alter table maindata add CHOL int;
alter table maindata add e_CHOL Text;
alter table maindata add CREA decimal (7,2);
alter table maindata add e_CREA Text;
alter table maindata add HDL int;
alter table maindata add e_HDL Text;
alter table maindata add HSRE decimal (7,2);
alter table maindata add e_HSRE Text;
alter table maindata add LDL decimal (7,2);
alter table maindata add e_LDL Text;
alter table maindata add NBZ int;
alter table maindata add e_NBZ Text;
alter table maindata add TRIGL int;
alter table maindata add e_TRIGL Text;
```


## Appendix C

## Java program to integrate the diagnosis in Table maindata

```
import java.sql.Connection;
import java.sql.Date;
import java.sql.DriverManager;
import java.sql.PreparedStatement;
import java.sql.ResultSet;
import java.sql.SQLException;
import java.sql.Statement;
import java.sql.Timestamp;
import java.util.ArrayList;
import java.util.HashMap;
import java.util.TreeMap;
import java.util.regex.Pattern;
import java.util.regex.Matcher;
// Program RefactorDiagnosisDB.java
// The colums "infarkt", "khk" and "kardio" will be appended in table
    "maindata".
// For each ergometry in table "maindata" the table "diagnosis" will be
        scanned for the strings "infarkt", "khk" oder "kardio" with the
    same patient_id as in table "maindata".
// In case of a hit, the particular columne will be marked
public class RefactorDiagnosisDB
{
    Connection db;
    boolean test = false;
    private ArrayList<HashMap<String, Object>> maindata;
    private ArrayList<HashMap<String, Object>> medication;
    private ArrayList<HashMap<String, Object>> diagnosis;
    public RefactorDiagnosisDB() throws SQLException
    {
        try {
            // The newInstance() call is a work around for some broken
                    Java implementations
                    Class.forName("com.mysql.jdbc.Driver").newInstance();
            }
            catch (Exception ex)
```

```
    {
        // handle the error
        }
    String username = "sqluser";
    String password = "sqluser";
    db = DriverManager.getConnection(
        "jdbc:mysql:/ /localhost:3306/ ergometry?autoReconnect=true&
        useSSL=false ",
    username, password);
    maindata = loadAllRows("maindata");
    medication = loadAllRows("medication");
    diagnosis = loadAllRows("diagnosis");
} // end constructor
ArrayList<HashMap<String, Object>> loadAllRows(String table) throws
    SQLException
{
    PreparedStatement ps = db.prepareStatement("SELECT ***FROM
        );
    ResultSet rs = ps.executeQuery();
    java.sql.ResultSetMetaData md = rs.getMetaData();
    int columns = md.getColumnCount();
    ArrayList<HashMap<String, Object>> ret = new ArrayList<>();
    while (rs.next())
    {
        HashMap<String, Object> row = new HashMap();
        ret.add(row);
        for (int i = 1; i <= columns; i++)
            row.put(md.getColumnName(i), rs.getObject(i));
            }
    }
    return ret;
} // end ArrayList
public void runMethod() throws SQLException
{
    String[] diagnostic = new String[53] ;
    diagnostic[0] = "aorta";
    diagnostic[1] = "aorten";
    diagnostic[2] = "aorto";
    diagnostic[3] = "arrhythmie";
    diagnostic[4] = "asystolie";
    diagnostic[5] = "av-block";
    diagnostic[6] = "blutdruckentgleisung";
    diagnostic[7] = "bradykardie";
    diagnostic[8] = "cabg";
    diagnostic[9] = "cardial";
    diagnostic[10] = "cardio";
    diagnostic[11] = "cordis";
    diagnostic[12] = "coronar";
    diagnostic[13] = "diastolisch";
```

```
diagnostic[14] = "endopericardiale";
diagnostic[15] = "erregungsleitungsstörung";
diagnostic[16] = "extrasystol";
diagnostic[17] = "flimmer";
diagnostic[18] = "herz";
diagnostic[19] = "hhk";
diagnostic[20] = "hinterwand";
diagnostic[21] = "hypertonus";
diagnostic[22] = "hypertropie";
diagnostic[23] = "insuffienz";
diagnostic[24] = "kardiovasculär";
diagnostic[25] = "khk";
diagnostic[26] = "klappe";
diagnostic[27] = "koronar";
diagnostic[28] = "ldh";
diagnostic[29] = "linksschenkelblock";
diagnostic[30] = "mins";
diagnostic[31] = "mitral";
diagnostic[32] = "myocardiopathie";
diagnostic[33] = "nstemi";
diagnostic[34] = "pericard";
diagnostic[35] = "pfo";
diagnostic[36] = "ptca";
diagnostic[37] = "rca";
diagnostic[38] = "rhythmopathia";
diagnostic[39] = "rv-reiz";
diagnostic[40] = "sa-block";
diagnostic[41] = "schenkelblock";
diagnostic[42] = "schrittmacher";
diagnostic[43] = "stenose";
diagnostic[44] = "stent";
diagnostic[45] = "sves";
diagnostic[46] = "svt";
diagnostic[47] = "synkope";
diagnostic[48] = "tachycardie";
diagnostic[49] = "vetrik";
diagnostic[50] = "ves";
diagnostic[51] = "vorhof";
diagnostic[52] = "zavk";
if(!maindata.iterator().next().containsKey("kardio"))
{
    Statement stmt = db.createStatement();
    stmt.execute("ALTER_TABLE_maindata_ADD_COLUMN_kardio_INT(1)" );
}
TreeMap<Integer, ArrayList<HashMap<String, Object >>>
    idxPIDDiagnosis;
idxPIDDiagnosis = new TreeMap <>();
for(HashMap<String, Object> row : diagnosis)
{
    Integer patient_id = (Integer) row.get("patient_id");
    ArrayList<HashMap<String, Object >> list = idxPIDDiagnosis.get(
        patient_id);
    if(list == null)
    {
        list = new ArrayList<>();
```

```
            idxPIDDiagnosis.put(patient_id, list);
    }
    list.add(row);
}
PreparedStatement cardio = db.prepareStatement("UPDATE_maindata_SET
    & kardio
int cardioCount = 0, no_diag_count = 0;
if (test) System.out.println("");
for(HashMap<String, Object> mainrow : maindata)
{
    Integer patient_id = (Integer) mainrow.get("patient_id");
    Timestamp start_time = (Timestamp) mainrow.get("start_time");
    ArrayList<HashMap<String, Object>> diaglist = idxPIDDiagnosis.get
            (patient_id);
    if(diaglist == null)
    {
```



```
                , patient_id));
            no_diag_count++;
    }
    else for(HashMap<String, Object> diagnosis : diaglist)
    {
        Date diagnosis_date = (Date) diagnosis.get("diagnosis_date");
        String diags = (String) diagnosis.get("diagnosis");
        if(diagnosis_date == null || diags == null) continue;
        if (test)
        {
```



```
            System.out.println("„diagnosis
            System.out.println("„diagnosis-date=" + diagnosis_date);
            System.out.println("SStart_time_涽=" + start_time);
            }
        if( diagnosis_date.before(start_time))
        {
        if( diags.toLowerCase().contains(diagnostic[0].toLowerCase())
            ||
            diags.toLowerCase(). contains(diagnostic[1].toLowerCase())
                    ||
            diags.toLowerCase().contains(diagnostic[2].toLowerCase ())
                    | |
            diags.toLowerCase().contains(diagnostic[3].toLowerCase())
                    ||
            diags.toLowerCase().contains(diagnostic[4].toLowerCase())
                    | |
            diags.toLowerCase().contains(diagnostic [5].toLowerCase())
                    ||
            diags.toLowerCase(). contains(diagnostic[6].toLowerCase ())
                    ||
            diags.toLowerCase(). contains(diagnostic [7].toLowerCase ())
                    | |
```

diags.toLowerCase (). contains (diagnostic [8]. toLowerCase ()) |।
diags.toLowerCase (). contains (diagnostic [9].toLowerCase ()) | $\mid$
diags.toLowerCase (). contains (diagnostic[10].toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic[11]. toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic[12].toLowerCase () ) ।।
diags.toLowerCase (). contains (diagnostic [13].toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic [14]. toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic [15].toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic[16].toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic [17].toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic[18]. toLowerCase () ) । \|
diags.toLowerCase (). contains (diagnostic [19]. toLowerCase () ) II
diags.toLowerCase (). contains (diagnostic [20]. toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic[21]. toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic[22]. toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic[23].toLowerCase () ) |l
diags.toLowerCase (). contains (diagnostic [24]. toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic[25].toLowerCase () ) ।।
diags.toLowerCase (). contains (diagnostic[26].toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic[27]. toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic[28].toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic[29]. toLowerCase () ) | \|
diags.toLowerCase (). contains (diagnostic[30]. toLowerCase () ) ।l
diags.toLowerCase (). contains (diagnostic[31].toLowerCase () ) |l
diags.toLowerCase (). contains (diagnostic[32]. toLowerCase () ) 1 I
diags.toLowerCase (). contains (diagnostic[33]. toLowerCase () ) । I
diags.toLowerCase (). contains (diagnostic [34]. toLowerCase () ) |l
diags.toLowerCase (). contains (diagnostic [35]. toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic[36].toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic [37].toLowerCase () ) II
diags.toLowerCase (). contains (diagnostic [38].toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic [39].toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic [40].toLowerCase () ) II
diags.toLowerCase (). contains (diagnostic [41]. toLowerCase () ) I।
diags.toLowerCase (). contains (diagnostic [42].toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic [43].toLowerCase () ) II
diags.toLowerCase (). contains (diagnostic[44].toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic [45].toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic [46].toLowerCase () ) II
diags.toLowerCase (). contains (diagnostic [47]. toLowerCase () ) I।
diags.toLowerCase (). contains (diagnostic [48].toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic [49].toLowerCase () ) 11
diags.toLowerCase (). contains (diagnostic [50].toLowerCase () ) |।
diags.toLowerCase (). contains (diagnostic [51].toLowerCase () ) II
diags.toLowerCase (). contains (diagnostic [52].toLowerCase () ) )
$\{$
int updateStatus=-1;
if (test)
\{
System.out. println(" patient_id=" + patient_id); System.out. println("_start_time=" + start_time);
\}
cardio.setInt (1, 1);
cardio.setInt(2, patient_id);
cardio.setTimestamp (3, start_time);
updateStatus=cardio.executeUpdate () ;
cardioCount ++;
if (test) System.out. println("„Update_Status=" + updateStatus);
break;
\} // end if diags.
\} // end if diagnostics_date before start_time
else
\{
 ergo: \% $\%$ tF", patient_id, diagnosis_date));
\} // end if diagnostics_date before start_time

```
            } // end else for HashMap ...
    } // end for HashMap
    System.out.println(String.format( " «%d_ Patients_had_no_diagnosis",
        no_diag_count ));
    System.out.println(String.format(" "%d_Patients_had_heart-Problems",
        cardioCount ));
    } // end Method
    public static void main(String[] args) throws Exception
    {
        RefactorDiagnosisDB dbc = new RefactorDiagnosisDB();
        dbc.runMethod();
    }
}
```


## Appendix D

## Java program to integrate the medication in Table maindata

```
import java.sql.Connection;
import java.sql.Date;
import java.sql.DriverManager;
import java.sql.PreparedStatement;
import java.sql.ResultSet;
import java.sql.SQLException;
import java.sql.Statement;
import java.sql.Timestamp;
import java.util.ArrayList;
import java.util.HashMap;
import java.util.TreeMap;
import java.util.regex.Pattern;
// Program RefactorMedDB.java
// The colums "statin" and "betablocker" will be appended in table
    "maindata".
// For each ergometry in the table "maindata" the table "medication"
    will be scanned for the substrings "statin" and "betablocker".
// The drugs to be considered are stored in the string-arrays "statine"
        and betablocker.
// Is the date of the intake of the drug bofore the date of beginning
        of the ergometry, will this be marked in the particular columne.
public class RefactorMedDB {
    Connection db;
    boolean test = false; // for testprints
    private ArrayList<HashMap<String, Object>> maindata;
    private ArrayList<HashMap<String, Object>> medication;
    private ArrayList<HashMap<String, Object>> diagnosis;
// Constructor refactorDB. in main wird mit new das Object dbc erzeugt.
// runMethod ist eine Methode des Objectes dbc.
    public RefactorMedDB() throws SQLException
    {
```

```
    try
    {
        // The newInstance() call is a work around for some broken Java
                implementations
        Class.forName("com.mysql.jdbc.Driver").newInstance ();
    } catch (Exception ex)
    {
        // handle the error
    }
    String username = "sqluser";
    String password = "sqluser";
    db = DriverManager.getConnection(
        "jdbc:mysql:/ / localhost:3306/ergometry?autoReconnect=true&
            useSSL=false",
        username, password);
        maindata = loadAllRows("maindata");
        medication = loadAllRows("medication");
        diagnosis = loadAllRows("diagnosis");
    } // end RefactorMedDB
    ArrayList<HashMap<String, Object>> loadAllRows(String table) throws
        SQLException
    {
        PreparedStatement ps = db.prepareStatement("SELECT **_FROM " + table
        );
    ResultSet rs = ps.executeQuery();
    java.sql.ResultSetMetaData md = rs.getMetaData();
    int columns = md.getColumnCount();
    ArrayList<HashMap<String, Object>> ret = new ArrayList<>();
    while (rs.next())
    {
        HashMap<String, Object> row = new HashMap();
        ret.add(row);
        for (int i = 1; i <= columns; i++)
        {
            row.put(md.getColumnName(i), rs.getObject(i));
        }
    }
    return ret;
} // end ArrayList
//
// Method runMethod
    public void runMethod() throws SQLException
    {
// 18 statines has been found in the Austrian Codex.
    String[] statine = new String[18];
    statine[0] = "Atorvadivid";
    statine[1] = "Atorvalan";
    statine[2] = "Atorvastatin";
    statine[3] = "Atozet";
    statine[4] = "Crestor";
```

```
    statine[5] = "Fluvastatin";
    statine[6] = "Gerosim";
    statine[7] = "Inegy";
    statine[8] = "Lovastatin";
    statine[9] = "Nyzoc";
    statine[10] = "Panchol";
    statine[11] = "Pravastatin";
    statine[12] = "Simvastad";
    statine[13] = "Simvarcana";
    statine[14] = "Simvastatin";
    statine[15] = "Simvatin";
    statine[16] = "Sortis";
    statine[17] = "Zocord";
    String[] betablocker = new String[29];
// Beta blocker without cardioselectivity
    betablocker[0] = "Carvedilol";
    betablocker[1] = "Dilatrend";
    betablocker[2] = "Hemangiol";
    betablocker[3] = "Inderal";
    betablocker[4] = "Sotacor";
    betablocker[5] = "Sotahexal";
    betablocker[6] = "Sotastad";
// Beta blocker with relative cardioselectivity
    betablocker[7] = "Atehexal";
    betablocker[8] = "Atenolan";
    betablocker[9] = "Atenolol";
    betablocker[10] = "Beloc";
    betablocker[11] = "Bilokord";
    betablocker[12] = "Bisocor";
    betablocker[13] = "Bisoprolol";
    betablocker[14] = "Bisostad";
    betablocker[15] = "Brevibloc";
    betablocker[16] = "Concor";
    betablocker[17] = "Esmolol";
    betablocker[18] = "Hypoloc";
    betablocker[19] = "Lanoc";
    betablocker[20] = "Metohexal";
    betablocker[21] = "Metoprolol";
    betablocker[22] = "Metoprololsuccinat";
    betablocker[23] = "Nebivolol";
    betablocker[24] = "Nomexor";
    betablocker[25] = "Rapibloc";
    betablocker[26] = "Rivacor";
    betablocker[27] = "Seloken";
    betablocker[28] = "Tenormin";
String meds;
    if(!maindata.iterator().next().containsKey("statin"))
    {
            Statement stmt = db.createStatement();
            stmt.execute("ALTER_TABLE_maindata_ADD_COLUMN_statin__INT(1)");
    }
    if(!maindata.iterator().next().containsKey("betablocker"))
    {
```

```
    Statement stmt = db.createStatement();
    stmt.execute("ALTER_TABLE_maindata_ADD_COLUMN_betablocker_INT(1)"
        );
    }
    TreeMap<Integer, ArrayList<HashMap<String, Object >>>
        idxPIDMedication;
    idxPIDMedication = new TreeMap <>();
    for(HashMap<String, Object> row : medication)
    {
    Integer patient_id = (Integer) row.get("patient_id");
    ArrayList<HashMap<String, Object >> list = idxPIDMedication.get(
        patient_id);
    if(list == null)
    {
        list = new ArrayList<>();
        idxPIDMedication.put(patient_id, list);
    }
    list.add(row);
} // for HashMap ... medication
// Question marks are placeholder in the SQL-Statement. They will be
replaced with actual values with the method statim.setInt(ind,
value)
PreparedStatement statin = db.prepareStatement("UPDATE maindata SET
        s statin
PreparedStatement betablock = db.prepareStatement("UPDATE maindata
        SET_betablocker 
int statinCount = 0, betablockerCount = 0, no_med_count = 0;
for(HashMap<String, Object> mainrow : maindata)
{
    Integer patient_id = (Integer) mainrow.get("patient_id");
    Timestamp start_time = (Timestamp) mainrow.get("start_time");
    boolean hasStatin = false, hasBetablocker = false;
    ArrayList<HashMap<String, Object>> medlist = idxPIDMedication.get
            (patient_id);
    if(medlist == null)
    {
        no_med_count++;
    }
    else for(HashMap<String, Object> medication : medlist)
    {
        Date medication_date = (Date) medication.get("medication_date")
        Integer medication_id = (Integer) medication.get("medication_id
            ");
        String smedication = (String) medication.get("medication");
        if ( smedication.indexOf("„") < 0)
```

```
    {
        meds = smedication;
    }
    else
    {
        meds = smedication.substring(0, smedication.indexOf("Ч"));
    }
    if (test)
    System.out.println( "index =" + smedication.indexOf(" "')+ " " + +
        smedication);
    if(medication_date == null || medication_id == null) continue;
// check for statines
    if( meds.equalsIgnoreCase(statine[0]) ||
        meds.equalsIgnoreCase(statine [1]) ||
        meds.equalsIgnoreCase(statine[2]) ||
        meds.equalsIgnoreCase(statine[3]) ||
        meds.equalsIgnoreCase(statine [4]) ||
        meds.equalsIgnoreCase(statine[5]) ||
        meds.equalsIgnoreCase(statine [6]) ||
        meds.equalsIgnoreCase(statine [7]) ||
        meds.equalsIgnoreCase(statine[8]) ||
        meds.equalsIgnoreCase(statine [9]) ||
        meds.equalsIgnoreCase(statine[10]) ||
        meds.equalsIgnoreCase(statine[11]) ||
        meds.equalsIgnoreCase(statine[12]) ||
        meds.equalsIgnoreCase(statine[13]) ||
        meds.equalsIgnoreCase(statine [14]) ||
        meds.equalsIgnoreCase(statine[15]) ||
        meds.equalsIgnoreCase(statine[16]) ||
        meds.equalsIgnoreCase(statine[17]) )
    {
        if( medication_date.before(start_time))
        {
            hasStatin = true;
        else
    {
        System.out. println(String.format("Patient %/%d_took afterer
            ergo:`%tF", patient_id, medication_date));
        }
        } // meds.equalsIgnoreCase(statine ...
// check for beta blocker
    if( meds.equalsIgnoreCase(betablocker[0]) ||
        meds.equalsIgnoreCase(betablocker[1]) ||
        meds.equalsIgnoreCase(betablocker[2]) ||
        meds.equalsIgnoreCase(betablocker[3]) ||
        meds.equalsIgnoreCase(betablocker[4]) ||
        meds.equalsIgnoreCase(betablocker[5]) ||
        meds.equalsIgnoreCase(betablocker[6]) ||
        meds.equalsIgnoreCase(betablocker[7]) ||
        meds.equalsIgnoreCase(betablocker[8]) ||
        meds.equalsIgnoreCase(betablocker[9]) ||
```

meds.equalsIgnoreCase(betablocker[10]) |।
meds.equalsIgnoreCase (betablocker[11]) |।
meds.equalsIgnoreCase (betablocker[12]) ||
meds.equalsIgnoreCase (betablocker[13]) |।
meds. equalsIgnoreCase (betablocker[14]) |।
meds.equalsIgnoreCase (betablocker[15]) |।
meds.equalsIgnoreCase (betablocker[16]) |।
meds.equalsIgnoreCase (betablocker[17]) |।
meds.equalsIgnoreCase (betablocker[18]) |।
meds.equalsIgnoreCase (betablocker[19]) |।
meds.equalsIgnoreCase (betablocker[20]) II
meds.equalsIgnoreCase (betablocker[21]) |।
meds.equalsIgnoreCase (betablocker[22]) II
meds.equalsIgnoreCase (betablocker[23]) |।
meds.equalsIgnoreCase (betablocker[24]) |।
meds.equalsIgnoreCase (betablocker[25]) |।
meds.equalsIgnoreCase (betablocker[26]) |।
meds.equalsIgnoreCase (betablocker[27]) |।
meds.equalsIgnoreCase (betablocker[28]) )
$\{$
if( medication_date.before(start_time)) \{
hasBetablocker = true;
else
\{

ergo: \% $\%$ tF", patient_id, medication_date));
\}
\} // meds.equalsIgnoreCase(betablocker ...
\} // else for HashMap ... medlist
if (hasStatin)
$\{$
statin.setInt (1, 1);
statin.setInt(2, patient_id);
statin.setTimestamp (3, start_time);
statin.executeUpdate () ;
statinCount ++;
\}
if (hasBetablocker)
\{
betablock.setInt(1, 1);
betablock.setInt(2, patient_id);
betablock.setTimestamp (3, start_time);
betablock. executeUpdate () ;
betablockerCount ++;
\}
\} // end for hashMap ... maindata
System.out. println (String.format("\%d_Patients ${ }_{\bullet}$ took_nothing",
no_med_count )) ;
System.out. println (String.format ("\%d_Patients took $_{\lrcorner}$statin",
statinCount ));
System.out.println (String.format("\%d_Patients took betablocker",
betablockerCount ));
public static void main(String[] args) throws Exception
\{
RefactorMedDB $\mathrm{dbc}=$ new RefactorMedDB();
dbc.runMethod ();
\} // end main
\} // end class RefactorMedDB

## Appendix E

## Java program to integrate the laboratory in Table maindata

```
import java.sql.Connection;
import java.sql.DriverManager;
import java.sql.SQLException;
import java.sql.PreparedStatement;
import java.sql.ResultSet;
import java.sql.Statement;
import java.lang.*;
import java.io.*;
import java.util.*;
import java.text.*;
// Program RefactorLabDB.java
// This Programm searches for each ergometry in the table "maindata"
    for labvalues in the table "lab", which have been taken in the
    range +/- 14 days of the start of the ergometry.
// Within this range that value will be taken, which is nearest to the
    start of the ergometry.
// The scaned value and the corresponding flag will be inserted into
    the table "maindata".
public class RefactorLabDB
{
    public static void main(String[] args)
    {
        Database db = new Database();
        try
        {
            boolean test = true;
            db.connect(); // open database
            System.out.println(" ");
            if (test) {System.out.println("__Die_Datenbank_isttverbunden_!")
                ;}
            db.read(); // evaluate data
            catch (Exception e)
        {
            e.printStackTrace();
            return;
```

```
    }
        db.close();
    } // end main
} // end class
//
class Database
    {
        private Connection con = null;
        private Statement stateMaindata = null;
        private Statement stateLab = null;
        private ResultSet reslab = null;
        private ResultSet resmain = null;
        private String string, device, sex;
        private String datum;
        private boolean update = false;
        private boolean test = false; // if true, activate testprints
        public void connect() throws Exception
        {
            if(con != null) return;
            try
            {
                    Class.forName("com.mysql.jdbc.Driver");
            } catch (ClassNotFoundException e)
            {
```



```
                +
                    "$&sudo_apt-get install_libmysql-java\n" +
                    "den_Driver installieren_und_die_Environment-Variable
                    "CLASSPATH_setzen mit:\n" +
            " export_CLASSPATH=\n" +
            "/Directory/von/TestDB:/usr/share/java/mysql-connector-java
                .jar");
            }
            String connectionURL =
            "jdbc:mysql:// localhost/ergometry?autoReconnect=true&useSSL=
                false";
            con = DriverManager.getConnection(connectionURL, "sqluser", "
                sqluser");
            return;
    } // end connect
//
//
    public void read() throws Exception
    {
        Calendar dateMin, dateMax = Calendar.getInstance();
        Calendar calMain = Calendar.getInstance();
        Calendar calLab = Calendar.getInstance();
        Calendar calMin = Calendar.getInstance();
        Calendar calMax = Calendar.getInstance();
        DateFormat format1, format2;
```

```
    Date dateMain=null, dateLab=null;
    int[] array_CHOL = new int[20];
    float[] array_CREA = new float[20];
    int[] array_HDL = new int[20];
    float[] array_HSRE = new float[20];
    float[] array_LDL = new float[20];
    int[] array_NBZ = new int[20];
int[] array_TRIGL = new int[20];
String[] labWerte = new String[7];
String[] flags = new String[7];
    long[] AtimeDiff = new long[20];
    long[] AtimeDiffMin = new long[20];
    int[] AindMin = new int[20];
    int ind=0;
    long timeDiff=0;
    long[] timeDiffMin = new long[7];
    int CHOL=0, CREA=1, HDL=2, HSRE=3, LDL=4, NBZ=5, TRIGL=6;
    int id=0, pid=0, record_nr=0, noLabData =0;
    format1 = new SimpleDateFormat("yyyy-MM-dd_HH:mm: ss");
    format2 = new SimpleDateFormat("yууу-MM-dd");
// timeDiffMin must be initialized with a time-value of 14 days (in ms)
    for (int i=0; i<7; i++)
    {
        timeDiffMin[i] = 1210000000;
        flags[i] = null;
    }
    try
    {
        stateMaindata = con.createStatement();
        stateLab = con.createStatement();
        if (stateMaindata != null)
        {
            System.out.println(" "_Das_SQL-Object_wurde_instantiiert\n");
        }
    resmain = stateMaindata.executeQuery("SELECT**&FROM_maindata;")
        ;
// With object.next() the focus will be set to the next line.
// Within a record the data will be read by her columne-name possible
    methods are:
// obj.getString("name"), obj.GetInt("name")), obj.getFloat("name")
    record_nr = 0;
    while (resmain.next())
    {
    record_nr = record_nr + 1;
    if (test) {System.out.println(" "Patientenrecord_" + record_nr)
        ;}
    int pidm = resmain.getInt("patient_id");
```

```
        String datumMain = resmain.getString("start_time");
// To be able to calculate with a date, it must be existent in the
        Calendar-Format.
// The conversion of a string into the Calendar-format has to be done
        via the Date-format: String ->> Date-format ->> Calendar-format.
// With the method getTime() the type Calendar will be converted into
        the type Date.
// Example for Calendar to Date: Date dateM = calMax.getTime(string);
// Example for Date to Calendar: Calendar calMax.setTime(dateMain);
// Only the type Date can be converted into a String. This string is
    necessary in the SQL-SELECT-Statement for comparison of time.
        dateMain = format1.parse(datumMain); // string to Date-format
        calMax.setTime(dateMain); // Date+format to Calendar-
        format
        calMin.setTime(dateMain); // Date+format to Calendar-
        format
        calMax.add(Calendar.DAY_OF_MONTH, 14);
        calMin.add(Calendar.DAY_OF_MONTH, -14);
        String sdateMin = format2.format(calMin.getTime());
        String sdateMax = format2.format(calMax.getTime());
// The variables for the lab-data must be initialized for each
    ergometry
        if (test) {System.out.println(""کWerte_werden
        for (int i=0; i<7; i++)
        {
        timeDiffMin[i] = 1210000000;
        flags[i] = null;
        labWerte[i] = null;
    }
        if (test)
        {
        System.out.println(")Suchbereich %" + sdateMin + "_bis_" +
                sdateMax);
        System.out.println("");
        System.out. println(")
        System.out.println(",ZZit, des_Pat.Records=_" + datumMain);
        System.out.println("");
```



```
            ;
    }
// The time-strings in the SELECT-Statement must be enclosed by single
    quotes ('yyyy-MMAdd')
        String sel1 = "SELECT_*_FROM_lab_WHERE_patient_id=" + pidm;
        String sel2 = "„and_lab_date_>>" + "'" + sdateMin + "'";
        String sel3 = "_and_lab_date_<<" + "'" + sdateMax + "'"';
        String selectstring = sel1 + sel2 + sel3 ;
        if (test) {System.out.println(")Select-String=\n" +
```

```
selectstring);}
// reslab is an objekt of Typ ResultSet, in which the results will be
    stored.
reslab = stateLab.executeQuery(selectstring);
ind =0;
update=false;
while (reslab.next())
{
    ind=ind +1;
    if (test) {System.out.println("\n_`■nächster_Record,_ind=" +
                ind);}
    String datumlab = reslab.getString("lab_date");
    dateLab = (Date)format2.parse(datumlab);
    calLab.setTime(dateLab);
    timeDiff = Math.abs(dateMain.getTime() - dateLab.getTime() );
    id = reslab.getInt("patient_id");
    pid = reslab.getInt("entry_id");
    String parameter = reslab.getString("parameter");
    String wert = reslab.getString("lab_value");
    String flag = reslab.getString("evaluation");
    if (test)
    {
        System.out.println("&ZZeitoffset_in ■ms=" + timeDiff);
        System.out.println(""ь" + pid+ "\t" + id +
            "\t" + datumlab + "\t" + parameter + "\t" + wert + "\t" +
                    flag);
    }
        switch (parameter)
        {
            case "CHOL":
            if (timeDiff < timeDiffMin[CHOL])
            {
                labWerte[CHOL] = wert;
                    flags[CHOL]="'" + flag + "'";
                timeDiffMin[CHOL] = timeDiff;
                    update = true;
        }
            break;
        case "CREA":
        if (timeDiff < timeDiffMin[CREA])
        {
            labWerte[CREA] = wert;
            flags[CREA]="'" + flag + "'";
            timeDiffMin[CREA] = timeDiff;
            update = true;
        }
            break;
        case "HDL":
        if (timeDiff < timeDiffMin [HDL])
        {
```

```
            labWerte[HDL] = wert;
            flags[HDL]="'" + flag + "'";
            timeDiffMin[HDL] = timeDiff;
            update = true;
        }
            break;
        case "HSRE":
        if (timeDiff < timeDiffMin[HSRE])
        {
            labWerte[HSRE] = wert;
            flags[HSRE]="'" + flag + "'";
            timeDiffMin[HSRE] = timeDiff;
            update = true;
        }
            break;
        case "LDL":
        if (timeDiff < timeDiffMin[LDL])
        {
            labWerte[LDL] = wert;
            flags[LDL]="'" + flag + "'";
            timeDiffMin[LDL] = timeDiff;
            update = true;
        }
            break;
        case "NBZ":
        if (timeDiff < timeDiffMin[NBZ])
        {
            labWerte[NBZ] = wert;
            flags[NBZ]="'" + flag + "'";
            timeDiffMin [NBZ] = timeDiff;
            update = true;
        }
            break;
        case "TRIGL":
        if (timeDiff < timeDiffMin[TRIGL])
        {
            labWerte[TRIGL] = wert;
            flags[TRIGL]="'" + flag + "'";
            timeDiffMin[TRIGL] = timeDiff;
            update = true;
        }
                    break;
    } // end switch
} // end while lab
if (test)
{
        System.out.println("\n_பேAktuellste_Laborwerte");
```



```
        System.out.println(",Evaluation_" + flags[0]);
        System.out.println("_Tagesoffset:" + timeDiffMin
        [0]/(24*3600*1000));
```



```
    System.out.println("_Evaluation_:" + flags[1]);
    System.out.println("_Tagesoffset:" + timeDiffMin
        [1]/(24*3600*1000));
```


System.out.println(" ${ }_{\square}$ Evaluation $: "+$ flags [2]); System.out. println(" ${ }^{\text {пь }}$ Tagesoffset:" + timeDiffMin [2]/(24*3600*1000));


System.out. println(" ${ }^{\text {■ }}$ Tagesoffset:" + timeDiffMin [3]/ $(24 * 3600 * 1000))$;

System.out.println(" ${ }_{\square}$ Evaluation $: "+$ flags [4]);
System.out. println(" Tـت Tagesoffset:" + timeDiffMin [4]/(24*3600*1000));
 System.out.println(" ${ }_{-}$Evaluation $\left.: ~ " ~+~ f l a g s[5]\right) ; ~$ System.out. println(" Tagesoffset:" + timeDiffMin [5]/(24*3600*1000));

 System.out. println(" Tagesoffset:" + timeDiffMin [6]/(24*3600*1000));
\}

String selectstringu1 = "UPDATE maindata SET"; $_{\checkmark}$;

";



;




for (int $\mathrm{i}=0 ; \mathrm{i}<7$; $\mathrm{i}++$ )
\{
System.out. println("flags(i)=" + flags[i]);
if (flags[i] == "null") \{flags[i]="NULL";\};
\}
String selectstringUpdate $=$ selectstringu1 +
selStringu11 + flags [0] +
selStringu21 + flags[1] +
selStringu31 + flags [2] +
selStringu41 + flags[3] +
selStringu51 + flags[4] +
selStringu61 + flags[5] +
selStringu71 + flags[6] +
selectstringu8;
if (test)


```
                    Laborwerte=\n" + selectstringUpdate);
            }
            if (update)
            System.out.println("
```

$\qquad$

``` Labordaten_bei patient_id=_" + pidm
                );
            int status = stateLab.executeUpdate(selectstringUpdate);
            } else
            {
                noLabData++;
                System.out.println("Keine_Labordaten_bei_patient_id=_" + pidm
                    );
            }
            } // end while maindata
        } // end try
            catch (Exception e)
            {
                throw e;
            }
            System.out.println("\nAnzahl_Ergometrie-Datensätze,
```

$\qquad$

```
                                    =" +
            record_nr);
System.out.println("Anz._Ergometrie-Datensätze_ohne_Labor=" +
            noLabData);
            System.out.println("\n");
            return;
    } // end function read
    public void close()
    {
        if(con != null)
        {
            try
            {
                con.close();
            } catch (SQLException e)
            {
                e.printStackTrace();
            }
        }
    } // end close
} // end class Database
```


## Appendix F

## R script for adjusting the tables

```
#reading the data form the data base
library(DBI)
mydb = dbConnect(RMySQL::MySQL(), user='sqluser', password='sqluser',
    dbname='ergometry', host='127.0.0.1 ')
maindata <- dbReadTable(conn = mydb, name = 'maindata')
#calculating additional variables
maindata$bmi<-maindata$weight/(maindata$height/100)^2
maindata$waist_to_height_ratio<-maindata$waist/maindata$height
maindata$workload_to_weight_ratio<-maindata$workload/maindata$weight
maindata$TCtoHDL<-maindata$CHOL/maindata$HDL
maindata$LDLtoHDL<-maindata$LDL/maindata$HDL
maindata$TGtoHDL<-maindata$TRIGL/maindata$HDL
maindata$date <- as.Date(maindata$start_time, '%Y-%m-%d')
maindata$year <- format(as.Date(maindata$start_time, format="%Y-%m-%d")
    ,"%Y")
maindata$surface<-0.007148* maindata$weight^0.425*maindata$ height^0.725
maindata$reg_paper_men<-6.773+136.141*maindata$surface - 0.916*maindata$
    surface* maindata$age
maindata$reg_paper_women<-3.933+86.641*maindata$surface - 0.346* maindata$
    surface*maindata$age
#creating values for regression from paper
for (i in 1:dim(maindata)[1]){
    maindata$reg_mod1[i]<-NA
}
for (i in 1:dim(maindata)[1]){
    if (maindata$gender[i]== 'MALE') {
        maindata$reg_mod1[i ]<-93.19284+105.67996*maindata$surface[i
            ] -1.09894*maindata$surface [ i ] * maindata$age [ i ]
    }
    if (maindata$gender[i]== 'FEMALE') {
        maindata$reg_mod1[i ]<-67.2302+83.0788*maindata$surface[i] - 0.9214*
                maindata$surface[i] * maindata$age[i ]
    }
}
#creating column for medication
for (i in 1:dim(maindata)[1]){
        maindata$medication[i]<-NA
}
```

```
for (i in 1:dim(maindata)[1]){
    if (is.na(maindata$statin[i])&&is.na(maindata$betablocker[i])){
        maindata$medication[i]<-0
    }
    if (!is.na(maindata$statin[i])){
        maindata$medication [ i ]<-1
    }
    if (!is.na(maindata$betablocker[i])){
        maindata$medication [ i ]<-2
    }
    if (!is.na(maindata$ statin[i])&&!is.na(maindata$betablocker[i])){
        maindata$medication [ i ]<-3
    }
}
#creating binary column for medication
for (i in 1:dim(maindata)[1]){
    maindata$medication_binary[i]<-NA
}
for (i in 1:dim(maindata)[1]){
    if (maindata$medication [i]==0){
        maindata$medication_binary[i]<-0
    }
    else {
        maindata$medication_binary [ i ] <-1
    }
}
#creating column for diagnosis
for (i in 1:dim(maindata)[1]){
    maindata$diagnosis_binary[i]<-NA
}
for (i in 1:dim(maindata)[1]){
    if (is.na(maindata$kardio[i])){
        maindata$diagnosis_binary[i]<-0
    }
    else{
        maindata$diagnosis_binary[i]<-1
    }
}
#data for rehabilitation
data_rehab <- maindata[ which((maindata$reason_for_study=='Phase_II_EU'
        )|
                                (maindata$reason_for_study== ' Phase_ \II L
                                    AU')।
                                (maindata$reason_for_study== 'Phase_III _
                                    EU')।
                                    (maindata$reason_for_study== ' Phase_汭
                                    ZU' )|
                                (maindata$reason_for_study== ' Phase_III _
                                    AU')),]
#creating data for stage 2
data_stage2 <- subset(maindata,(maindata$reason_for_study== 'Phase_II_EU
```

'।
dim(data stage2) [1]
data_stage 2 _duration $<-$ data.frame (patient_id $=$ unique (data_stage $2 \$$
patient_id))
for (i in 1:dim(data_stage2_duration) [1]) \{
data_stage2_duration\$date_EU[i]<-NA
data_stage2_duration\$date_AU[ i ]<-NA
data_stage 2 _duration $\$$ duration [ i$]<-\mathrm{NA}$
data_stage2_duration\$workload_max_EU[ i ]<-NA
data_stage2_duration\$gender[i]<-NA
data_stage2_duration \$age[i]<-NA
data_stage2_duration \$weight [i]<-NA
data_stage2_duration\$height [i]<-NA
data_stage2_duration \$waist [i]<-NA
data_stage2_duration \$bmi[i]<-NA
data_stage2_duration\$waist_to_height_ratio[i]<-NA
data_stage2_duration \$workload_to_weight_ratio[i]<-NA
data_stage2_duration\$systolicbp_rest[i]<-NA
data_stage2_duration\$diastolicbp_rest[i]<-NA
data_stage2_duration\$hr_rest[i]<-NA
data_stage2_duration \$ workload_max_AU[ i ]<-NA
data_stage2_duration \$CHOL[i]<-NA
data_stage2_duration\$e_CHOL[i]<-NA
data_stage2_duration \$CREA[i]<-NA
data_stage2_duration \$e_CREA[i]<-NA
data_stage2_duration \$HDL[ i $]<-$ NA
data_stage2_duration \$e_HDL[ i ]<-NA
data_stage2_duration $\$ 2 \mathrm{DL}[\mathrm{i}]<-\mathrm{NA}$
data_stage2_duration\$e_LDL[i]<-NA
data_stage2_duration \$HSRE[i]<-NA
data_stage2_duration\$e_HSRE[i]<-NA
data_stage2_duration \$NBZ[i]<-NA
data_stage2_duration\$e_NBZ[i]<-NA
data_stage2_duration \$TRIGL[i]<-NA
data_stage2_duration\$e_TRIGL[i]<-NA
for ( j in 1: $\operatorname{dim}($ data_stage 2$)[1])\{$
if (data_stage 2 \$patient_id[j]==data_stage2_duration\$patient_id[i] \&
\& data_stage $2 \$$ reason_for_study[j]== 'Phase_II_EU' \&\& is .na(data_
stage2_duration\$date_EU[j]))\{
data_stage2_duration \$date_EU[i]<-data_stage2\$date[j]
data_stage2_duration\$workload_max_EU[ $\bar{i}]<-$ data_stage2 ${ }^{\text {\$ }}$ workload_max
[ j ]
data_stage2_duration\$gender[i]<-data_stage2\$gender[j]
data_stage2_duration \$age[i]<-data_stage2\$age[j]
data_stage2_duration \$weight[i]<-data_stage2\$weight [j]
data_stage2_duration \$height $[i]<-$ data_stage2 \$height $[j]$
data_stage2_duration\$waist[i]<-data_stage2\$waist[j]
data_stage2_duration $\$$ bmi[i]<-data_stage $2 \$ b m i[j]$
data_stage2_duration\$waist_to_height_ratio[i]<-data_stage2\$waist_
to_height_ratio[j]
data_stage2_duration\$workload_to_weight_ratio[i]<-data_stage2\$
workload_to_weight_ratio[j]
data_stage2_duration\$systolicbp_rest[i]<-data_stage2\$systolicbp_
rest [j]
data_stage2_duration\$diastolicbp_rest[i]<-data_stage2\$diastolicbp

```
                _rest[j]
            data_stage2_duration$hr_rest[i]<-data_stage2$hr_rest[j]
            data_stage2_duration $CHOL[ i ]<-data_stage2 $CHOL[j ]
            data_stage2_duration$e_CHOL[i ]<-data_stage2$e_CHOL[j ]
            data_stage2_duration$CREA[i ]<-data_stage2 $CREA[j]
            data_stage2_duration$e_CREA[i]<-data_stage2$e_CREA[j]
            data_stage2_duration$HDL[i]<-data_stage2$HDL[j]
            data_stage2_duration$e_HDL[i]<-data_stage2$e_HDL[j]
            data_stage2_duration$LDL[i]<-data_stage2$$DL[j]
            data_stage2_duration$e_LDL[i]<-data_stage2$e_LDL[j]
            data_stage2_duration$HSRE[i]<-data_stage2$HSRE[j]
            data_stage2_duration$e_HSRE[i]<-data_stage2$e_HSRE[j]
            data_stage2_duration$NBZ[ i ]<-data_stage2 $NBZ[j ]
            data_stage2_duration$e_NBZ[i]<-data_stage2$e_NBZ[j]
            data_stage2_duration$TRIGL[i ]<-data_stage2$TRIGL[j ]
            data_stage2_duration$e_TRIGL[i]<-data_stage2$e_TRIGL[j]
        }
    }
    for (j in 1:dim(data_stage2)[1]){
    if (data_stage2$patient_id[j]== data_stage2_duration$patient_id[i] &
            & data_stage2$reason_for_study[j]== 'Phase_II_AU'&& is .na(data_
            stage2_duration$date_AU[j])){
            data_stage2_duration$date_AU[i]<--data_stage2$date[j]
            data_stage2_duration$workload_max_AU[i]<-data_stage2$workload_max
                [ j]
            if(is.na(data_stage2_duration$gender[i])){
                data_stage2_duration$gender[i]<-data_stage2$ $gender[j]
            }
    }
    }
    data_stage2_duration$duration[i]<-data_stage2_duration$date_AU[i]-
        data_stage2_duration$date_EU[i]
    data_stage2_duration$improvement[i]<-data_stage2_duration$workload_
        max_AU[i]-data_stage2_duration$workload_max_EU[i ]
    }
# creating data for stage 3
data_stage3 <- subset(maindata,(maindata$reason_for_study=='Phase _III
    EU'| maindata$reason_for_study== 'Phase_III_ZU'| maindata$reason_for
    _study== 'Phase_III_AU'))
    dim(data_stage3)[1]
    data_stage3_duration <-
            data.frame(patient_id = unique(data_stage3$patient_id))
    dim(data_stage3_duration) [1]
    for (i in 1:dim(data_stage3_duration)[1]){
        data_stage3_duration$date_EU[i ]<-NA
        data_stage3_duration$date_ZU[i ]<-NA
        data_stage3_duration$date_AU[i ]<-NA
        data_stage3_duration$duration [i]<-NA
    data_stage3_duration$duration1[i]<-NA
    data_stage3_duration$duration2[i]<-NA
    data_stage3_duration$workload_max_EU[ i ]<-NA
    data_stage3_duration$workload_max_ZU[i]<-NA
    data_stage3_duration$workload_max_AU[i]<-NA
    data_stage3_duration$gender[i]<-NA
    data_stage3_duration$age[i]<-NA
    data_stage3_duration$weight[i]<-NA
    data_stage3_duration$height[i]<-NA
```

data_stage3_duration\$waist[i]<-NA
data_stage3_duration \$bmi[i]<-NA
data_stage3_duration\$waist_to_height_ratio[i]<-NA
data_stage3_duration \$workload_to_weight_ratio[i]<-NA
data_stage3_duration\$systolicbp_rest[i]<-NA
data_stage3_duration\$diastolicbp_rest[i]<-NA
data_stage3_duration\$hr_rest[i]<-NA
data_stage3_duration \$ workload_max_AU[ i ]<-NA
data_stage3_duration \$CHOL[ i ]<-NA
data_stage3_duration\$e_CHOL[ i ]<-NA
data_stage3_duration \$CREA[i]<-NA
data_stage3_duration\$e_CREA[i]<-NA
data_stage3_duration \$HDL[i]<-NA
data_stage3_duration\$e_HDL[ i ]<-NA
data_stage3_duration $\$ 2 \mathrm{DL}[\mathrm{i}]<-\mathrm{NA}$
data_stage3_duration \$e_LDL[ i ]<-NA
data_stage3_duration \$HSRE[ i $]<-$ NA
data_stage3_duration\$e_HSRE[i]<-NA
data_stage3_duration \$NBZ[i]<-NA
data_stage3_duration\$e_NBZ[i]<-NA
data_stage3_duration \$TRIGL[i]<-NA
data_stage3_duration\$e_TRIGL[i]<-NA
for (j in 1:dim(data_stage3) [1]) \{
if (data_stage3\$patient_id[j]==data_stage3_duration\$patient_id[i] \& \& data_stage 3 \$reason_for_study [j]== 'Phase_III_EU')\{
data_stage3_duration\$date_EU[i]<-data_stage $\mathbf{\$ d a t e}[\mathrm{j}]$
data_stage3_duration \$workload_max_EU[i]<-data_stage3\$workload_max[j]
data_stage3_duration\$gender[i]<-data_stage3\$gender[j]
data_stage3_duration \$age[i]<-data_stage3\$age[j]
data_stage3_duration\$weight [i]<-data_stage3\$weight[j]
data_stage3_duration\$height[i]<-data_stage3\$height[j]
data_stage3_duration\$waist[i]<-data_stage3\$waist[j]
data_stage3_duration\$bmi[i]<-data_stage $3 \mathbf{\$ b m i}[j]$
data_stage3_duration\$waist_to_height_ratio[i]<-data_stage3\$waist_to_
height_ratio[j]
data_stage3_duration \$workload_to_weight_ratio [i]<-data_stage3 \$workload _to_weight_ratio [j]
data_stage3_duration\$systolicbp_rest[i]<-data_stage3\$systolicbp_rest[j
]
data_stage3_duration\$diastolicbp_rest[i]<-data_stage3\$diastolicbp_rest
[ j ]
data_stage3_duration\$hr_rest[i]<-data_stage3\$hr_rest[j]
data_stage3_duration \$CHOL[ $i$ ]<-data_stage 3 \$CHOL[ $j$ ]
data_stage3_duration\$e_CHOL[i]<-data_stage3\$e_CHOL[j]
data_stage3_duration \$CREA[i]<-data_stage 3 \$CREA[ j ]
data_stage3_duration\$e_CREA[i]<-data_stage3\$e_CREA[j]
data_stage3_duration \$HDL[i]<-data_stage3\$HDL[j]
data_stage3_duration\$e_HDL[i]<-data_stage3\$e_HDL[j]
data_stage3_duration \$LDL[i]<-data_stage 3 \$LDL[ $j$ ]
data_stage3_duration\$e_LDL[i]<-data_stage3\$e_LDL[j]
data_stage3_duration \$HSRE[i]<-data_stage3\$HSRE[j]
data_stage3_duration\$e_HSRE[i]<-data_stage3\$e_HSRE[j]
data_stage3_duration \$NBZ[i]<-data_stage3\$NBZ[j]
data_stage3_duration\$e_NBZ[i]<-data_stage3\$e_NBZ[j]
data_stage3_duration\$TRIGL[i]<-data_stage3\$TRIGL[j]
data_stage3_duration\$e_TRIGL[i]<-data_stage3\$e_TRIGL[j]
\}

```
}
for (j in 1:dim(data_stage2)[1]){
    if (data_stage2$patient_id[j]== data_stage3_duration$patient_id[i] &
            & (is.na(data_stage3_duration$date_EU[j])&&data_stage2$reason_
            for_study[j]== 'Phase_II_AU')){
            data_stage3_duration$date_EU[i]<--data_stage2$date[j]
            data_stage3_duration$workload_max_EU[i]<-data_stage2$workload_max
                [j]
            data_stage3_duration$gender[i]<-data_stage2$gender[j]
            data_stage3_duration$age[i]<-data_stage2$age[j]
            data_stage3_duration$weight[i]<-data_stage2$weight[j]
            data_stage3_duration$height[i]<-data_stage2$height[j]
            data_stage3_duration$waist[i]<-data_stage2$waist[j]
            data_stage3_duration$bmi[i]<-data_stage2$bmi[j]
            data_stage3_duration$waist_to_height_ratio[i]<-data_stage2$waist_
                    to_height_ratio[j]
            data_stage3_duration$workload_to_weight_ratio[i]<-data_stage2$
                workload_to_weight_ratio[j]
            data_stage3_duration$systolicbp_rest[i]<-data_stage2$systolicbp_
                rest[j]
            data_stage3_duration$diastolicbp_rest[i]<-data_stage2$diastolicbp
                _rest[j]
            data_stage3_duration$hr_rest[i]<-data_stage2$hr_rest[j]
            data_stage3_duration$CHOL[i ]<-data_stage2 $CHOL[j ]
            data_stage3_duration$e_CHOL[i ]<-data_stage2$e_CHOL[j ]
            data_stage3_duration$CREA[ i ]<-data_stage2 $CREA[ j ]
            data_stage3_duration$e_CREA[i]<-data_stage2$e_CREA[j ]
            data_stage3_duration$HDL[i]<-data_stage2 $HDL[j]
            data_stage3_duration$e_HDL[i ]<-data_stage2$e_HDL[j]
            data_stage3_duration$LDL[i]<-data_stage2 $LDL[j]
            data_stage3_duration$e_LDL[i]<-data_stage2$e_LDL[j]
            data_stage3_duration$HSRE[i ]<-data_stage2 $HSRE[j]
            data_stage3_duration$e_HSRE[i ]<-data_stage2$e_HSRE[j]
            data_stage3_duration$NBZ[ i ]<-data_stage2 $NBZ[j ]
            data_stage3_duration$e_NBZ[i]<-data_stage2$e_NBZ[j ]
            data_stage3_duration$$TRIGL[i ]<-data_stage2 $TRIGL[ j ]
            data_stage3_duration$e_TRIGL[i]<-data_stage2$e_TRIGL[j]
        }
}
for (j in 1:dim(data_stage3)[1]){
    if (data_stage3$patient_id[j]== data_stage3_duration$patient_id[i] &
                & data_stage3$reason_for_study[j]== 'Phase_ III_ZU'){
            data_stage3_duration$date_ZU[i]<-data_stage3$date[j]
            data_stage3_duration$workload_max_ZU[i]<-data_stage3$workload_max
                [ j]
    }
}
for (j in 1:dim(data_stage3)[1]){
    if (data_stage3$patient_id[j]== data_stage3_duration$patient_id[i] &
                & data_stage3$reason_for_study[j]== 'Phase_III_AU'){
            data_stage3_duration$date_AU[i]<-data_stage3$date[j]
data_stage3_duration$workload_max_AU[i ]<-data_stage3$workload_max[j]
if (is.na(data_stage3_duration$gender[i])){
    data_stage3_duration$gender[i]<-data_stage3$gender[j]
}
    }
}
```

data_stage3_duration\$duration [i]<-data_stage3_duration\$date_AU[i]data_stage3_duration\$date_EU[i]
data_stage3_duration\$duration1[i]<-data_stage3_duration\$date_ZU[i]data_stage3_duration \$date_EU[i]
data_stage3_duration\$duration2[i]<-data_stage3_duration\$date_AU[i]data_stage3_duration\$date_ZU[i]
data_stage3_duration \$improvement[i]<-data_stage3_duration\$workload_ $\boldsymbol{m a x}$ _AU[ i]-data_stage3_duration \$ workload_max_EU[ i ]
data_stage3_duration\$improvement1[i]<-data_stage3_duration\$workload_ $\boldsymbol{m a x}$ _ZU[i]-data_stage3_duration\$ workload_max_EU[i]
data_stage3_duration\$improvement2[i]<-data_stage3_duration\$workload_ $\boldsymbol{m a x}$ _AU[i]-data_stage3_duration\$workload_max_ZU[i]


[^0]:    ${ }^{1} 0 .$. man, $1 .$. woman

[^1]:    ${ }^{1}$ These lines are constructed by local polynomial regression fitting. For the documentation of the algorithm see (Cleveland et al., 1992]

[^2]:    ${ }^{2}$ The bias of an estimator is the difference between an estimator's expected value and the true value of the parameter.

